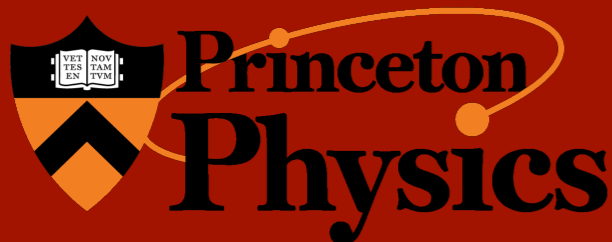


# The cosmological history of axion minihalos

**Malte Buschmann**  
Princeton University

10/29/2020  
Oklahoma State University



National Energy Research  
Scientific Computing Center

# Axions

- Axions originally introduced to solve the **strong CP problem**:

$$\mathcal{L} = \theta \frac{1}{16\pi^2} F_{\mu\nu}^a \tilde{F}^{\mu\nu a} \longrightarrow \mathcal{L}_{axion} = (\partial_\mu a)^2 + \frac{(a/f_a + \theta)}{32\pi^2} F \tilde{F}$$

- U(1) PQ symmetry **spontaneously broken** at high scale

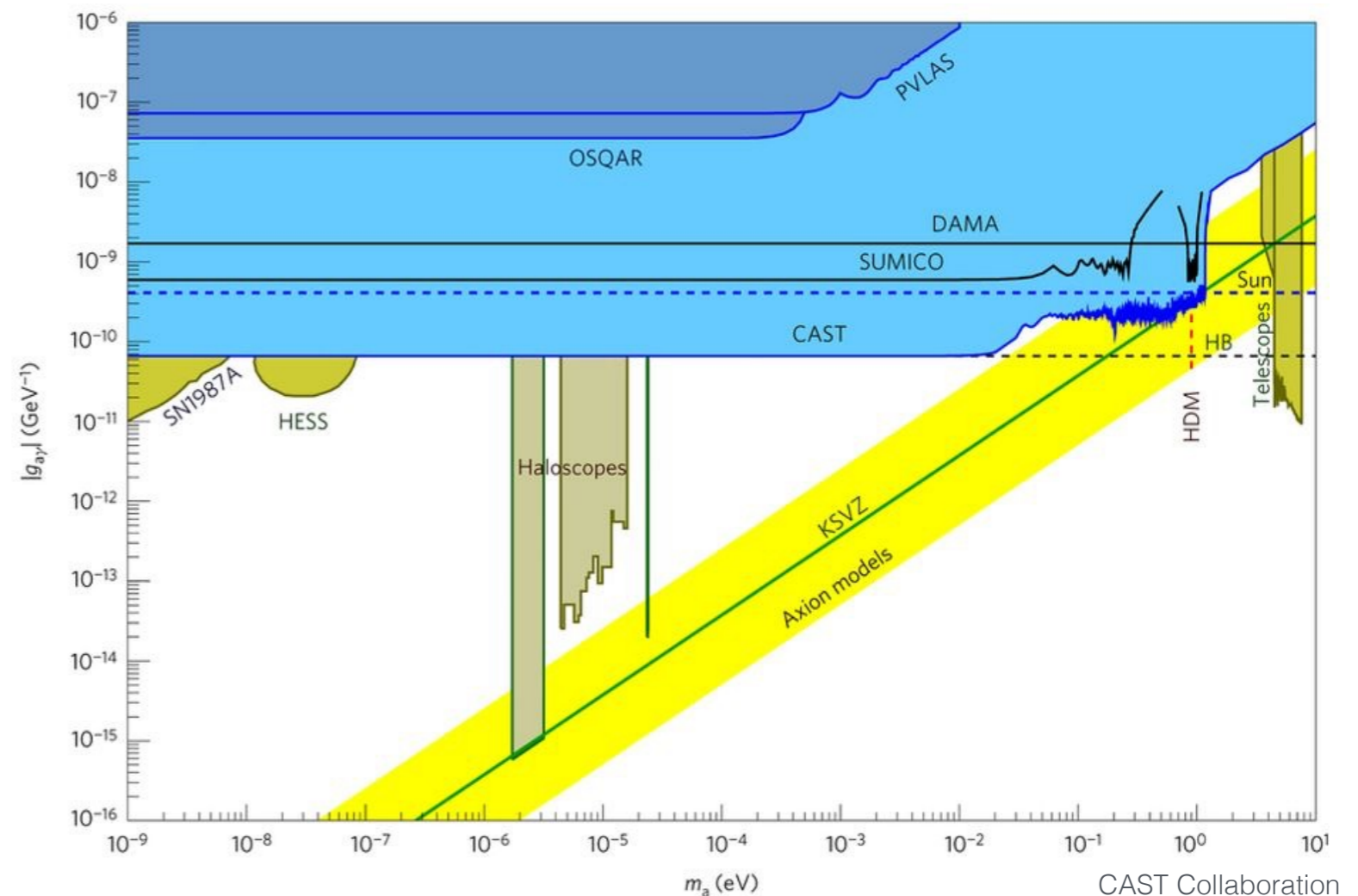
- **Axion mass** is small (QCD effects),

$$m_a^2 \approx \frac{m_\pi^2 f_\pi^2}{f_a^2}$$

as are its couplings

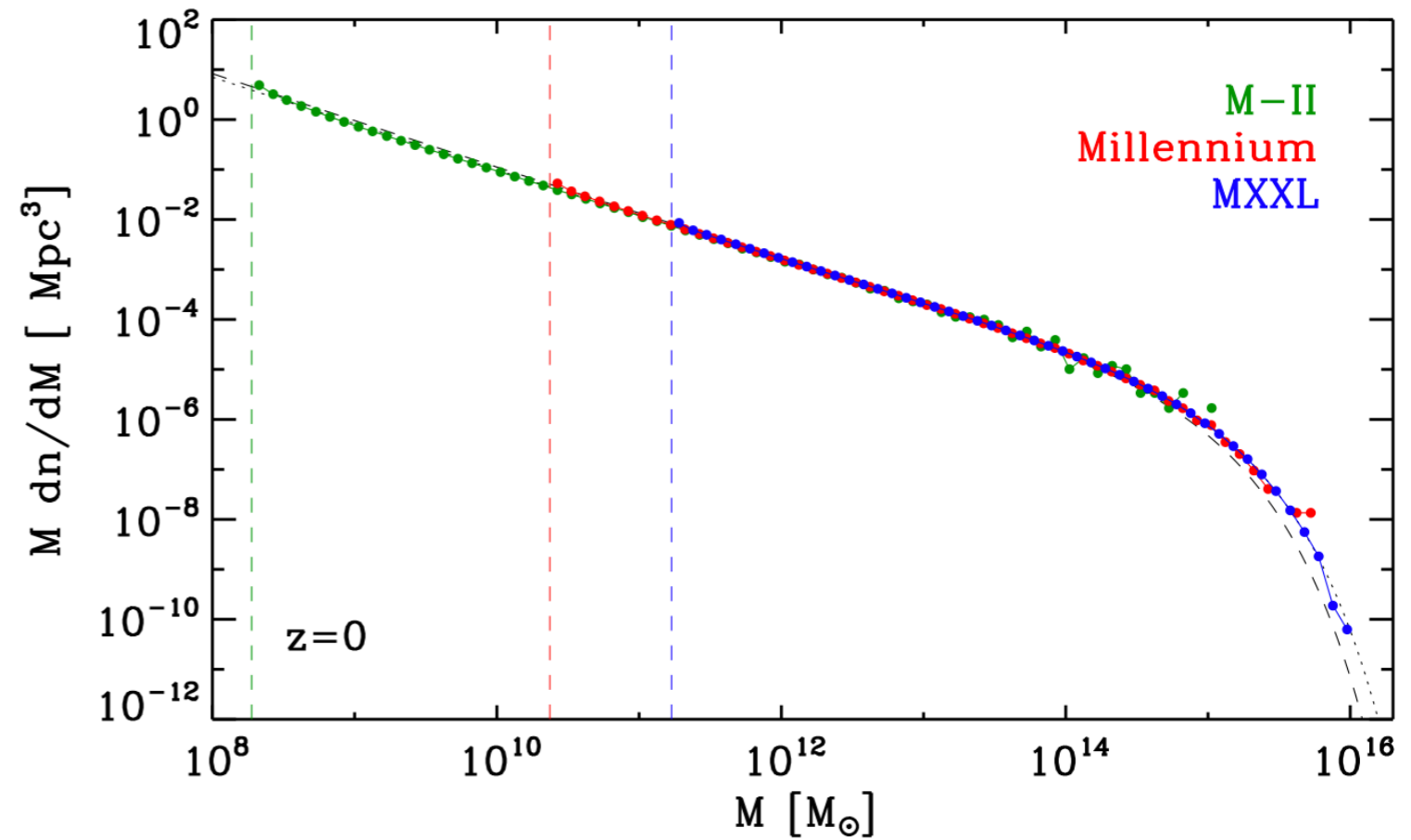


good cold **DM candidate**

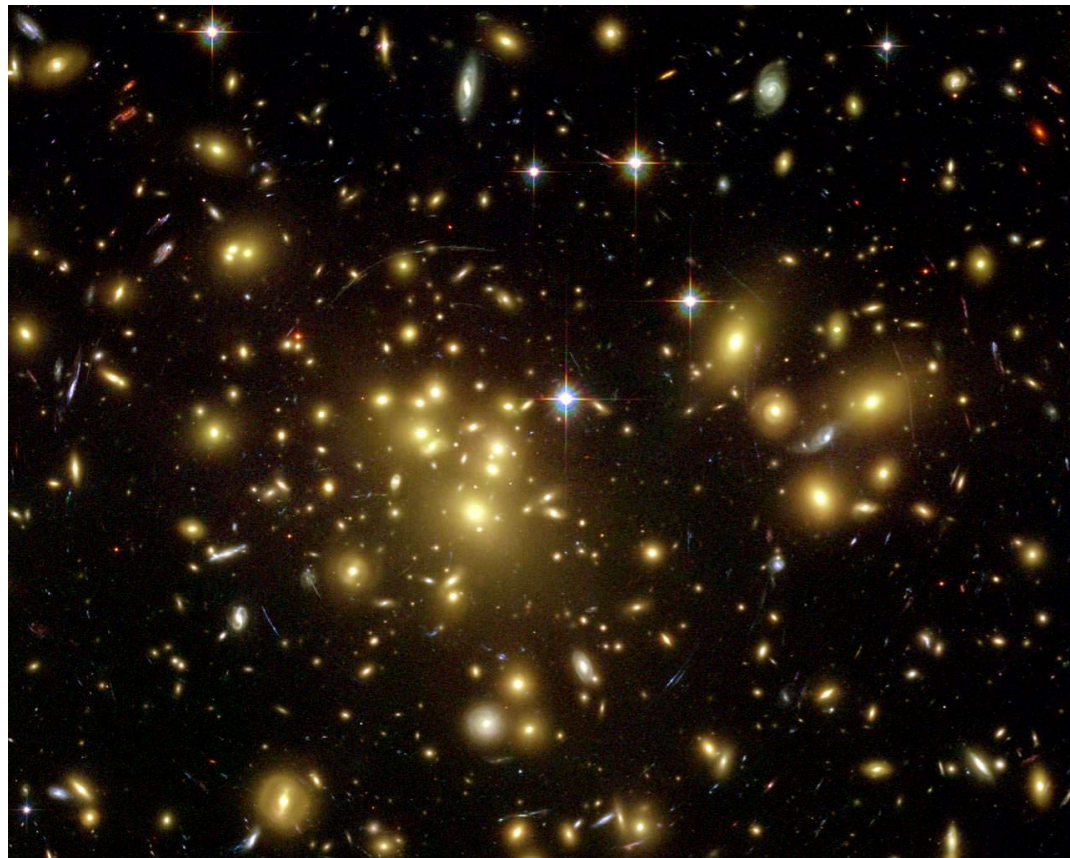


CAST Collaboration

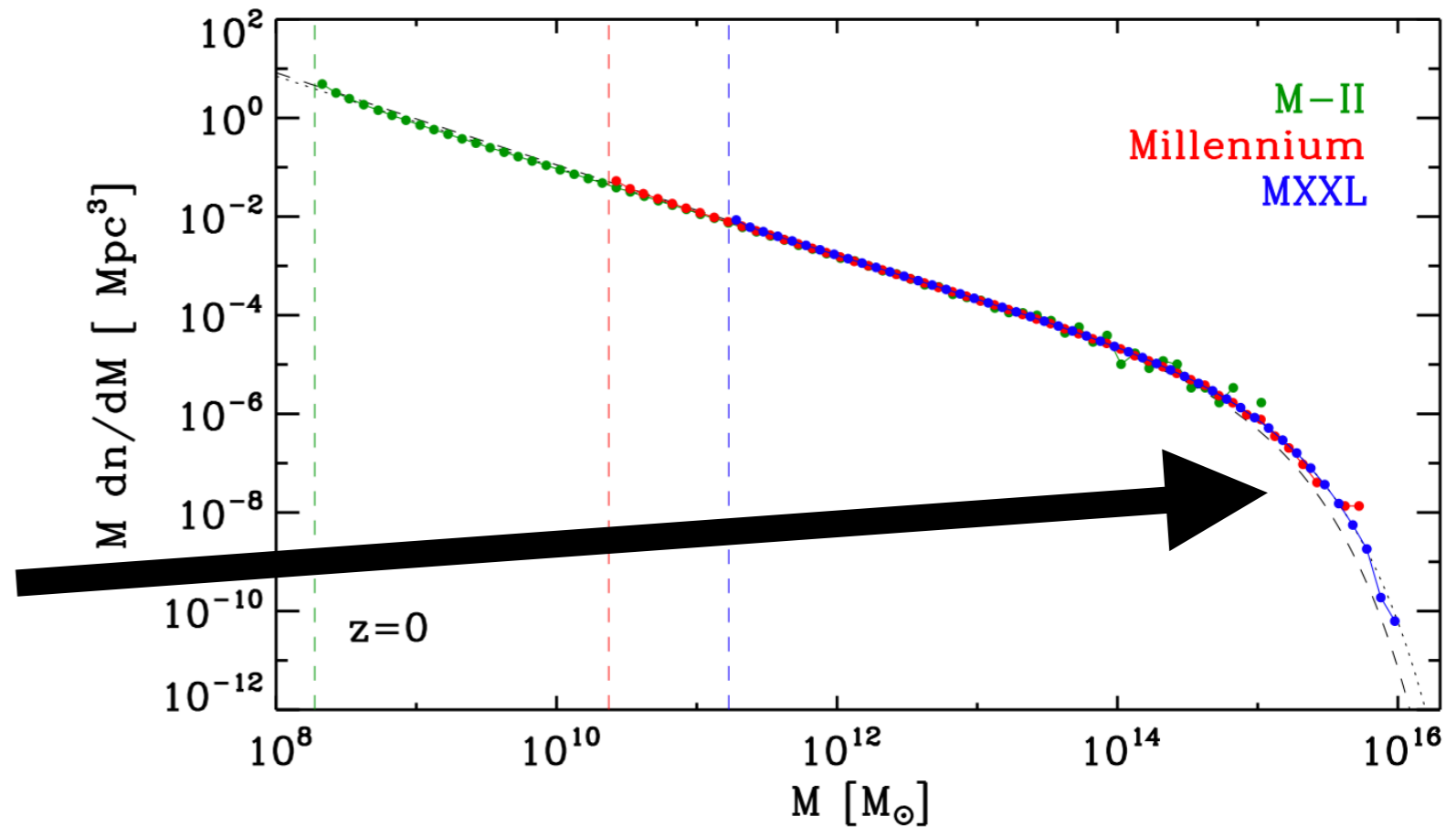
# What are axion minihalos?



# What are axion minihalos?



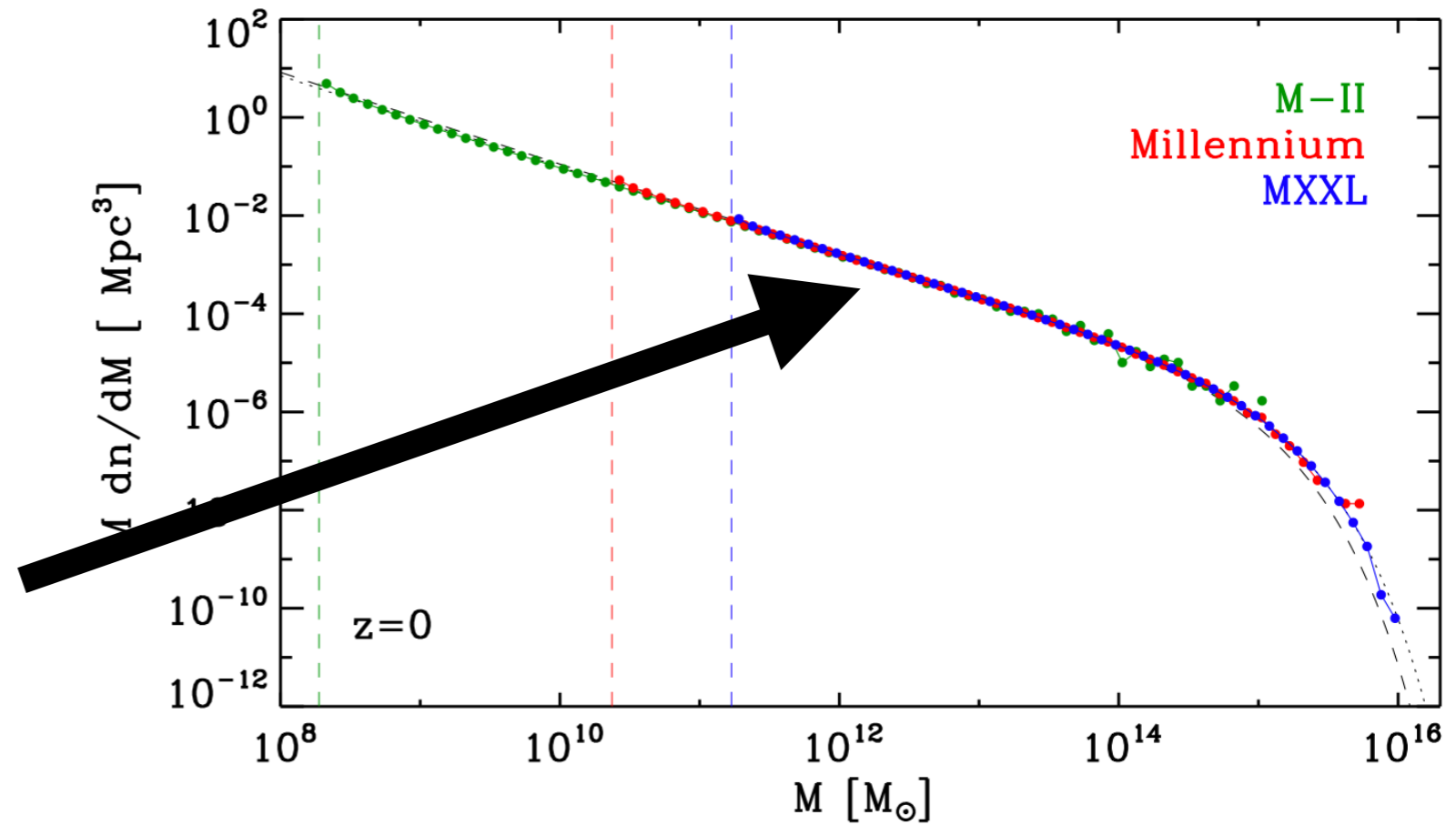
Galaxy Clusters



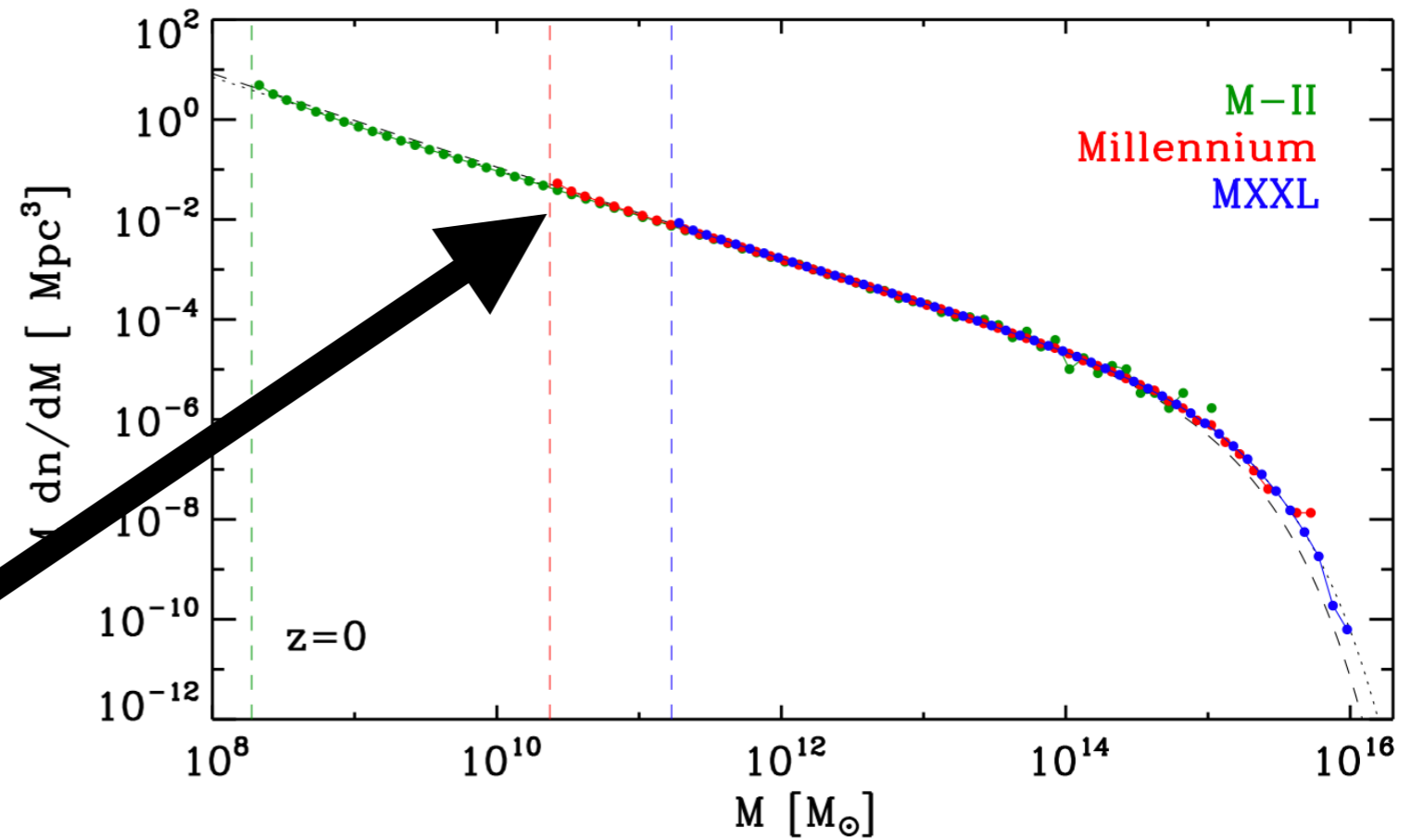
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Galaxies



# What are axion minihalos?

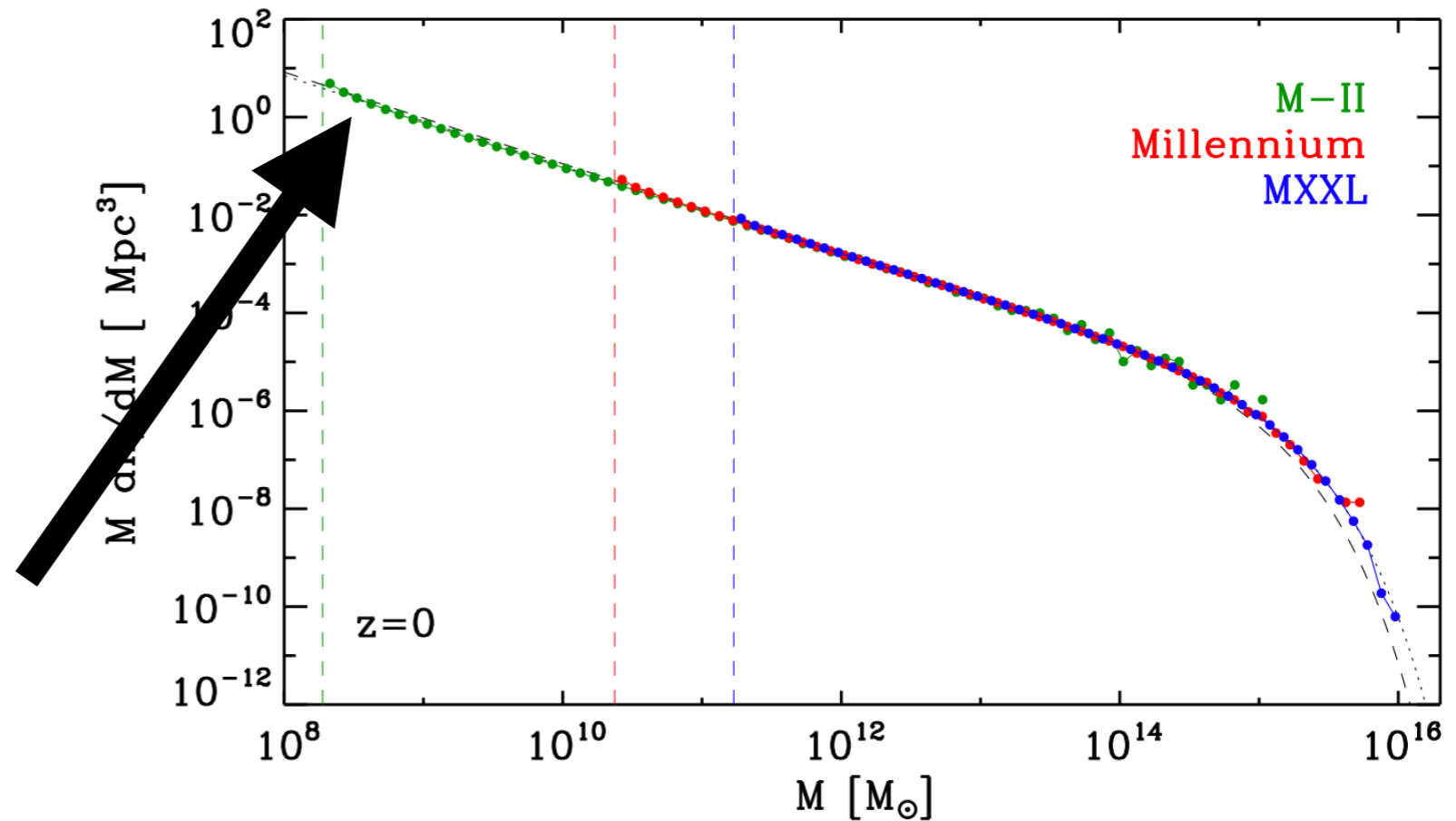


Dwarf Galaxies

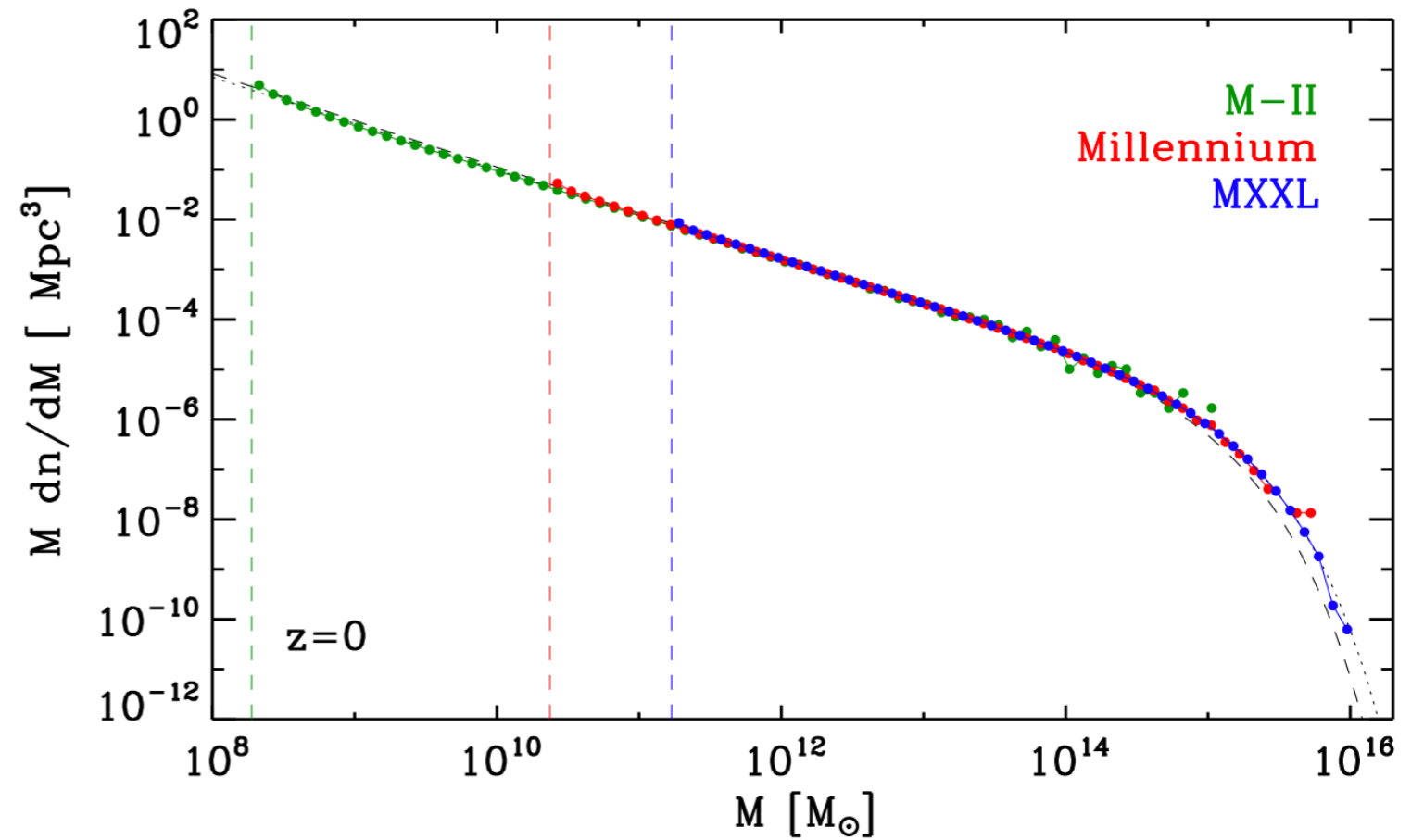
# What are axion minihalos?



DM subhalos  
(ultra-faint)

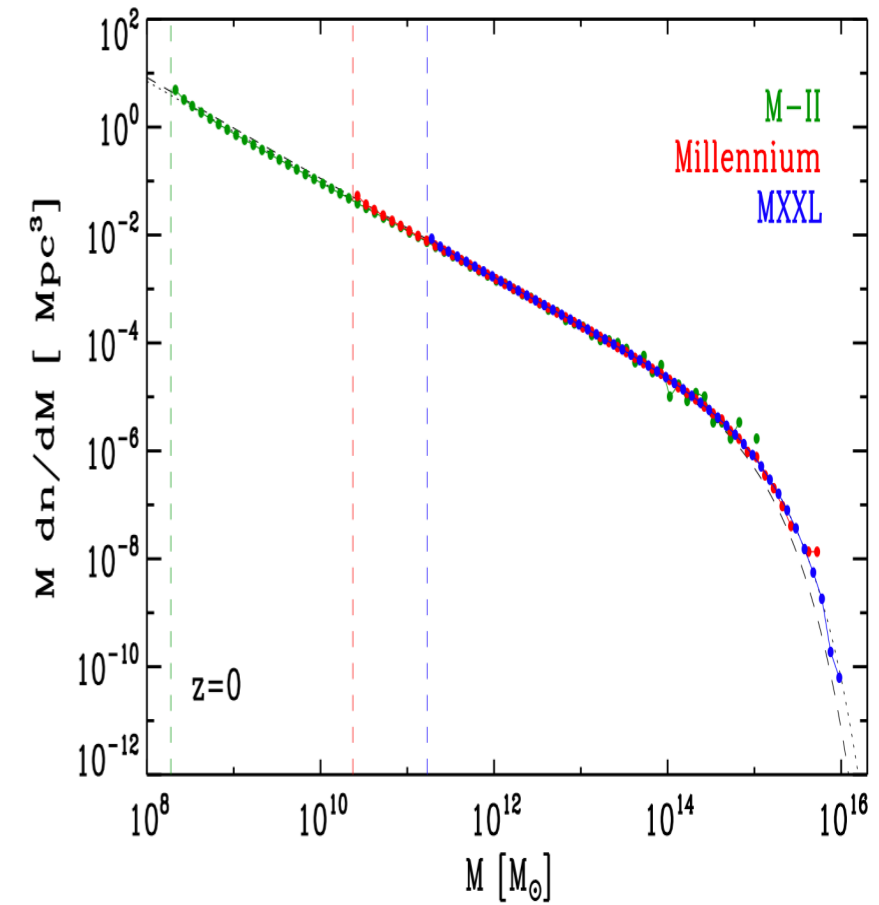


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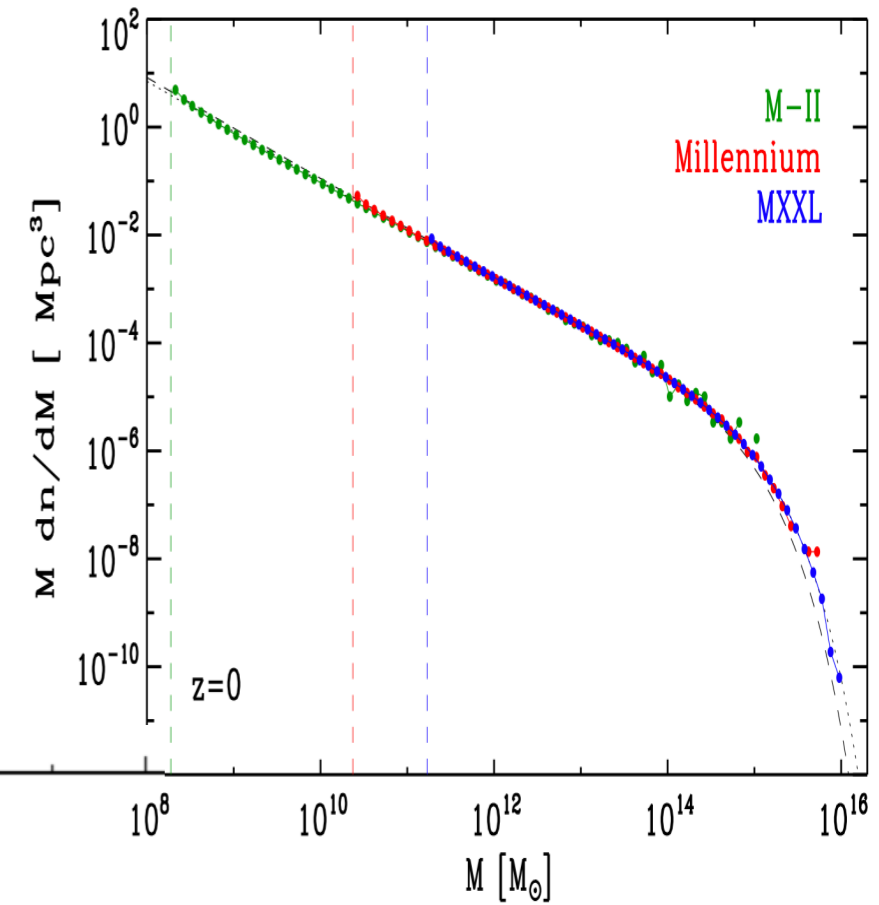




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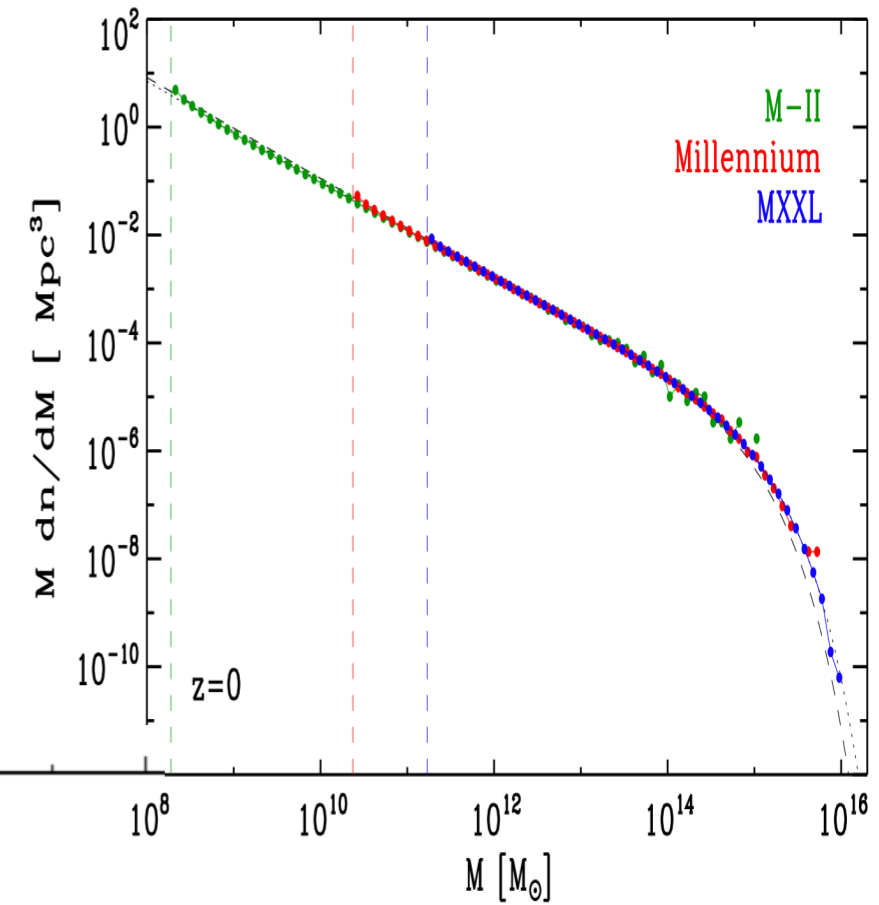


# What are axion minihalos?

Axion minihalos



$10^{-12}$   $10^{-10}$   $10^{-8}$



# What are axion minihalos?

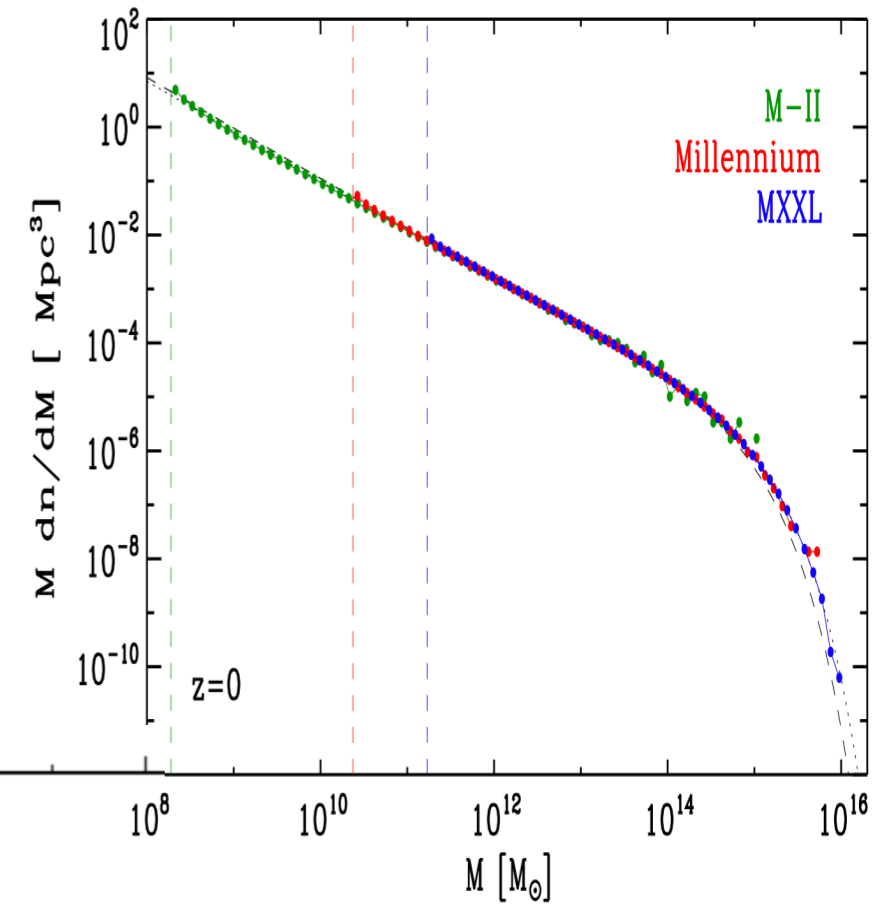
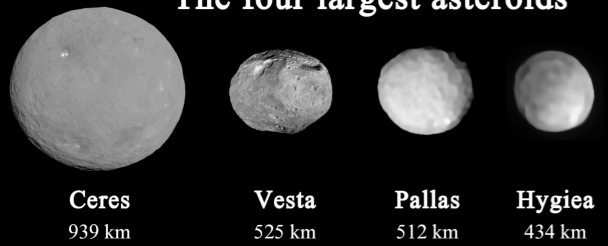
Axion minihalos



$10^{-12}$   $10^{-10}$   $10^{-8}$



The four largest asteroids



# What are axion minihalos?

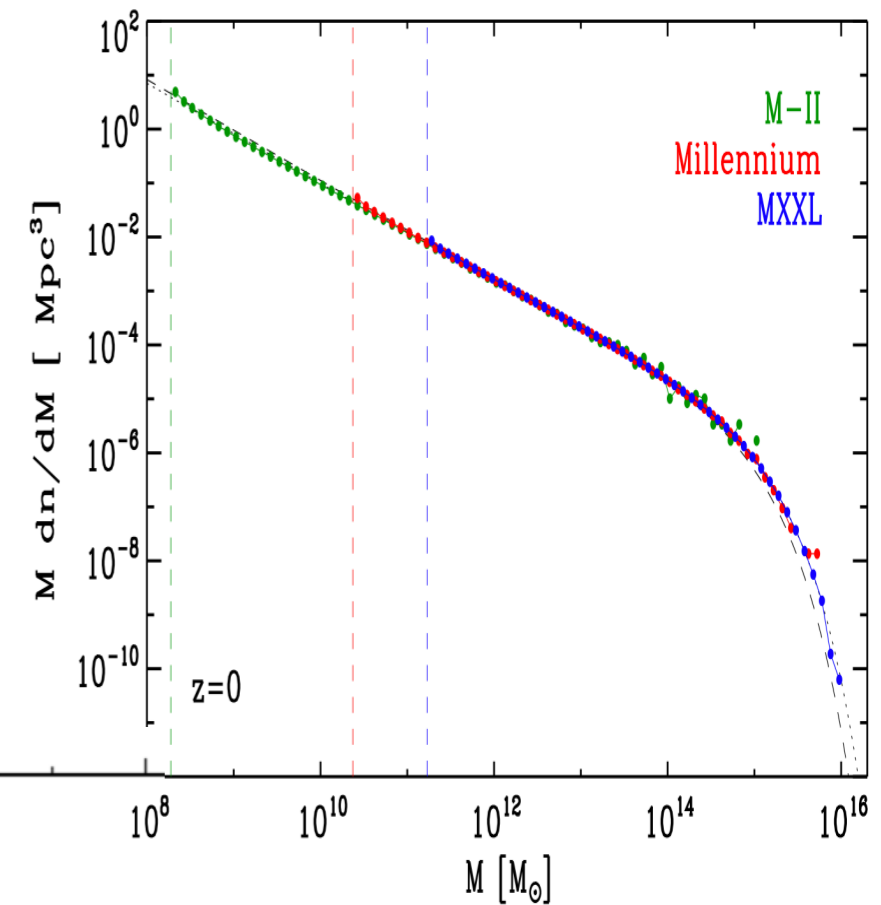
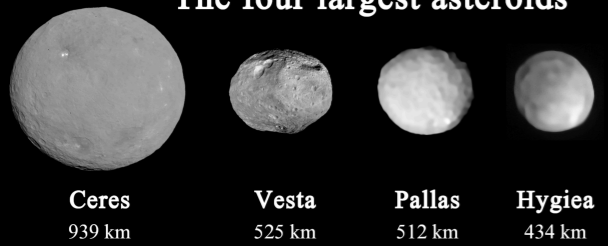
Axion minihalos



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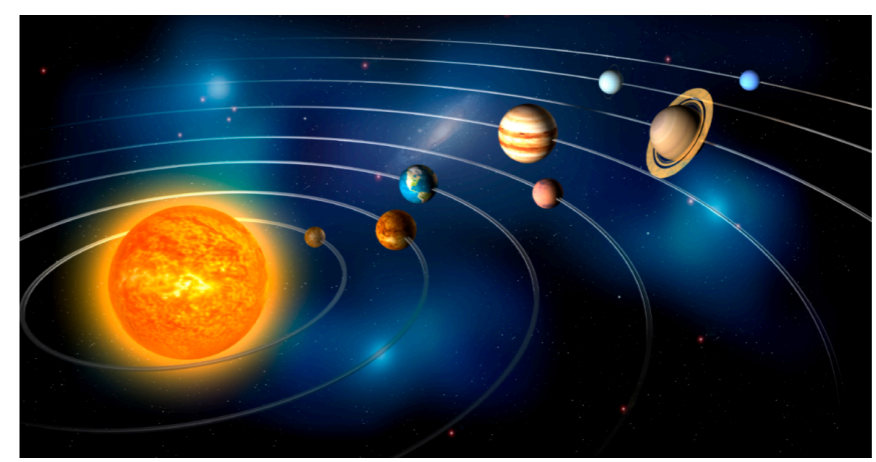
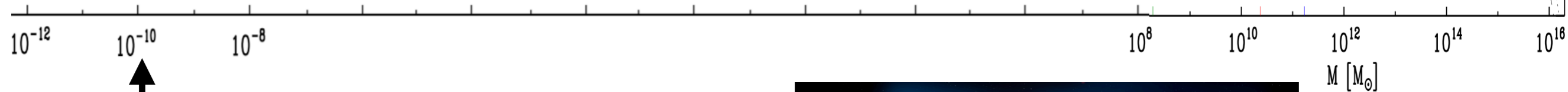


The four largest asteroids



# What are axion minihalos?

Axion minihalos



Pallas spread out over our solar system (roughly)

# What are axion minihalos?

## Facts:

- $10^{-10}$  solar masses heavy
  - solar system sized
- } True within a few orders of magnitude

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They are formed through axion self-interactions



# What are axion minihalos?

## Facts:

- $10^{-10}$  solar masses heavy
  - solar system sized
- } True within a few orders of magnitude
- Requirement: PQ symmetry is broken after inflation!  
They are formed through axion self-interactions
  - Why should we care about them?
    - Direct detection (are we sitting in a local void?)
    - We can search for them (e.g. through neutron stars)
    - Scenario provides prediction for axion mass
    - Can they host axion stars?

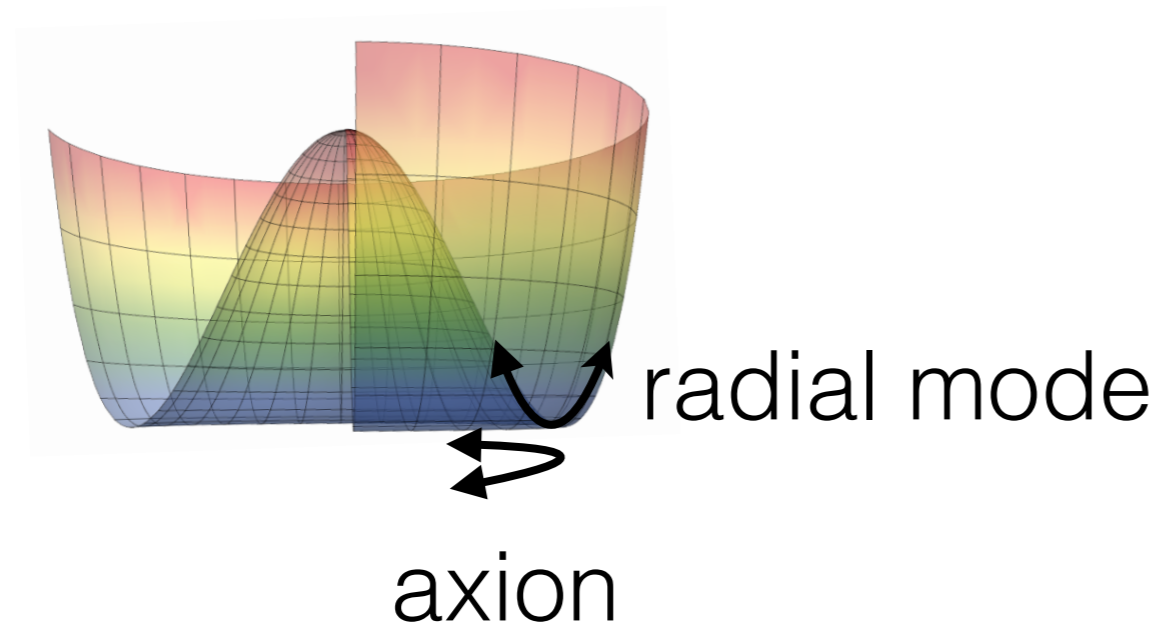
# Post- vs Pre-inflationary scenario

Two different scenarios can be considered:  
Breaking the PQ symmetry **before** or **after** inflation

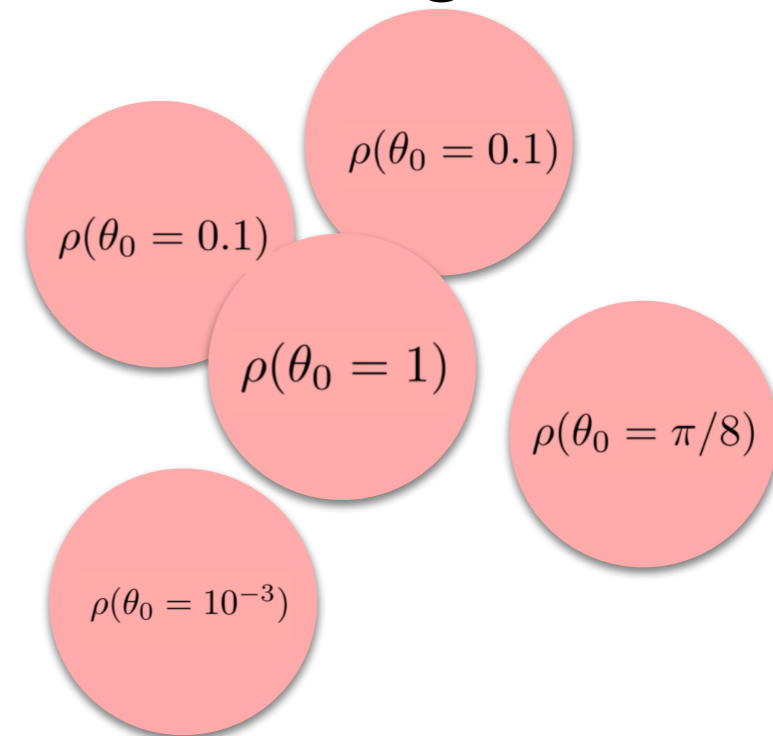
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$$V(\Phi, T) = \frac{\lambda}{4} (|\Phi|^2 - f_a^2)^2$$



Breaking PQ:

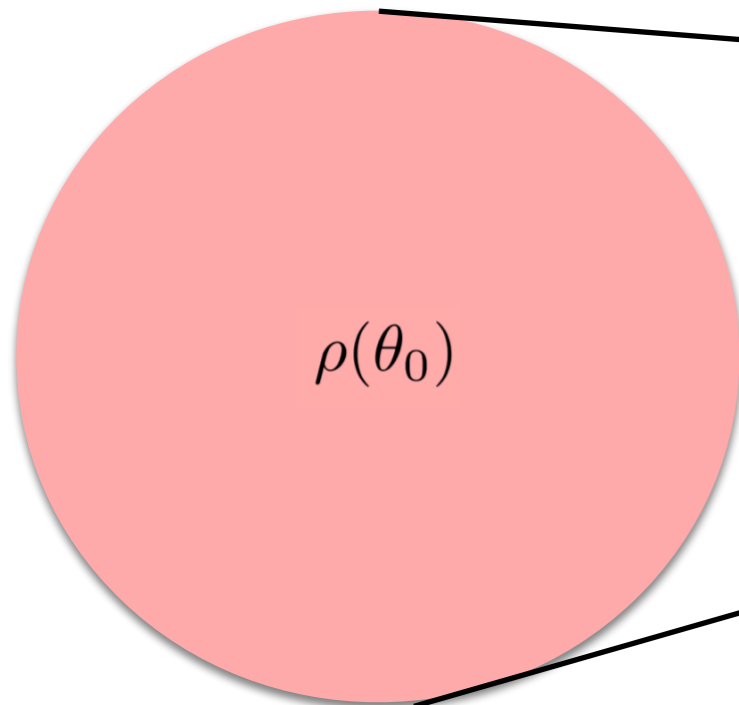


Hubble-sized patches

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**before inflation:**

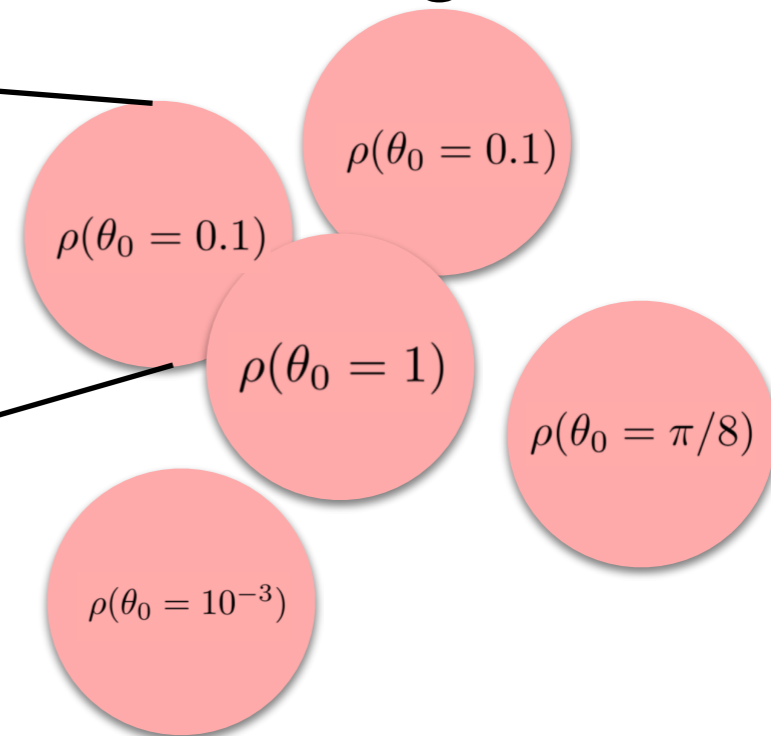


$$\Omega_{a,0} \sim \theta_0^2$$

two free parameters:

$$\theta_0, f_a$$

Breaking PQ:

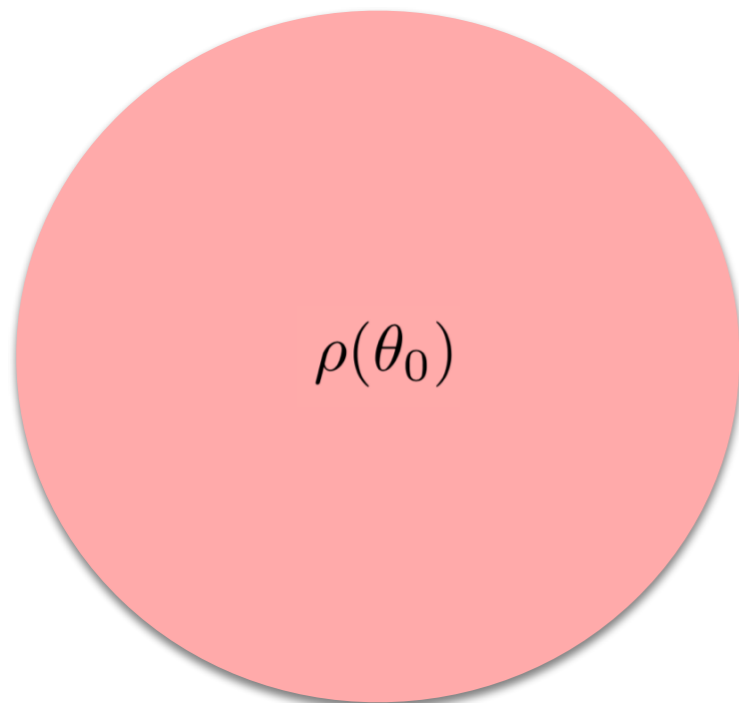


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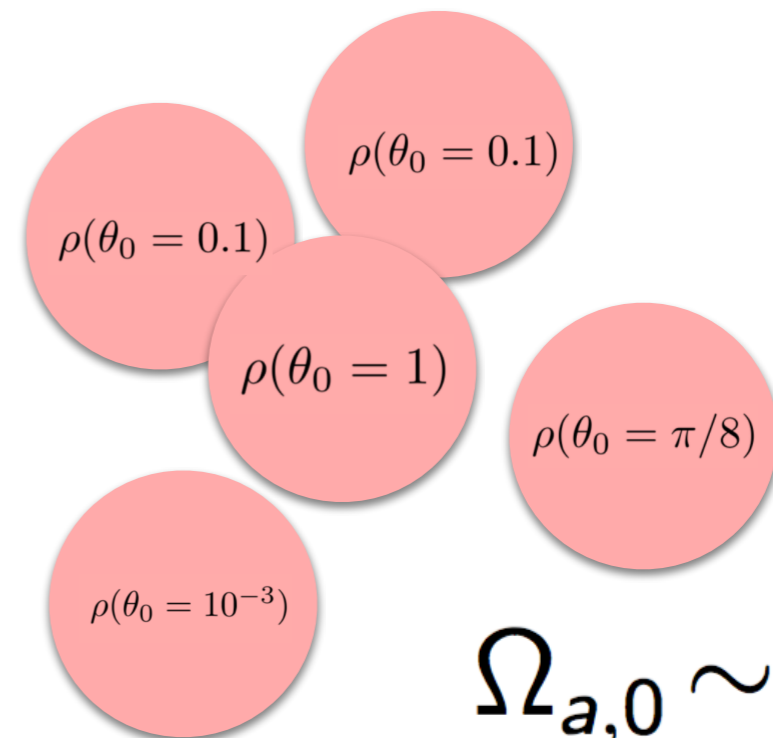
**before inflation:**



$$\Omega_{a,0} \sim \theta_0^2$$

two free parameters:  
 $\theta_0, f_a$

**after inflation:**



$$\Omega_{a,0} \sim \langle \theta_0^2 \rangle$$

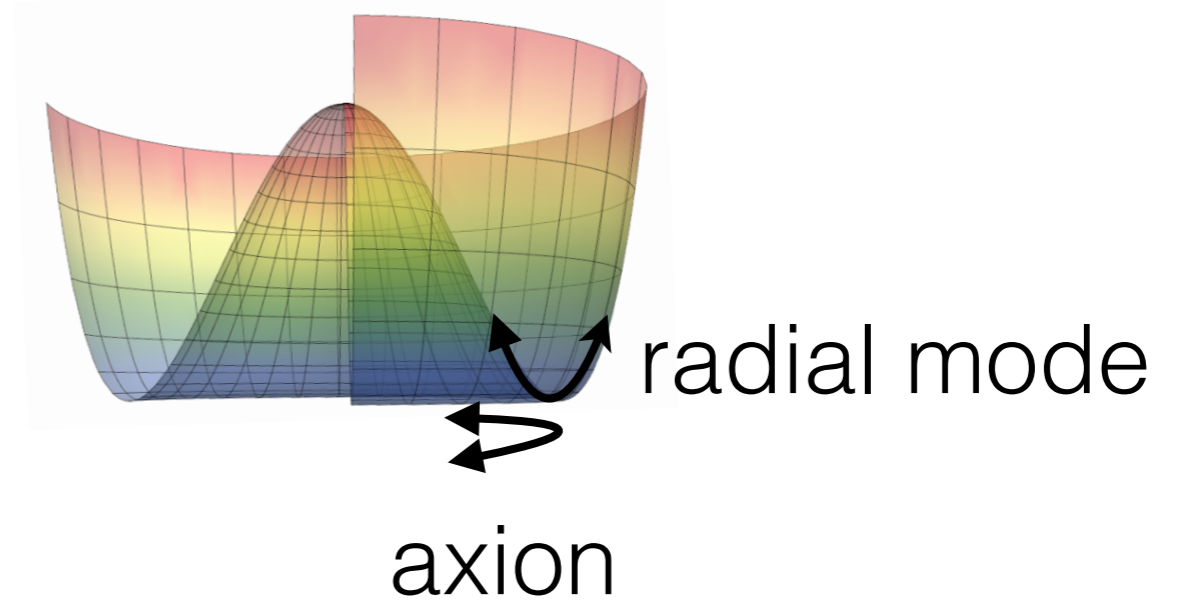
one free parameter:  $f_a$

Inflation

simulation

PQ transition @  $T \approx f_a$

$$V(\Phi, T) = \frac{\lambda}{4} (|\Phi|^2 - f_a^2)^2$$



time (not to scale)

time (not to scale)

simulation

Inflation

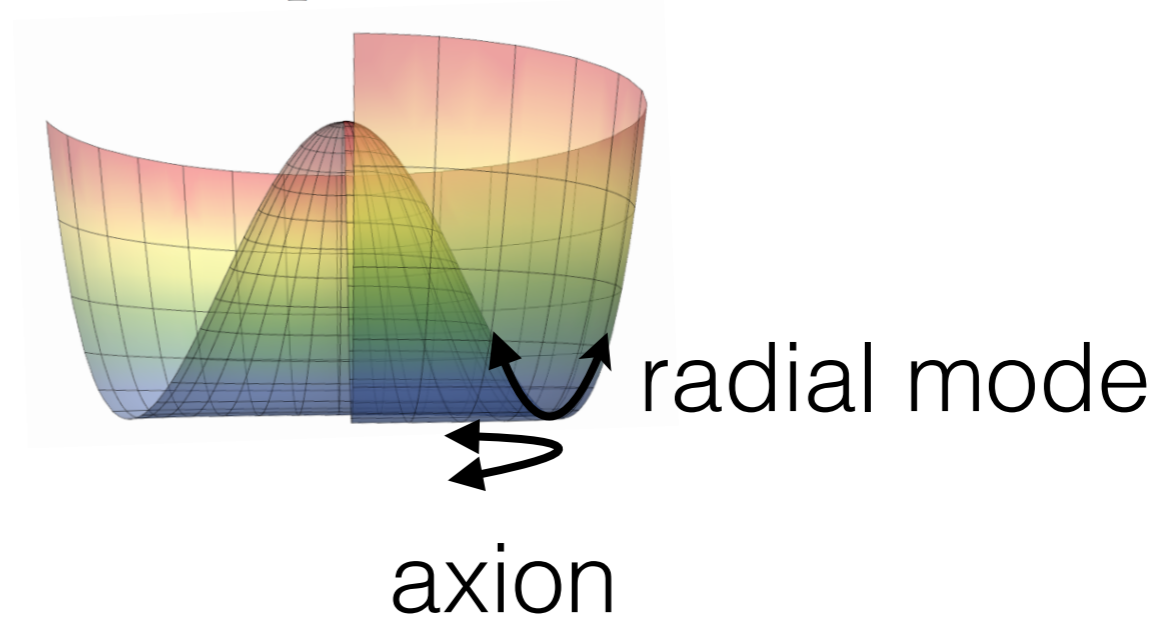
thermal spec.

PQ transition

@  $T \approx f_a$

radial @ vev

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time (not to scale)

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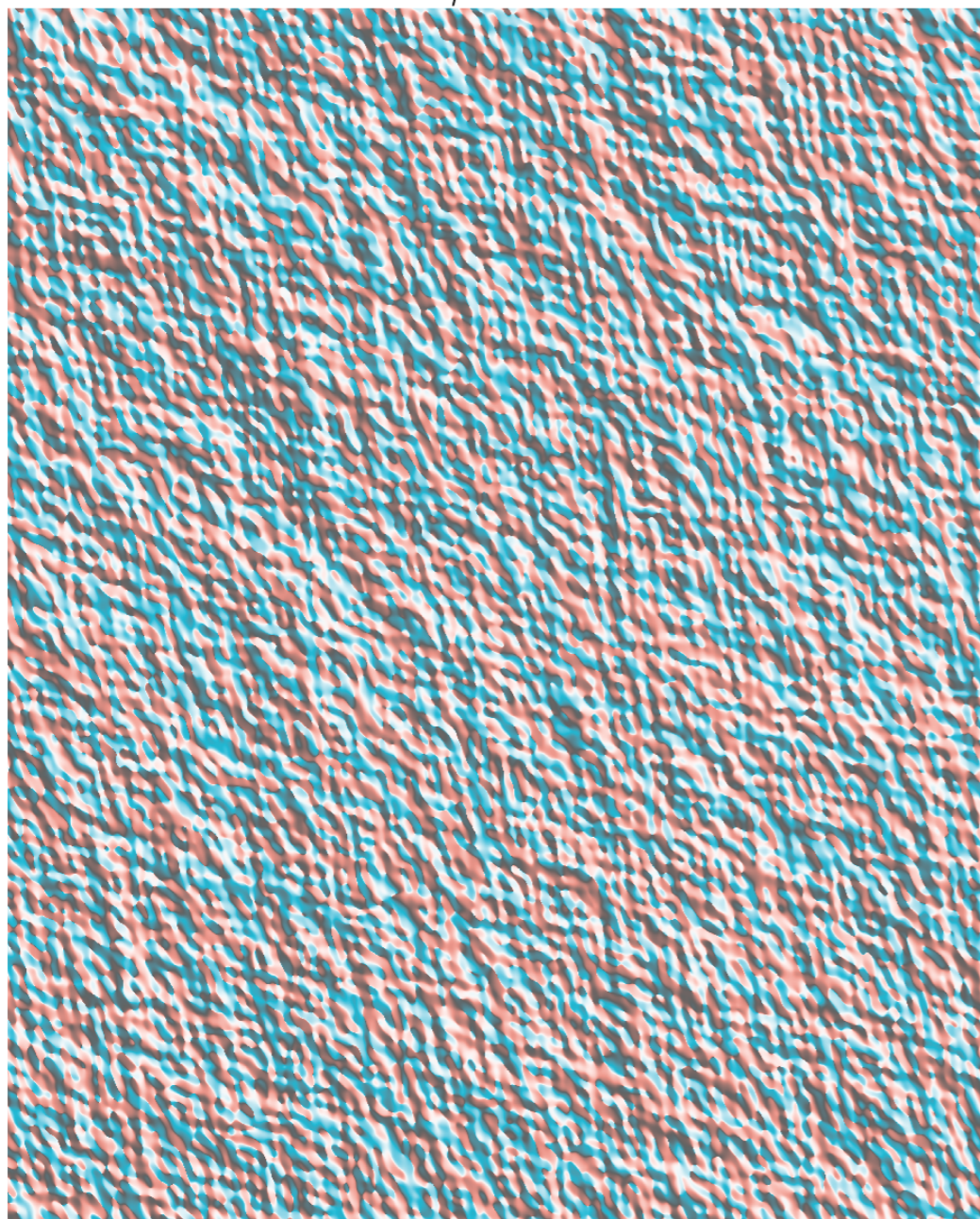
Inflation

thermal spec.

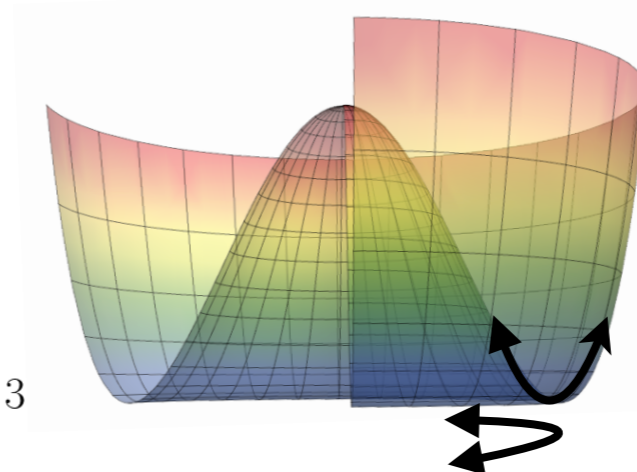
PQ transition @  $T \approx f_a$

radial @ vev

$\eta = 0.12$



$$V(\Phi, T) = \frac{\lambda}{4} (|\Phi|^2 - f_a^2)^2$$



radial mode

axion

Solve Equations of Motion  
on a large 3D grid  
(about  $10^{11}$  grid sites)



time (not to scale)

simulation

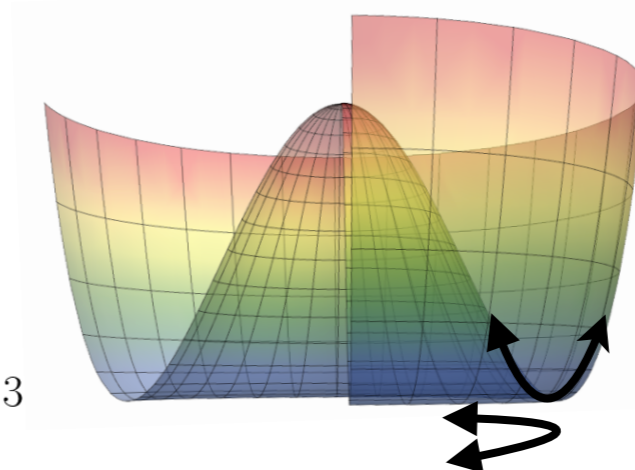
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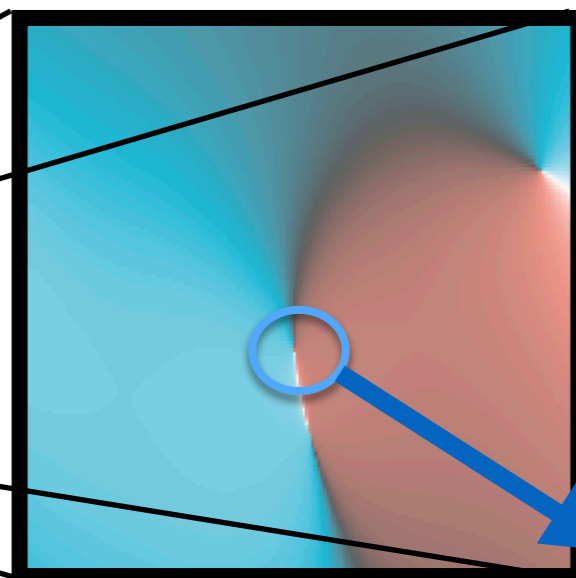
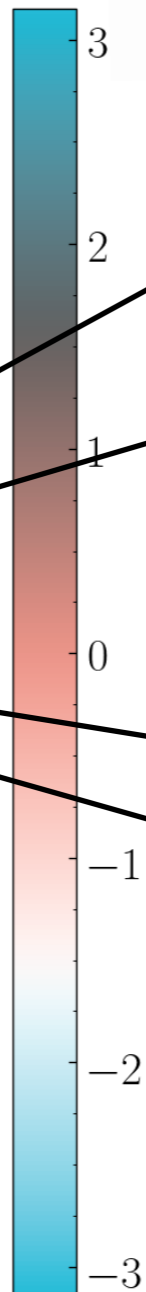
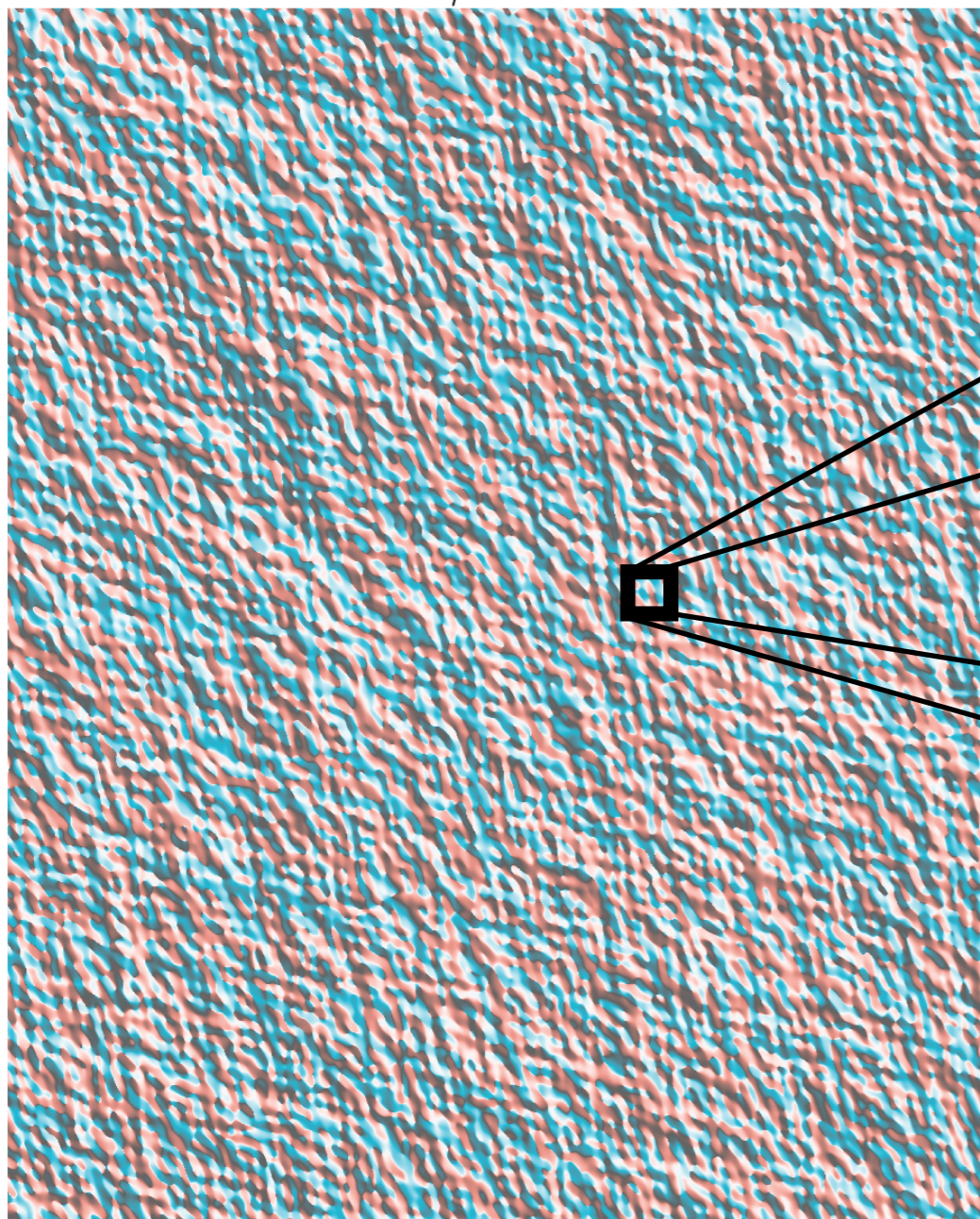
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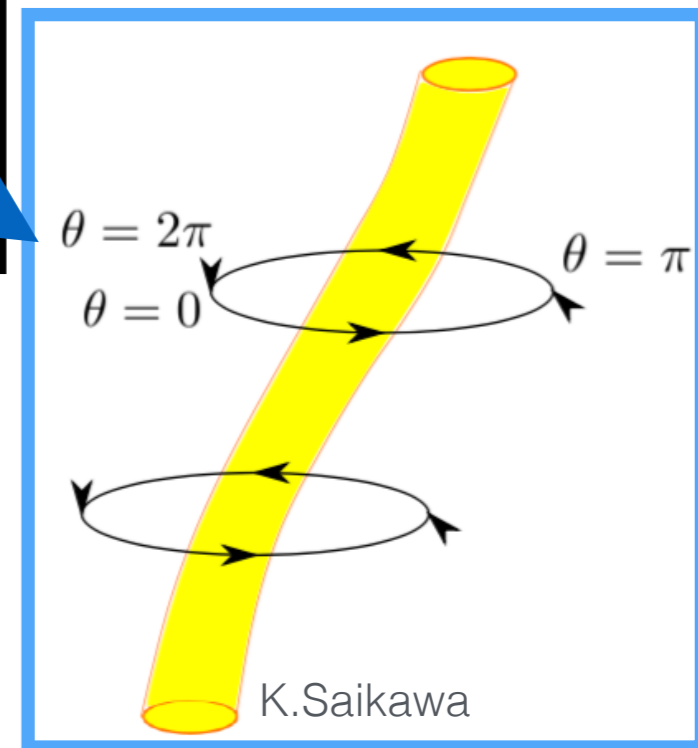
radial mode

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**network of cosmic strings**



K.Saikawa

time (not to scale)

simulation

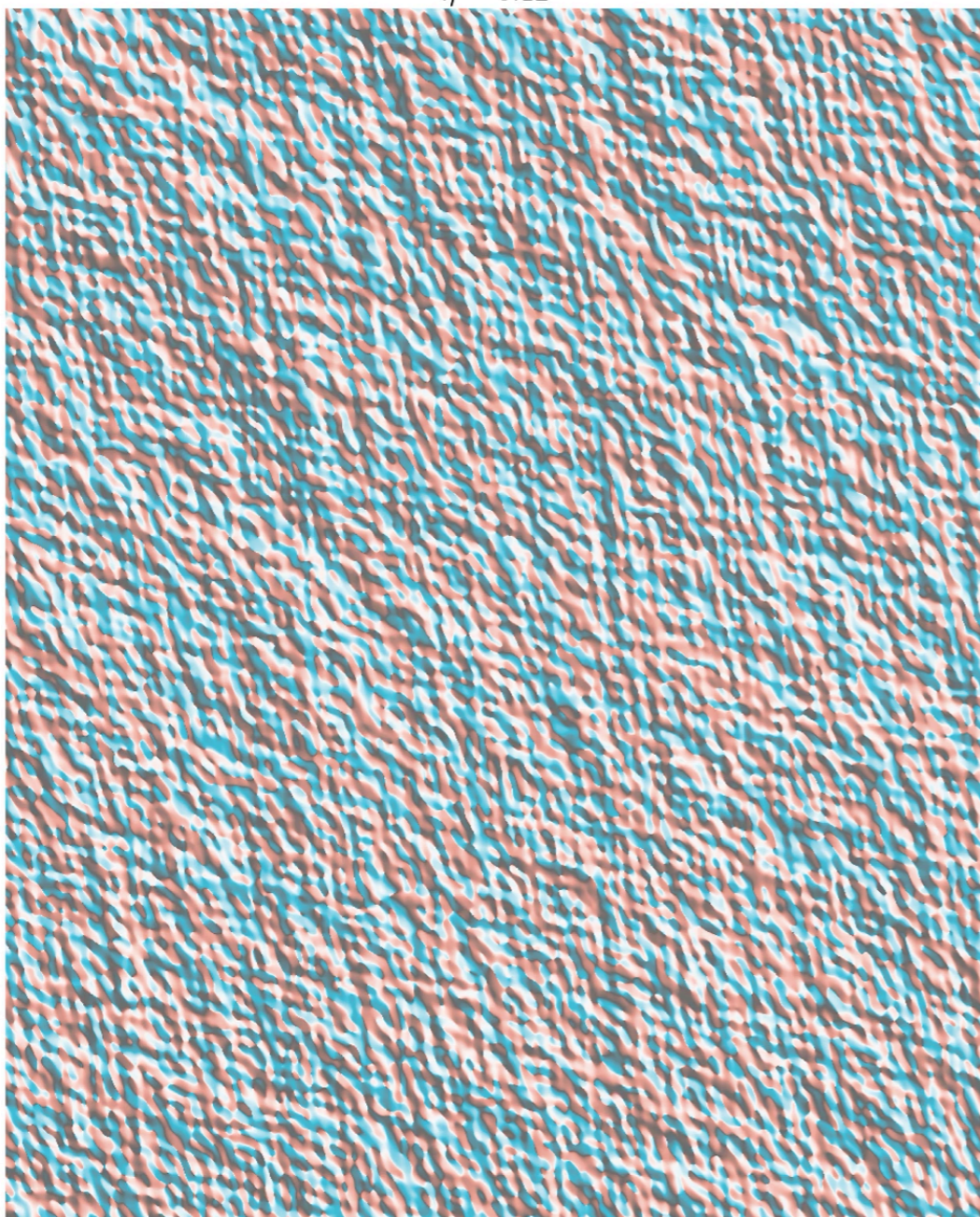
Inflation

thermal spec.

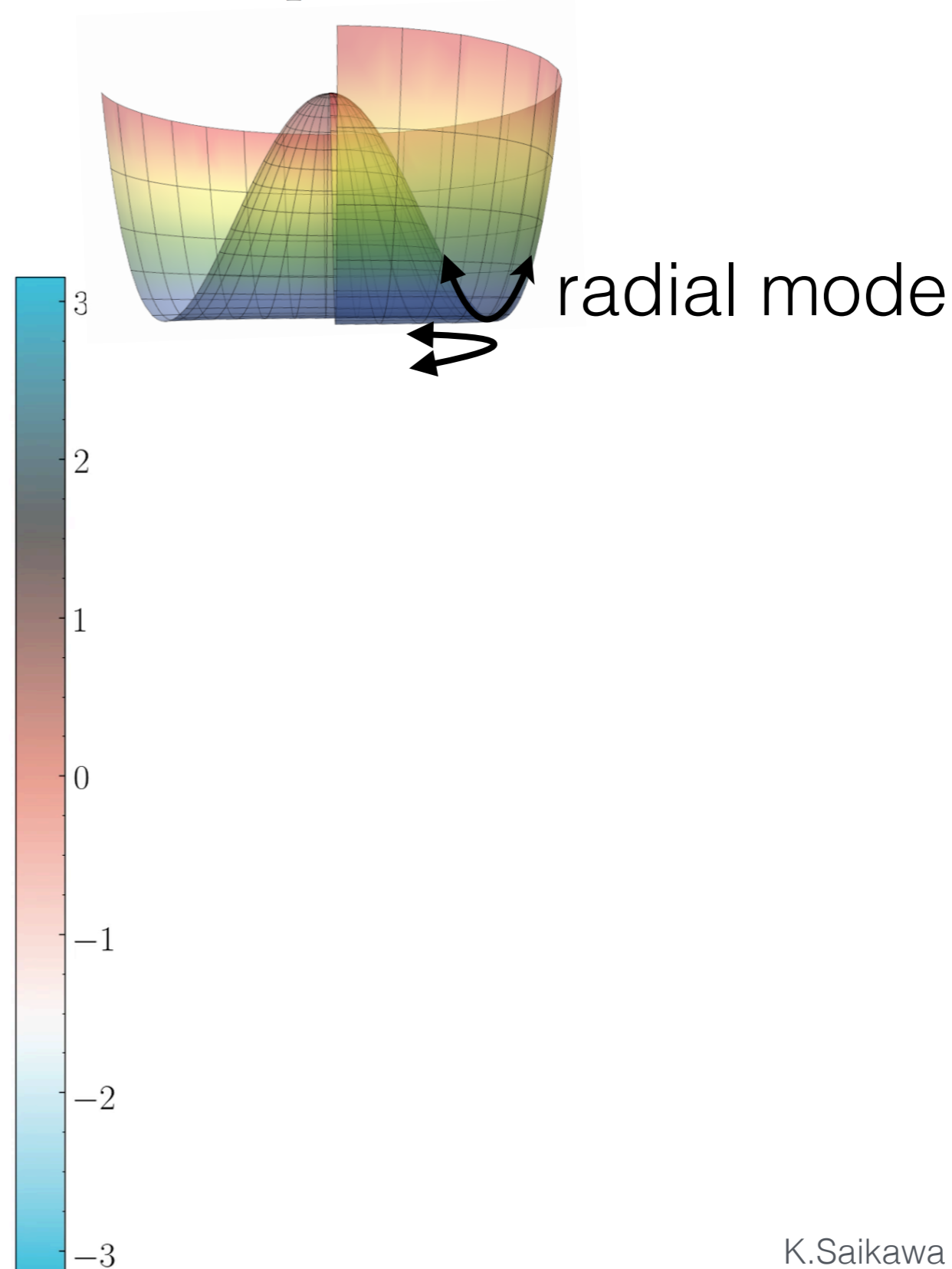
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K.Saikawa

time (not to scale)

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PQ transition

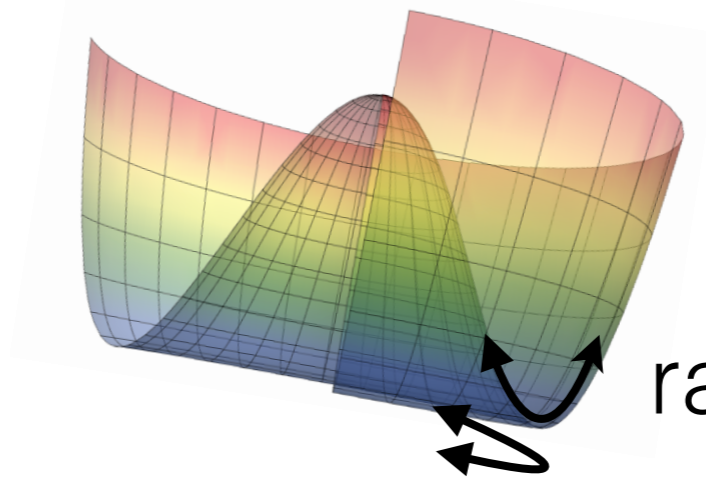
radial @ vev

QCD transition

@  $T \approx 1$  GeV

simulation

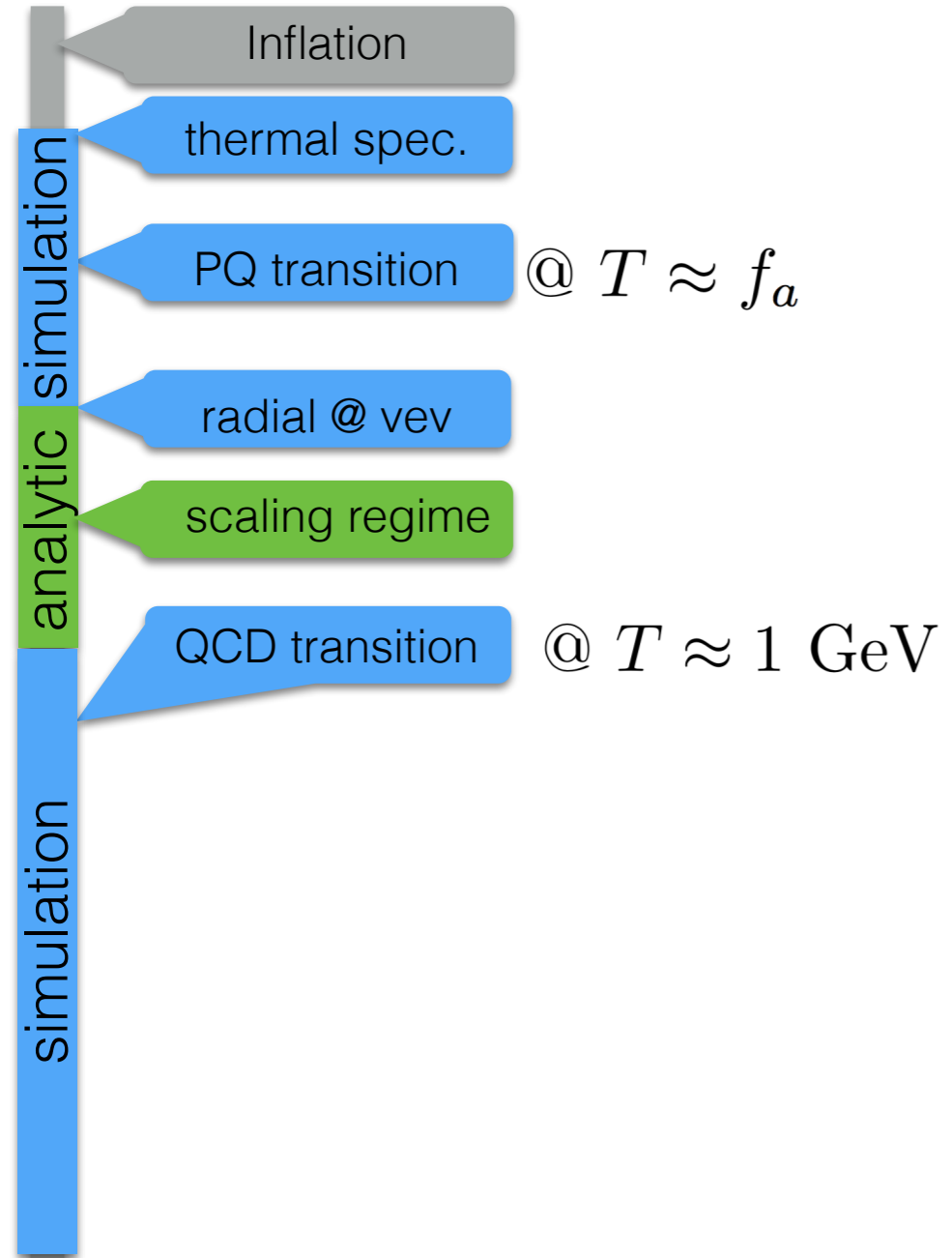
$$V(\Phi, T) = \frac{\lambda}{4} (|\Phi|^2 - f_a^2)^2 + m_a(T)^2 f_a^2 [1 - \cos \text{Arg}(\Phi)]$$



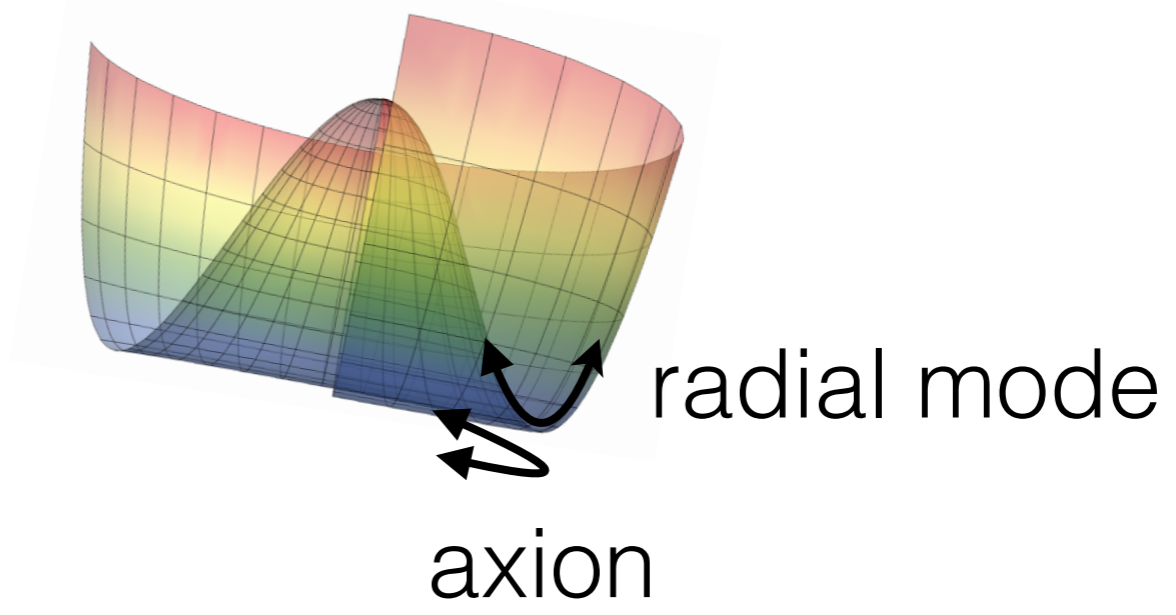
radial mode

axion

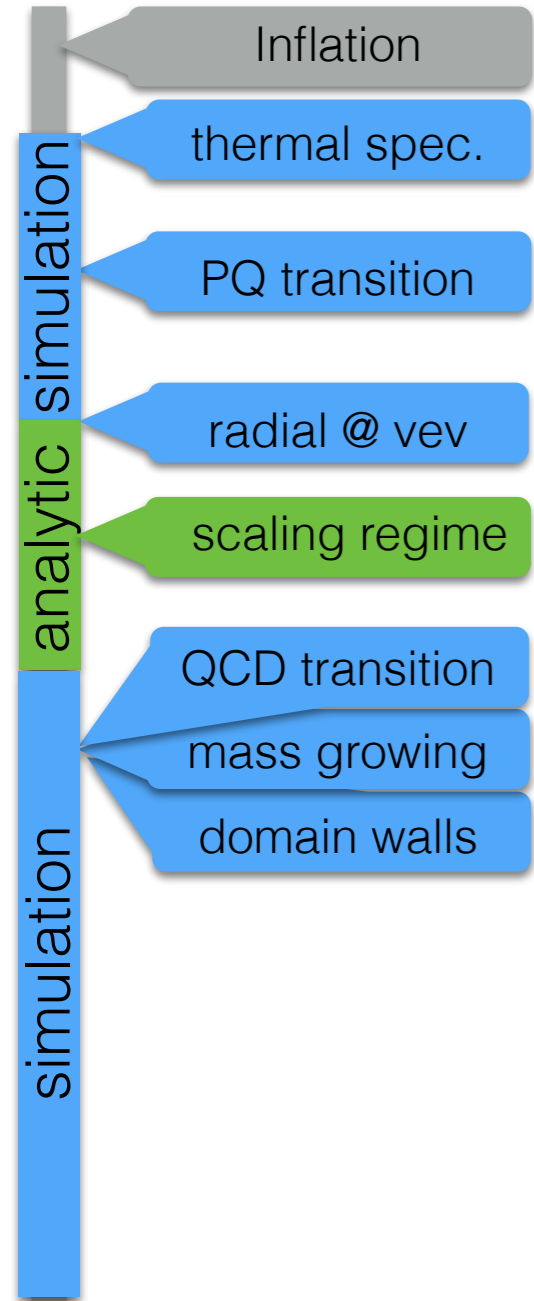
time (not to scale)



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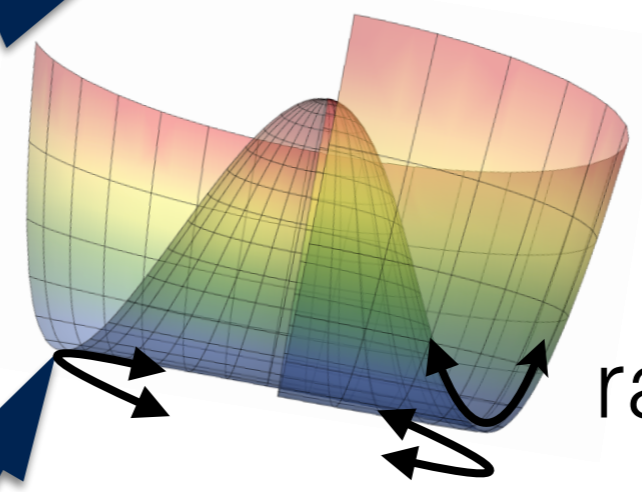
time (not to scale)



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growing axion mass  
@  $T \approx 1 \text{ GeV}$

domain walls form



radial mode

axion

time (not to scale)

simulation

Inflation

thermal spec.

PQ transition

radial @ vev

scaling regime

QCD transition

mass growing

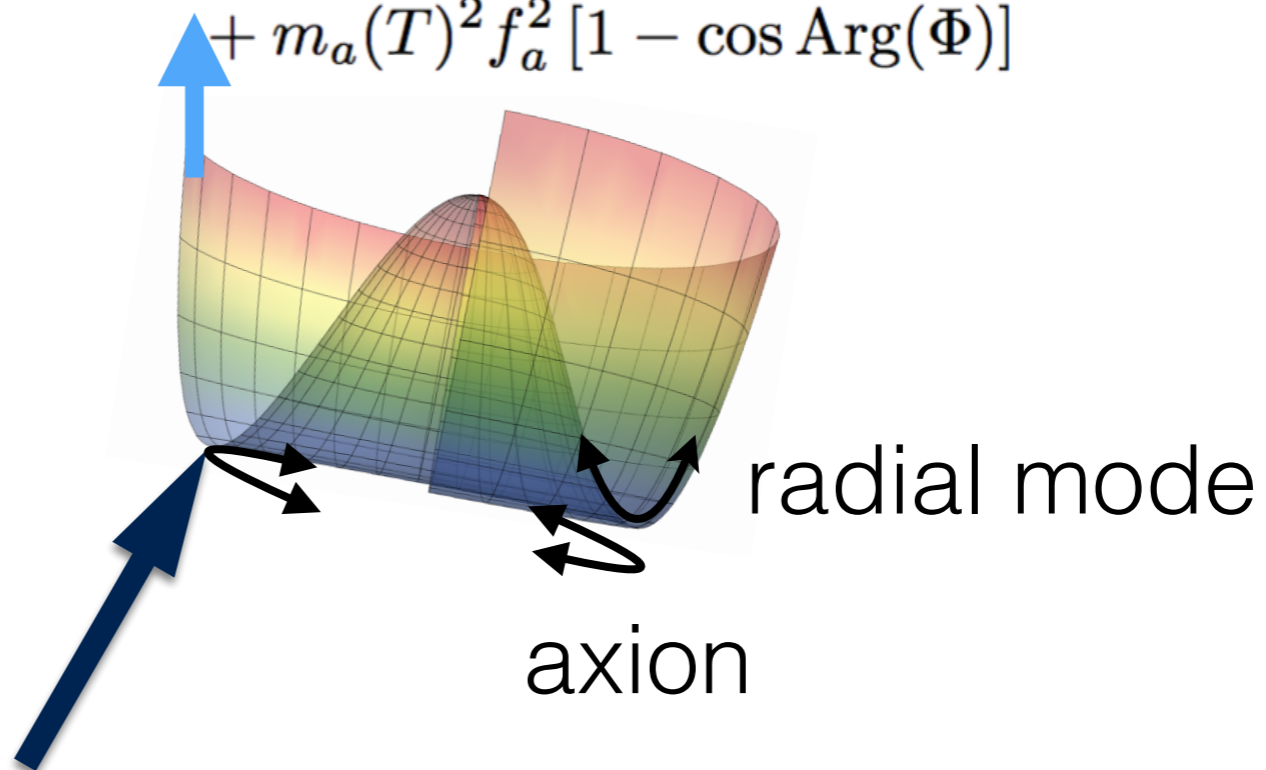
domain walls

network collapse

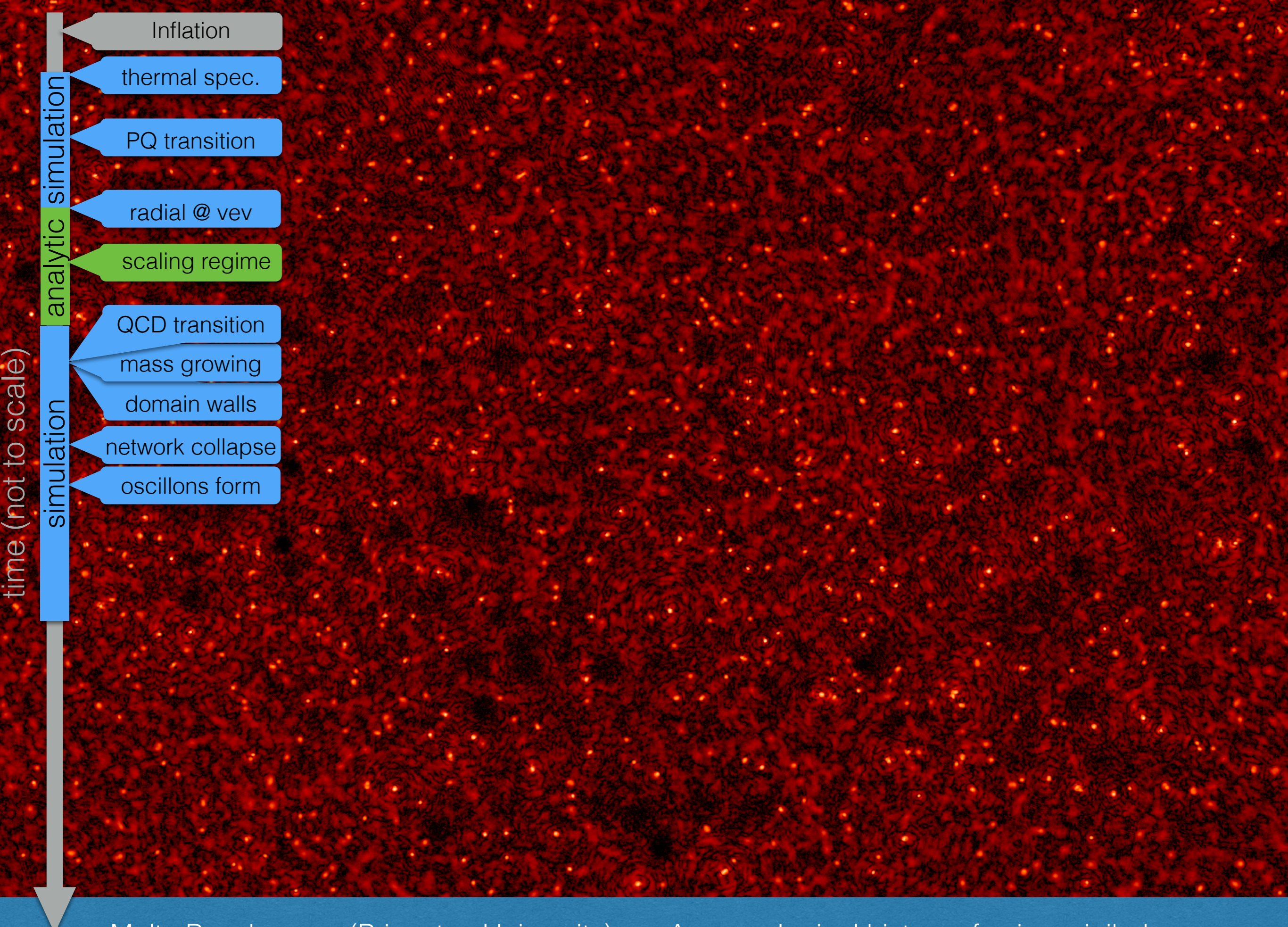
@  $T \approx 1 \text{ GeV}$

$$V(\Phi, T) = \frac{\lambda}{4} (|\Phi|^2 - f_a^2)^2$$

$$+ m_a(T)^2 f_a^2 [1 - \cos \text{Arg}(\Phi)]$$



tension in domain walls  
causes string-domain wall network  
to collapse



Inflation

thermal spec.

PQ transition

radial @ vev

scaling regime

QCD transition

mass growing

domain walls

network collapse

oscillons form

time (not to scale)

analytic

simulation

# Evolution of Oscillons

time (not to scale)

simulation analytic simulation

Inflation

thermal spec.

PQ transition

radial @ vev

scaling regime

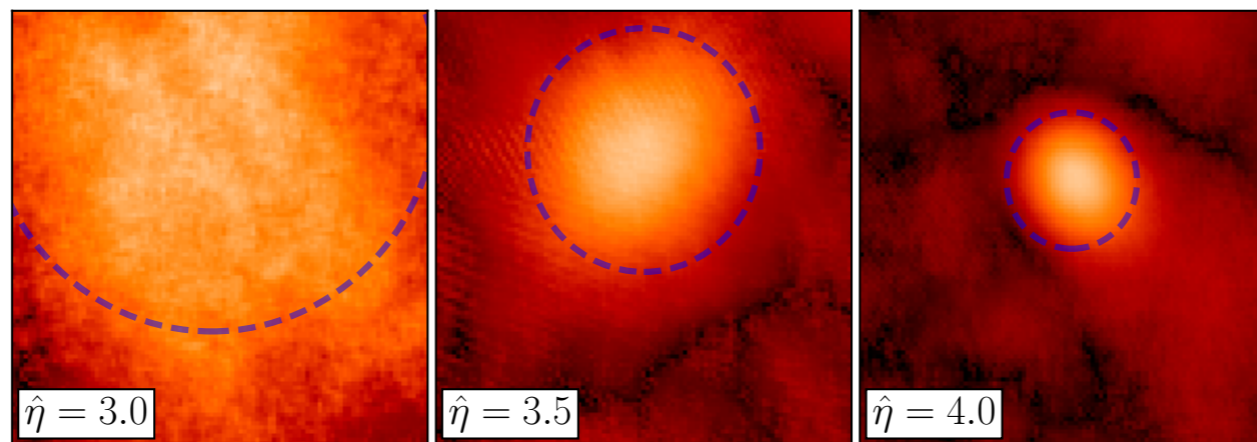
QCD transition

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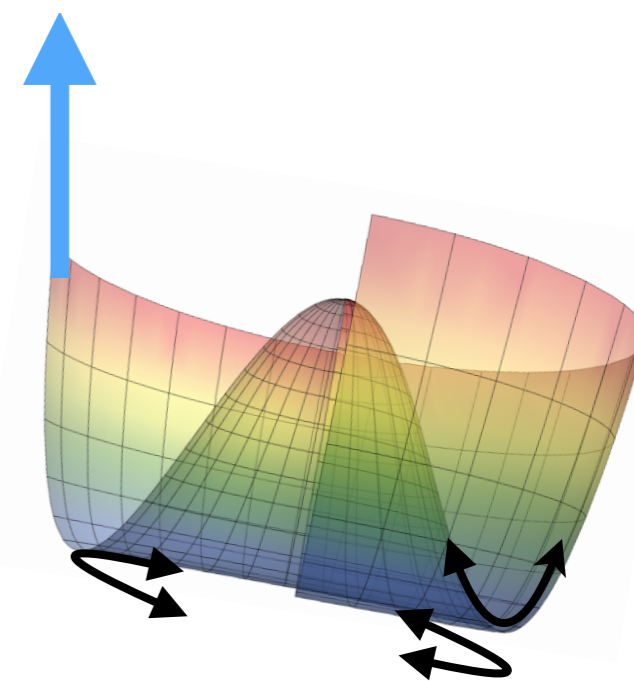
domain walls

network collapse

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$$m_a(T)^2 f_a^2 [1 - \cos \text{Arg}(\Phi)]$$

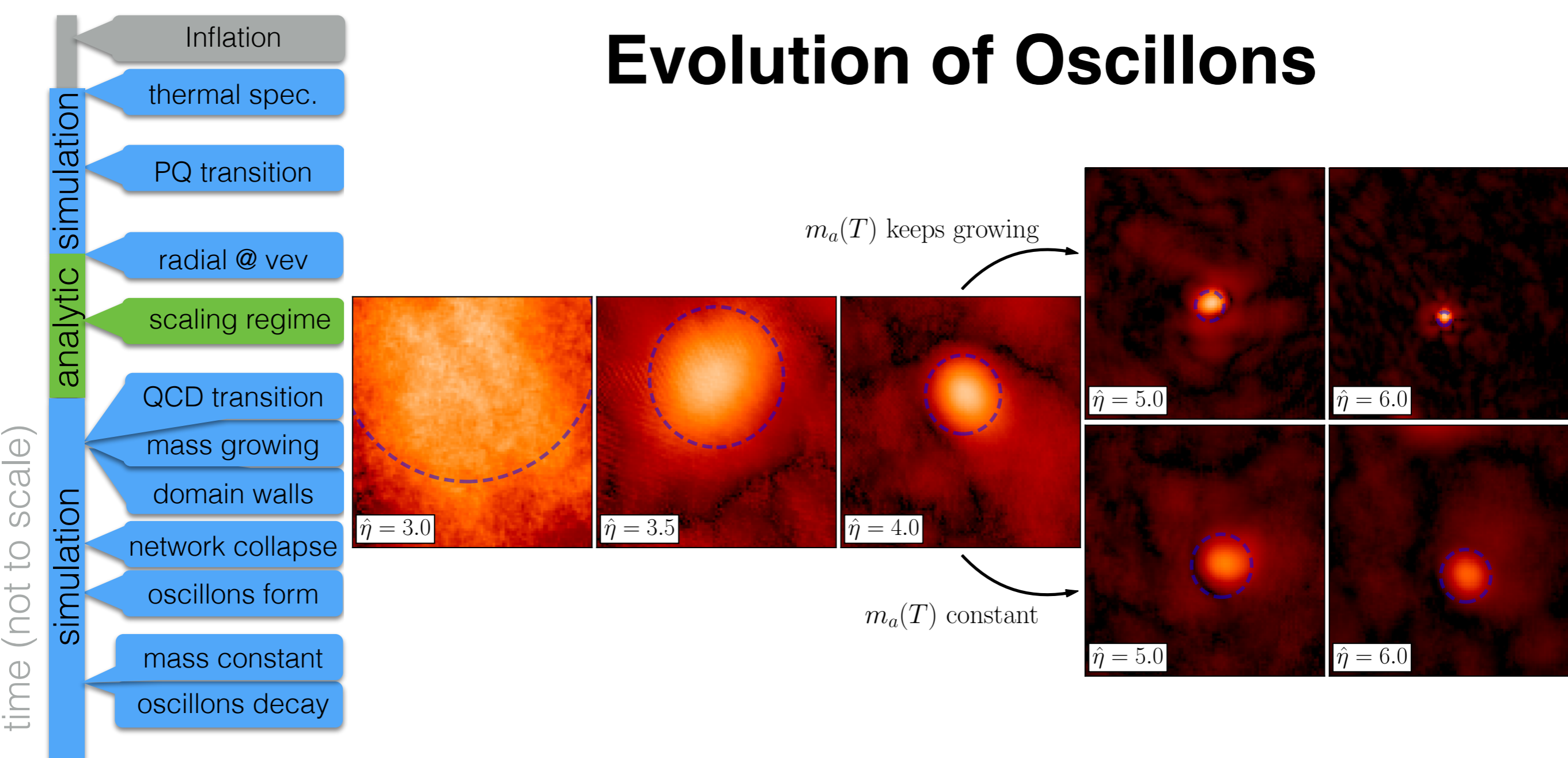


## Facts about Oscillons:

1. They are regions with large field values/large energy density
2. Their size is given by the axion wavelength  $\sim$  inverse  $m_a(T)$
3. They remain stable as long as  $m_a(T)$  is increasing
4. Start to dilute once the axion reaches its zero-temperature mass



# Evolution of Oscillons

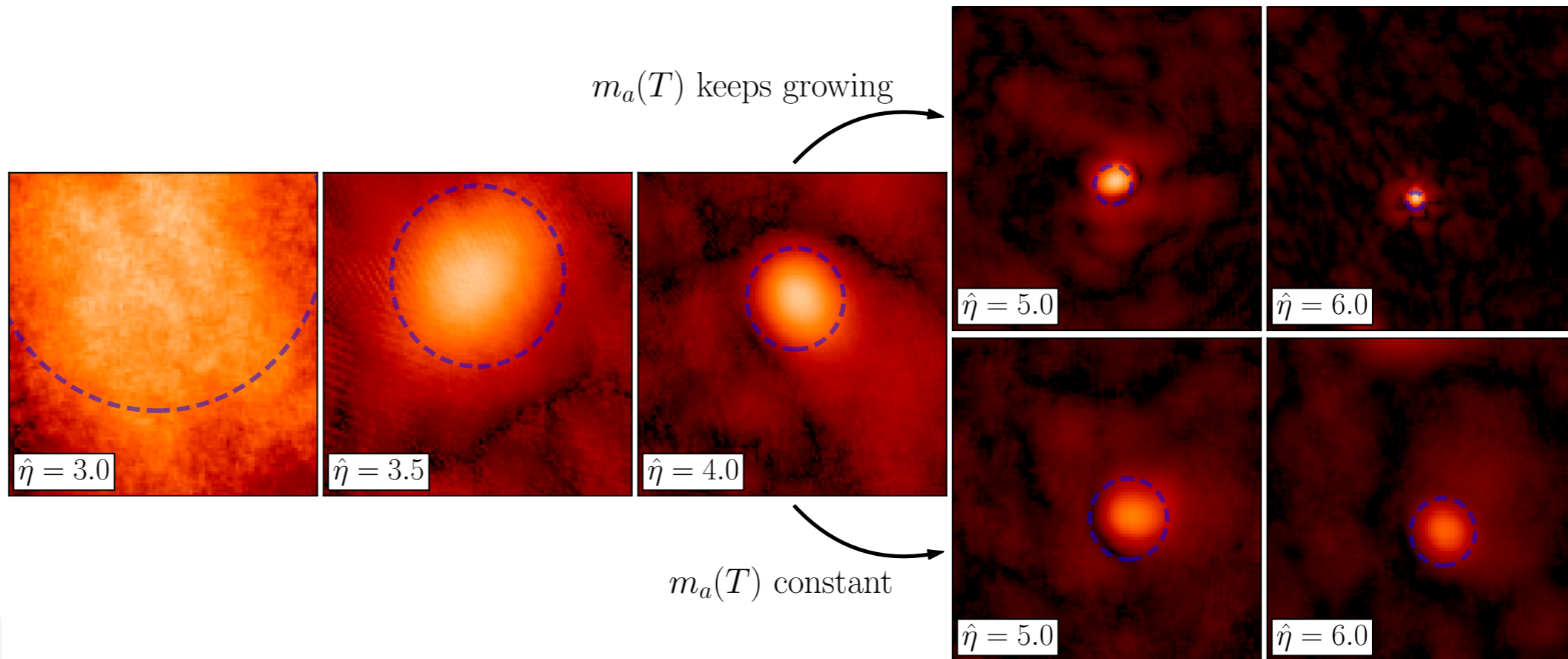
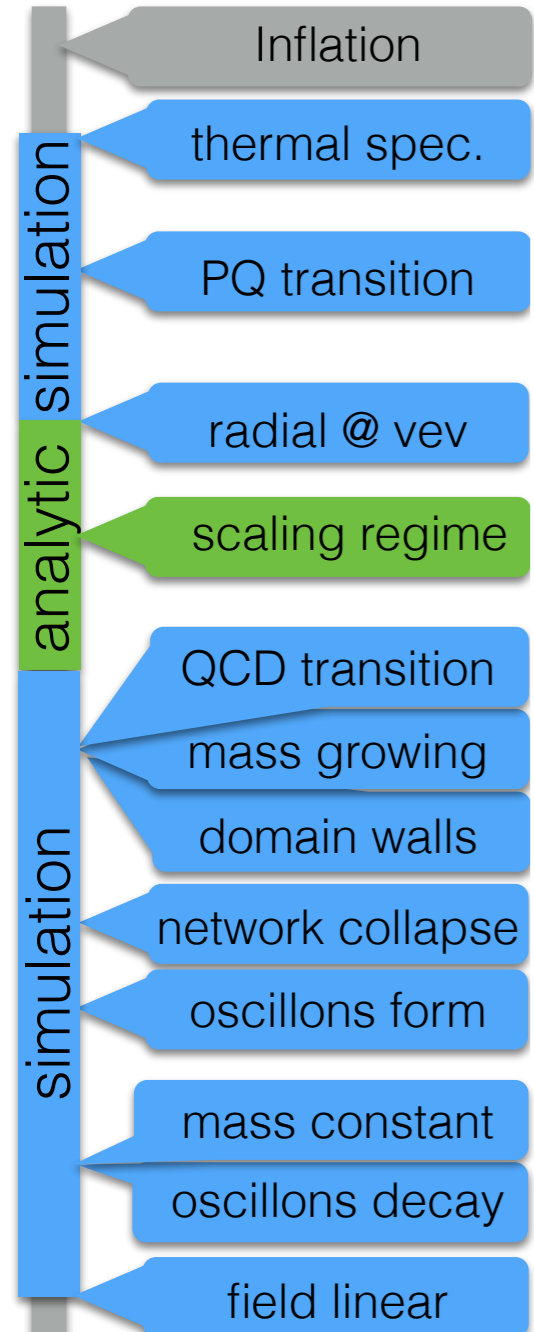


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time (not to scale)



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time (not to scale)

analytic simulation

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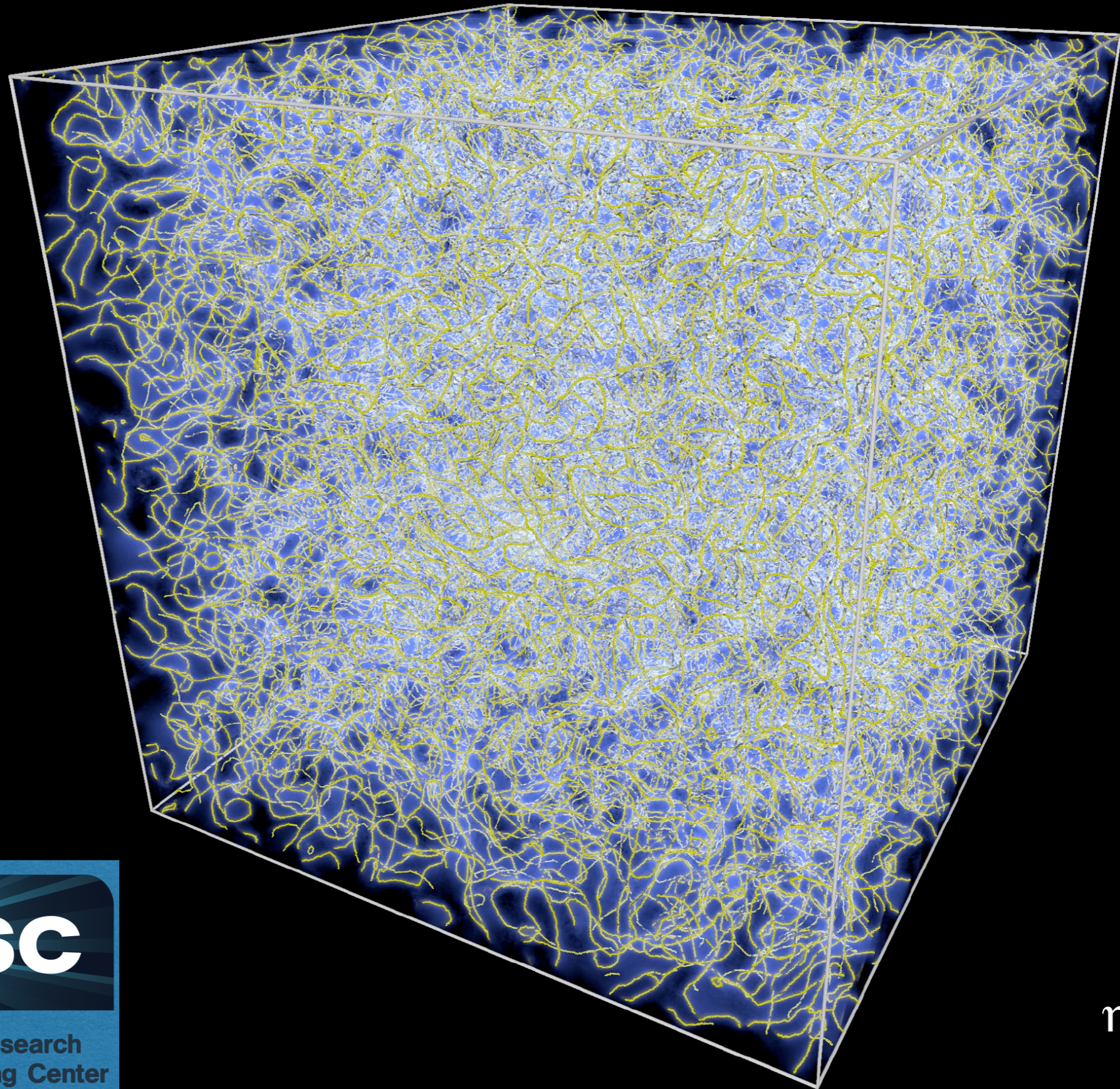
network collapse

oscillons form

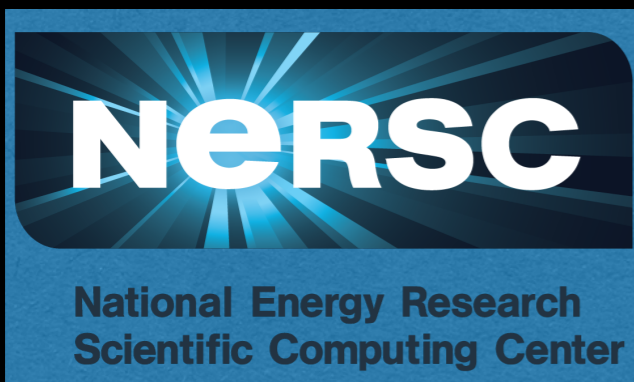
mass constant

oscillons decay

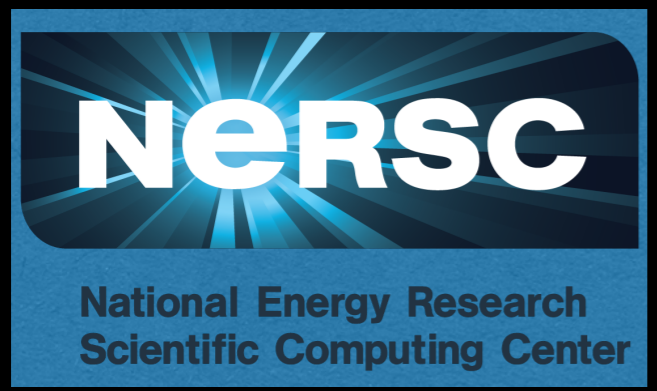
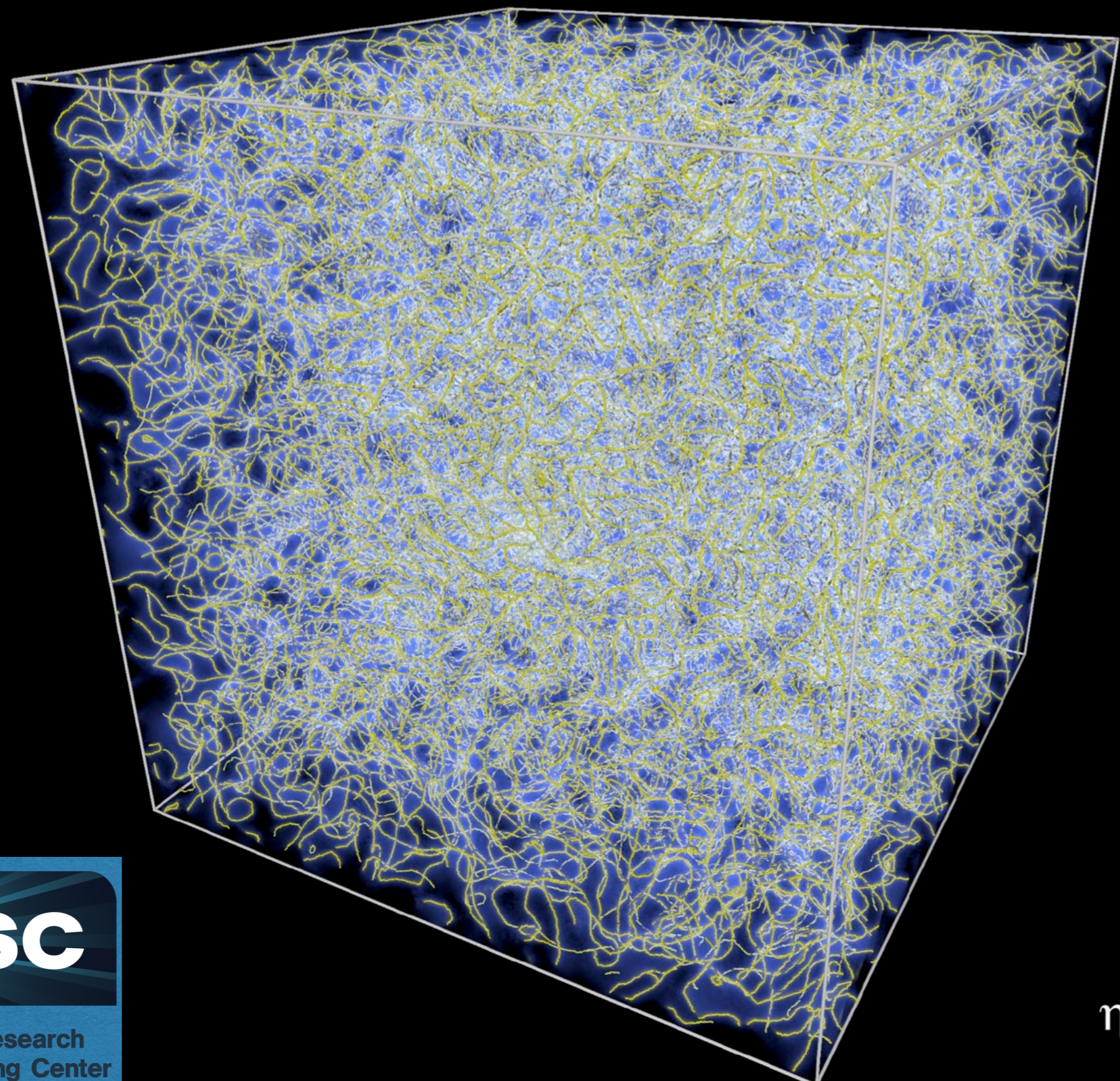
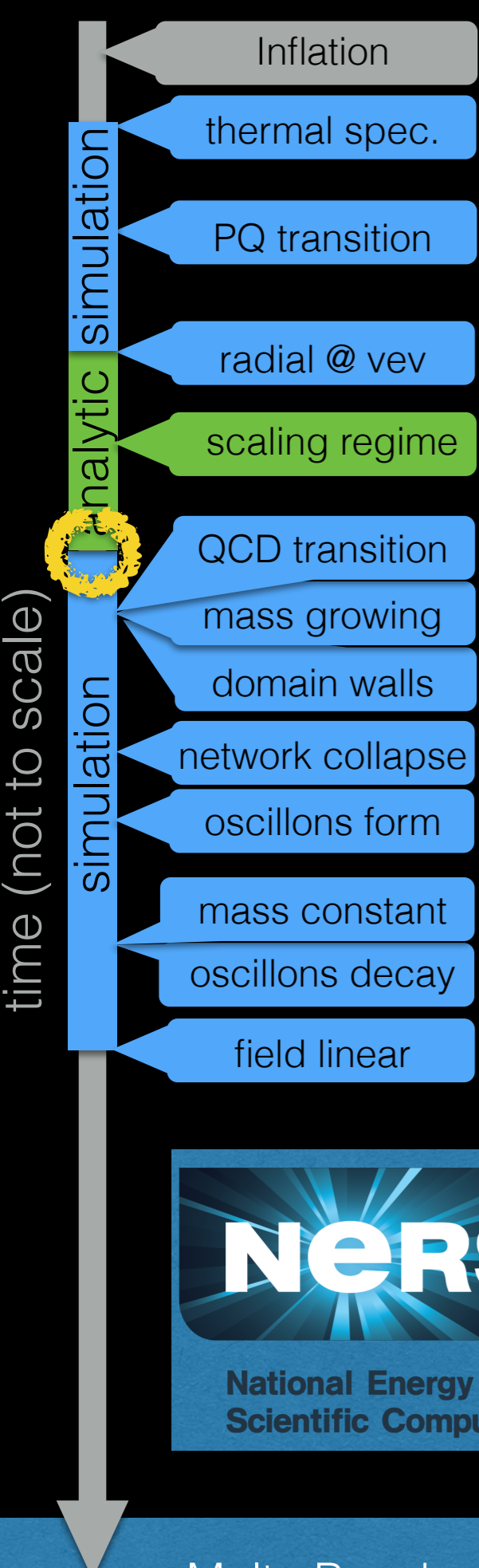
field linear



$\eta=0.40$



<https://youtu.be/1By1DMq1Epl>



$\eta=0.40$

<https://youtu.be/1By1DMq1Epl>

time (not to scale)

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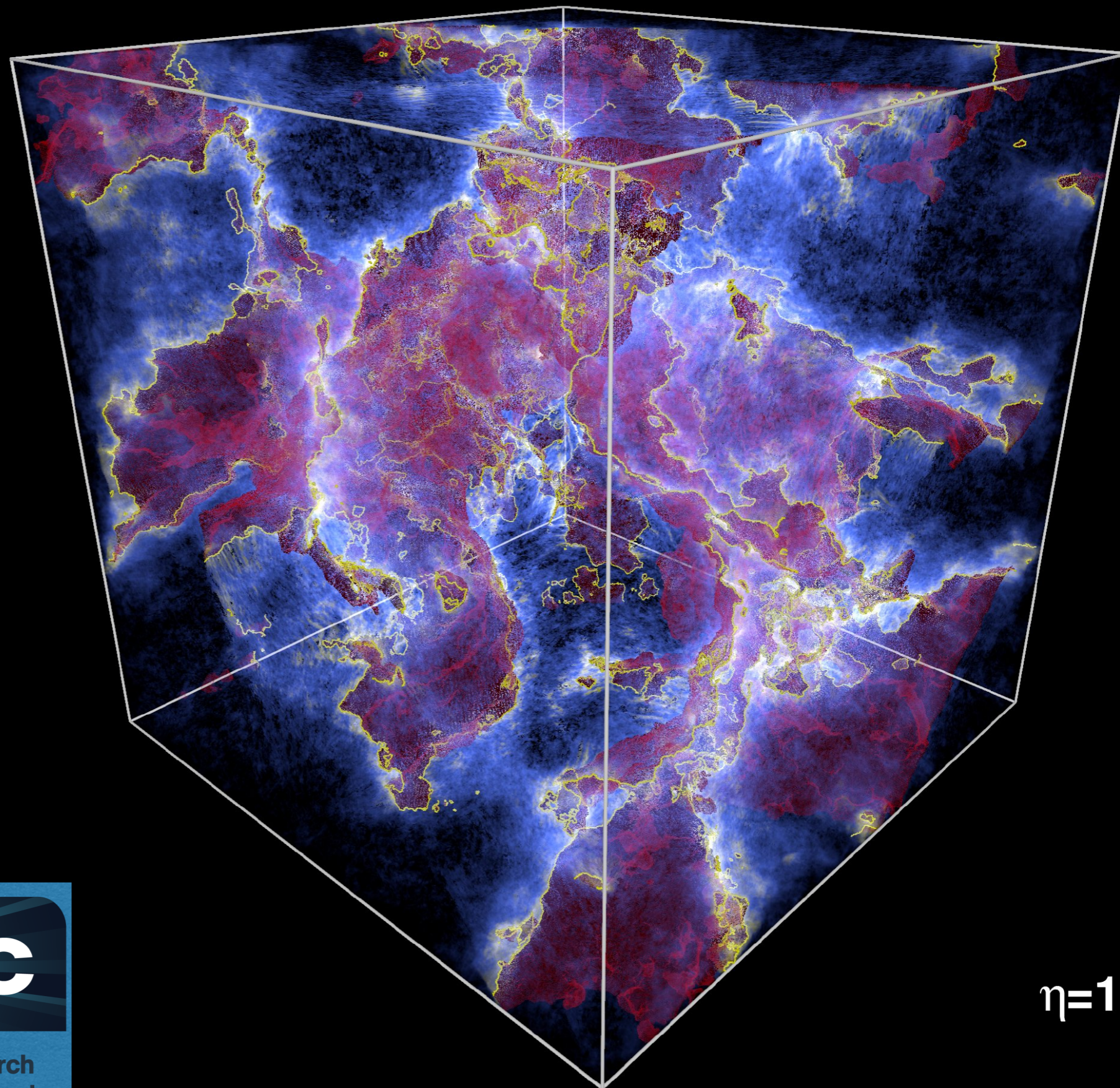
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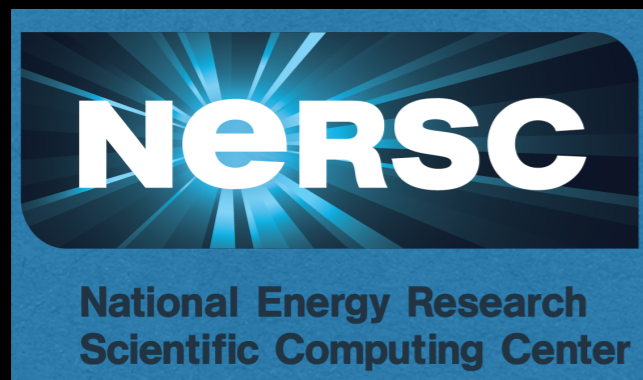
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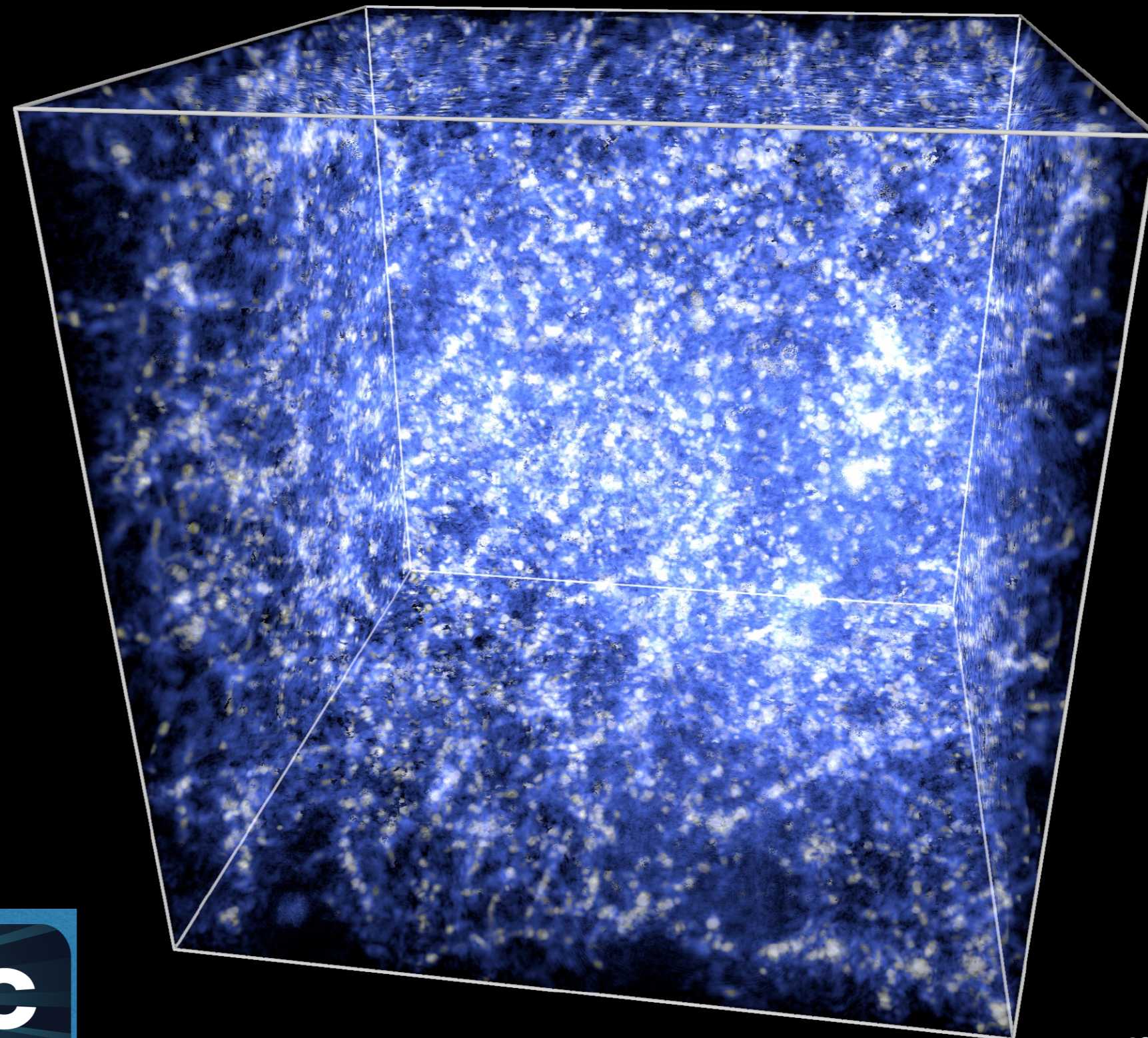
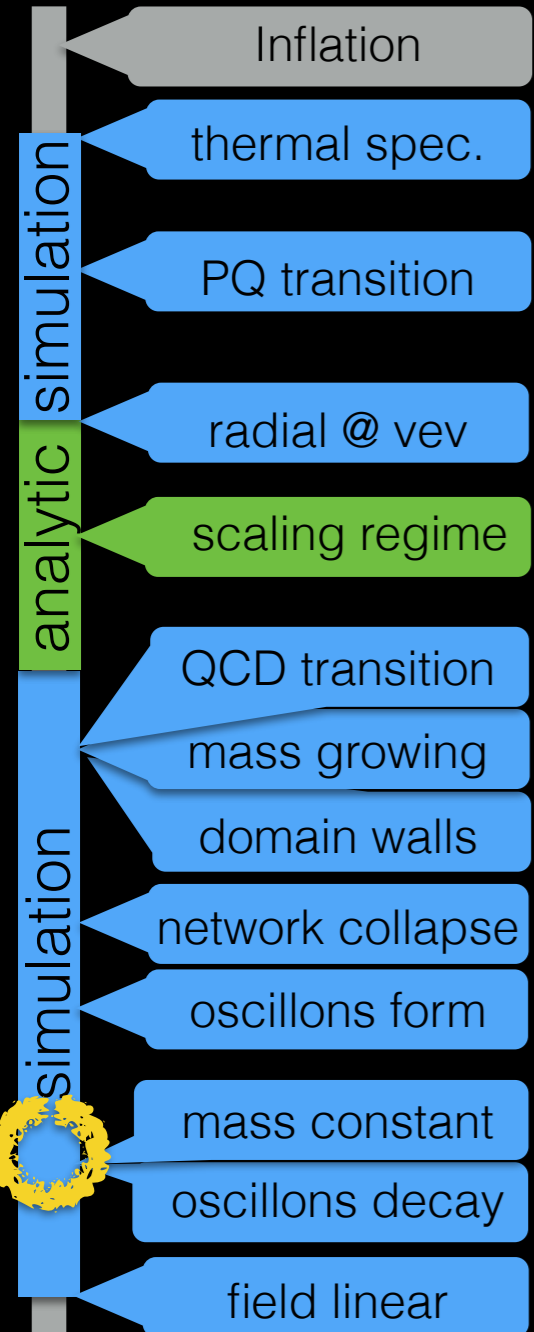


$\eta=1.10$

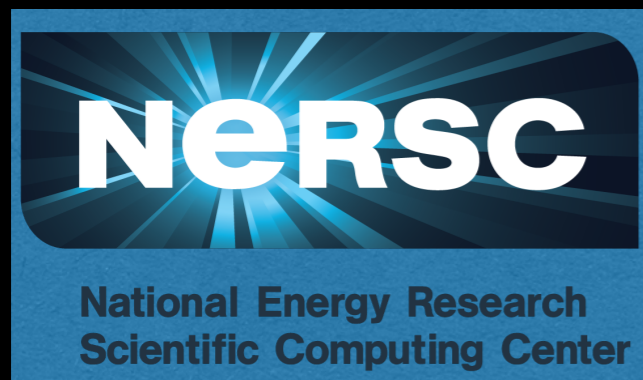


<https://youtu.be/1By1DMq1Epl>

time (not to scale)



$\eta=3.90$



<https://youtu.be/1By1DMq1Epl>

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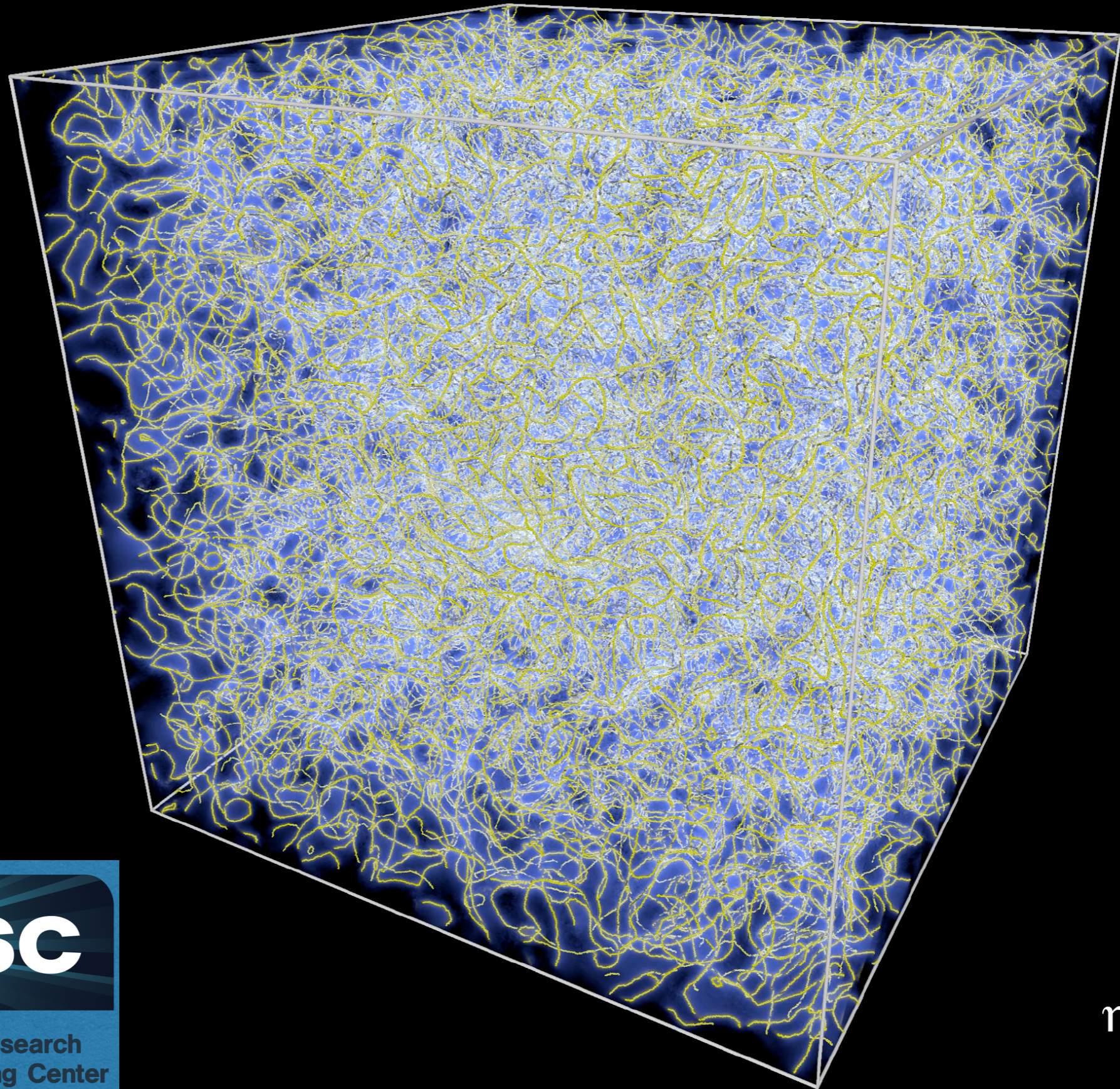
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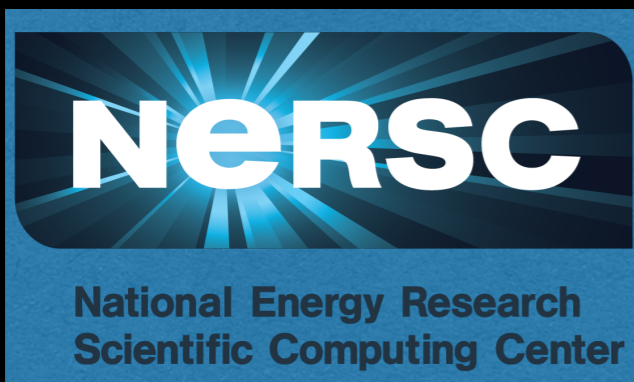
mass constant

oscillons decay

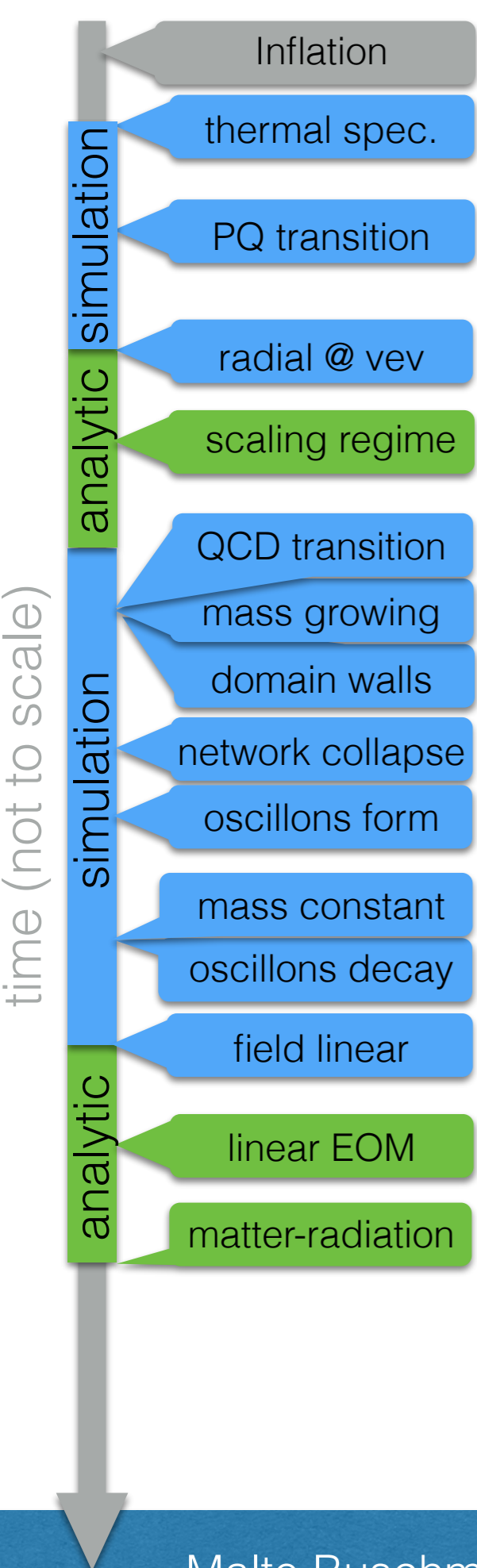
field linear



$\eta=0.40$

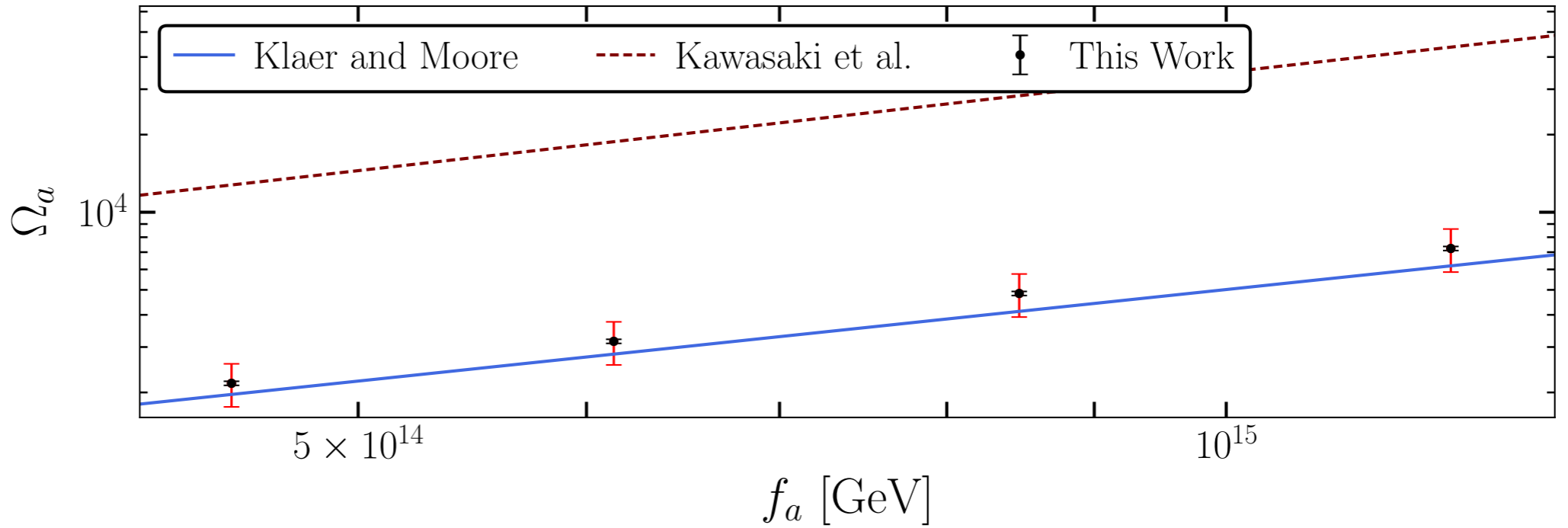
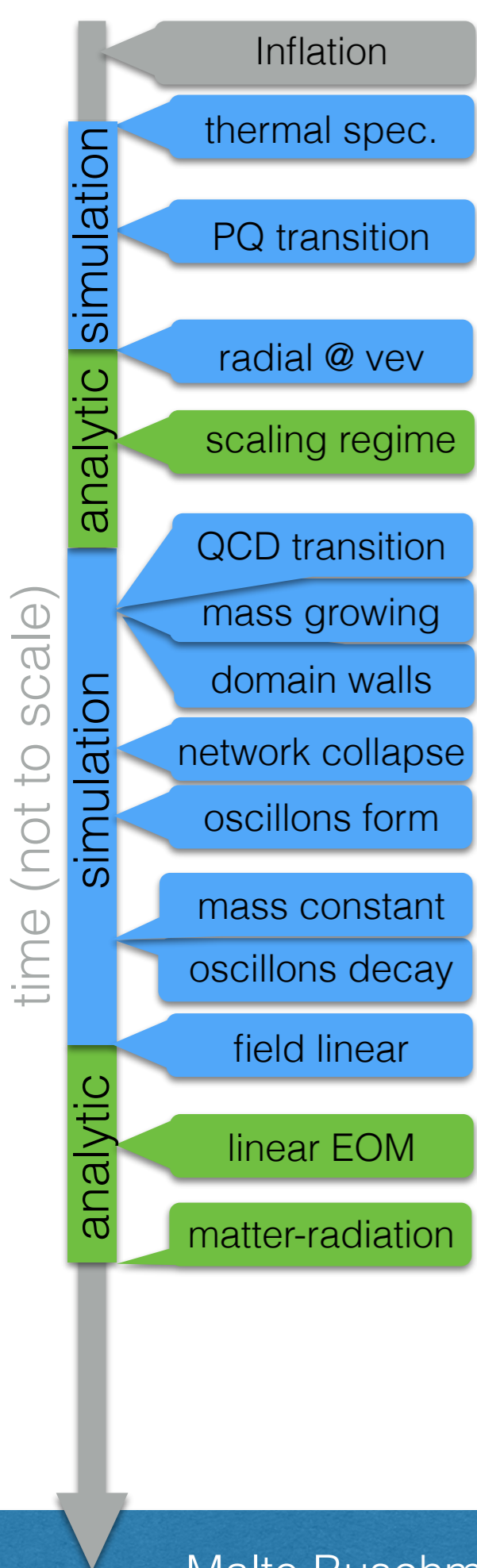


<https://youtu.be/1By1DMq1Epl>

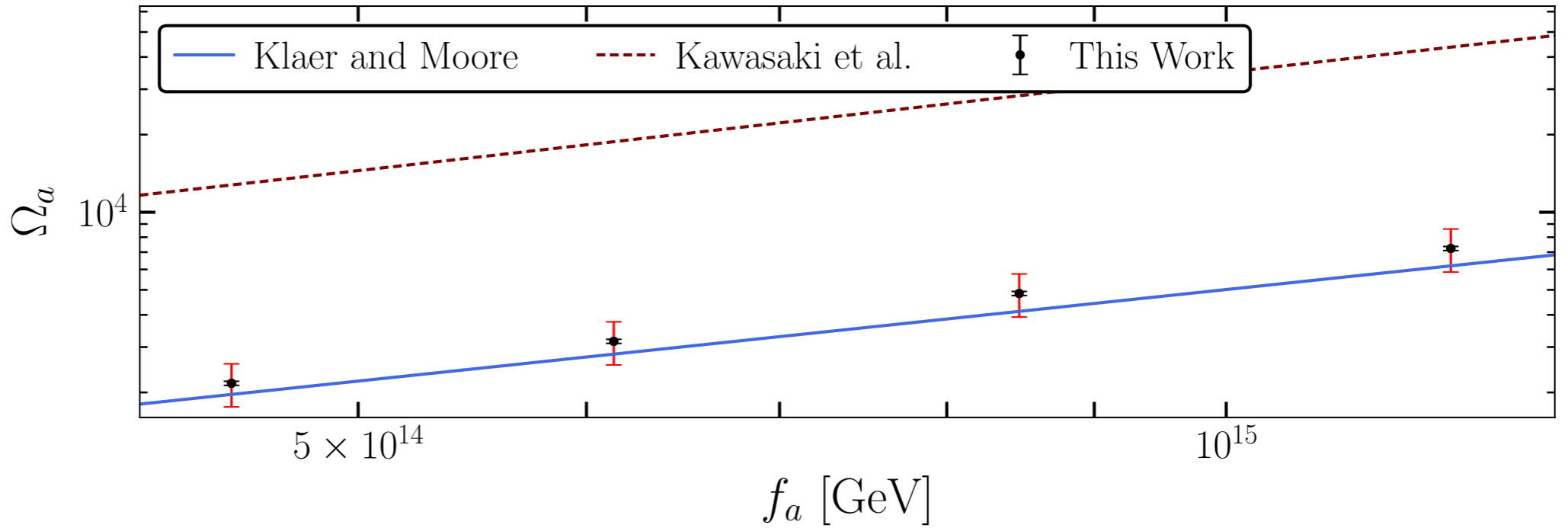
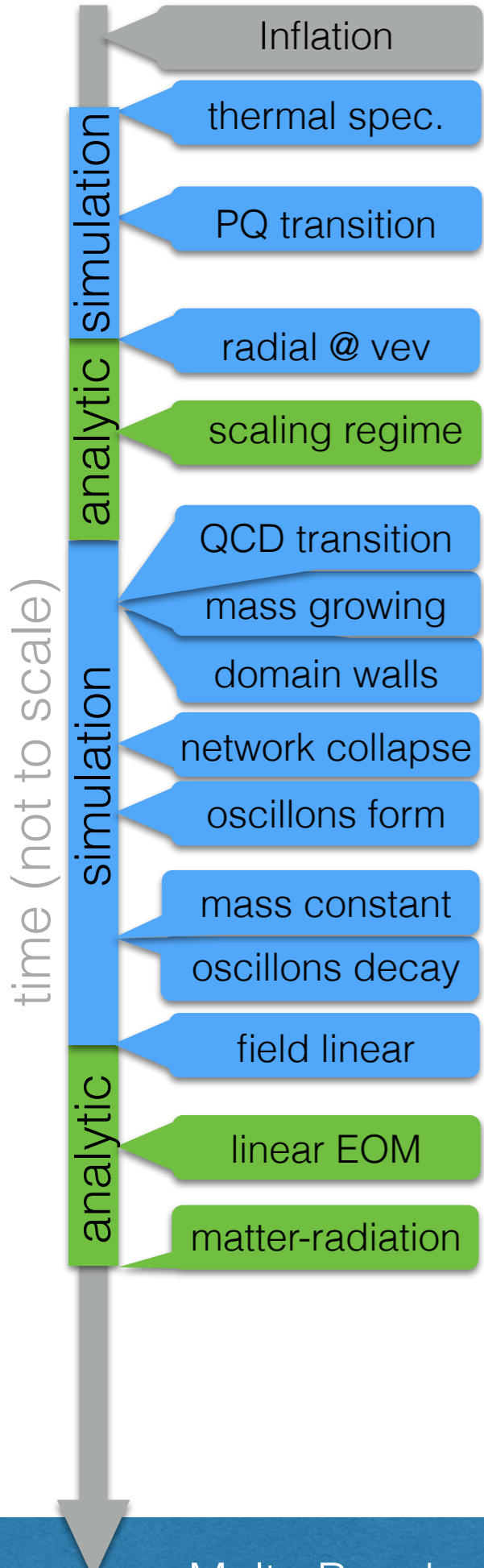




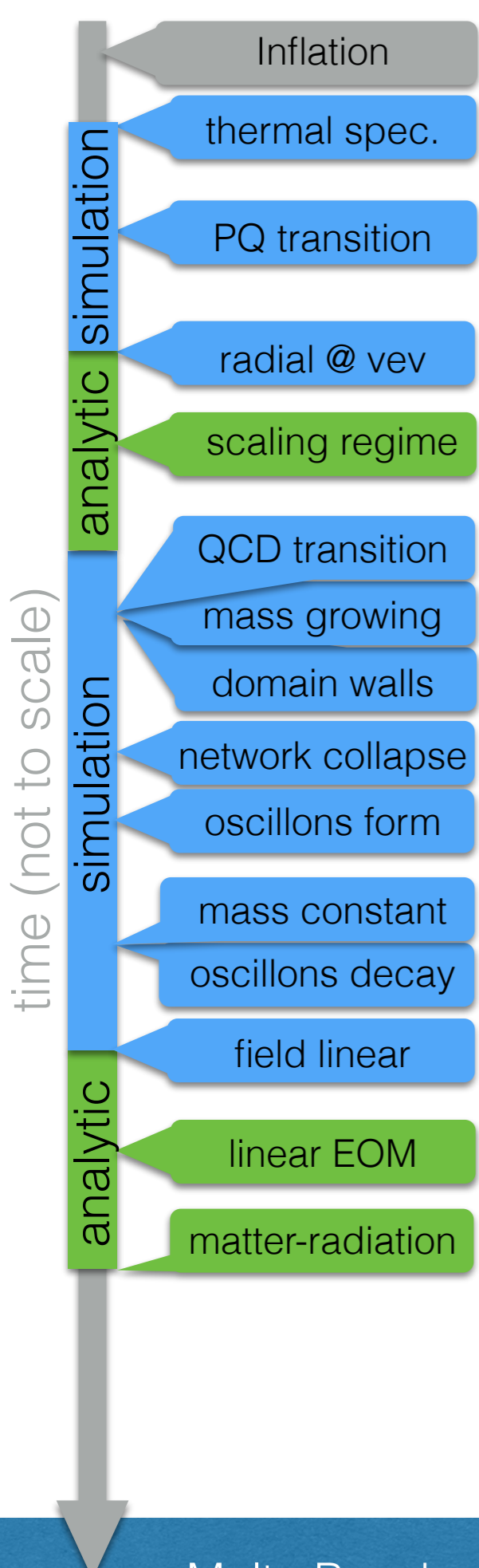
# Obtaining the relic abundance



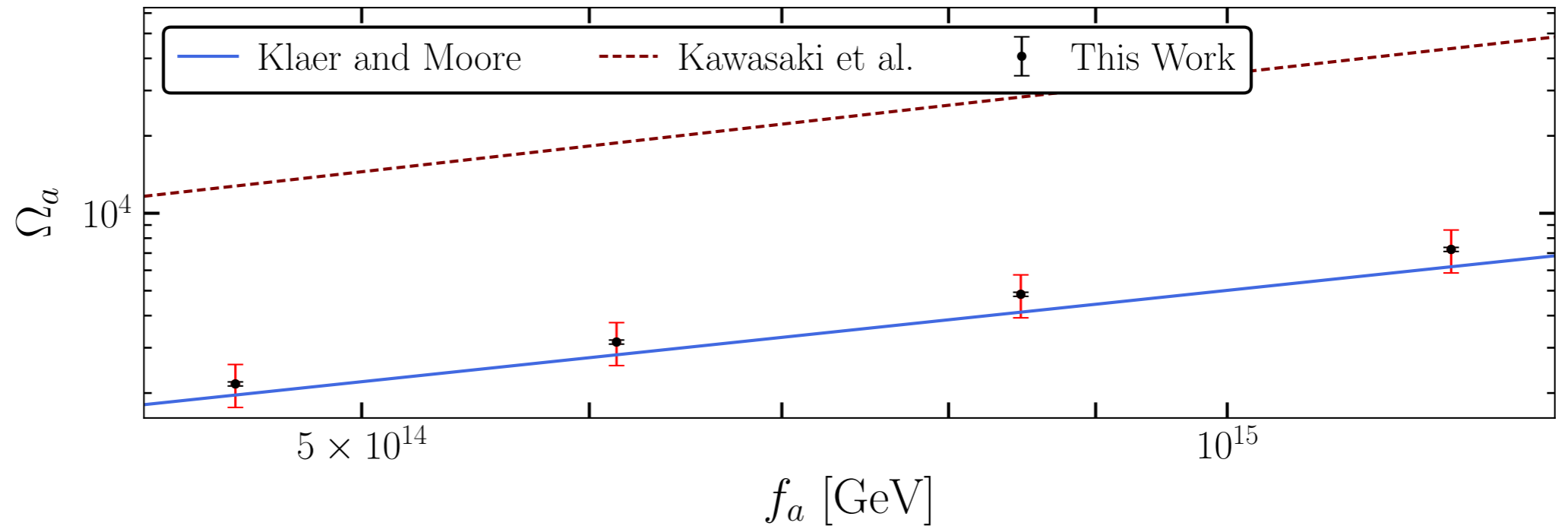
# Obtaining the relic abundance



Correct relic abundance reached for:  
 $m_a = 25.2 \pm 11.0 \mu\text{eV}$



# Obtaining the relic abundance



Correct relic abundance reached for:

$$m_a = 25.2 \pm 11.0 \mu\text{eV}$$

## Uncertainties coming from:

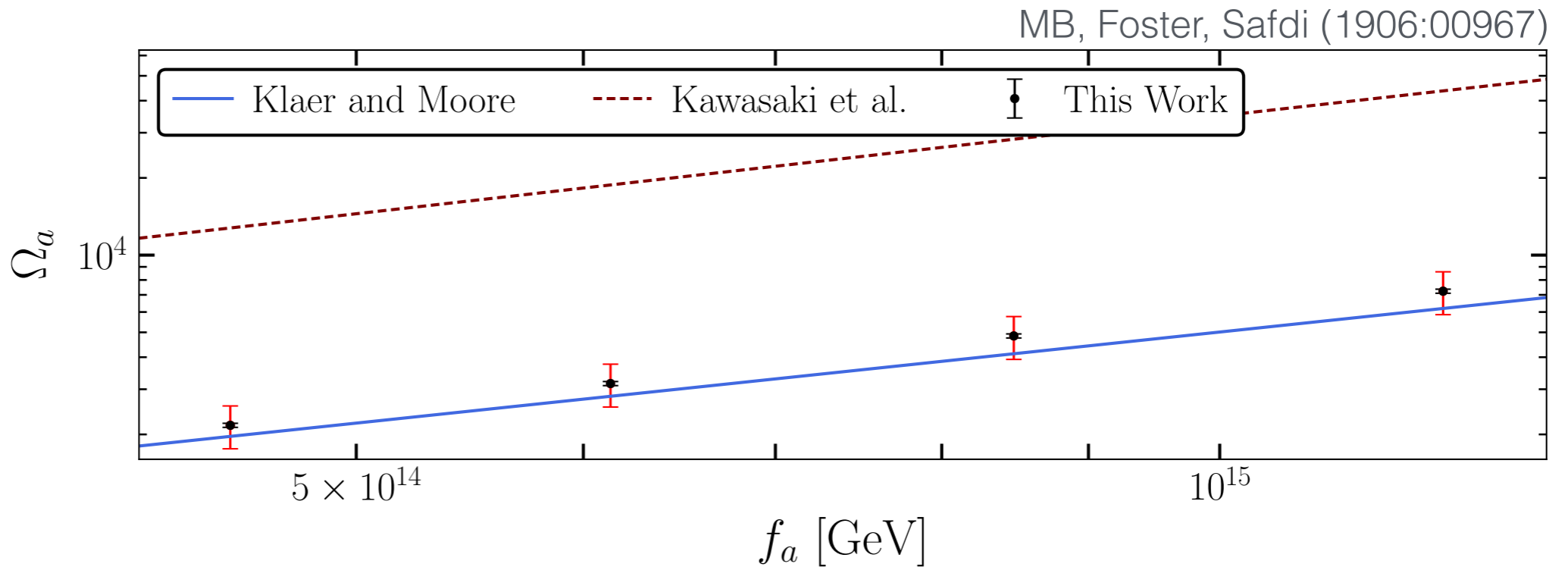
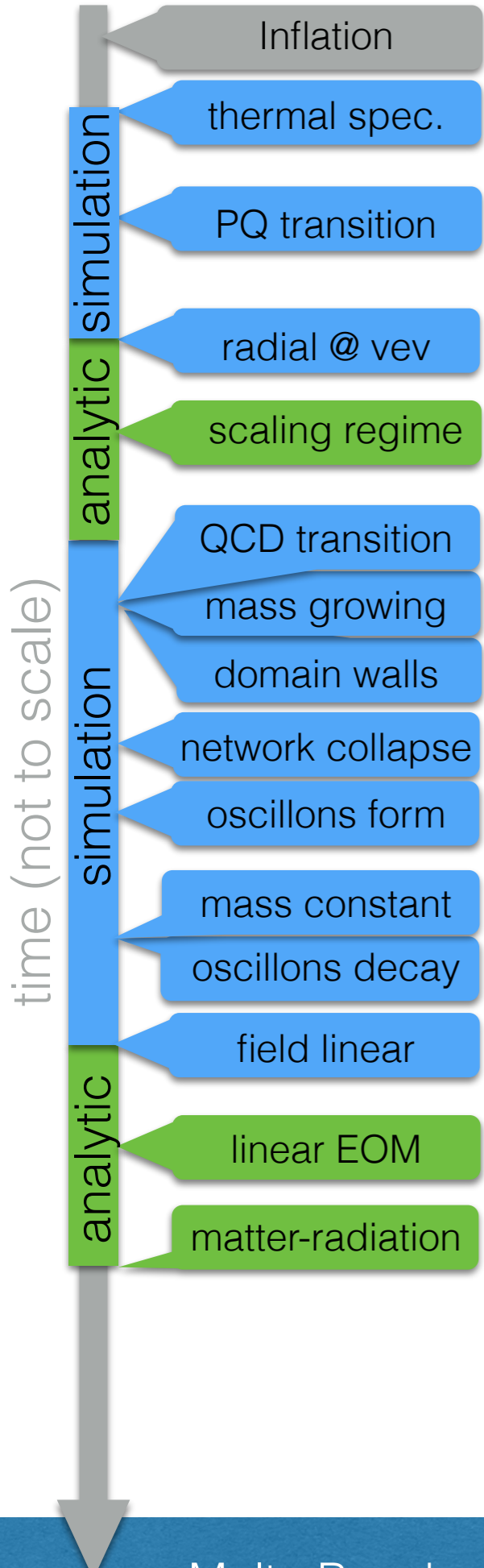
31% uncertainty on the relation between abundance and  $f_a$

27% uncertainty from mass growth  $m_a(T)$

15% from violation of scaling regime

~10% others: statistical, fixed degrees of freedom,...

# Sources of Uncertainties on the Axion Mass



In particular oscillons make it impossible to simulate at low breaking scales. Extrapolations needed:

$$\rho_a \propto f_a^{(6+n)/(4+n)}$$

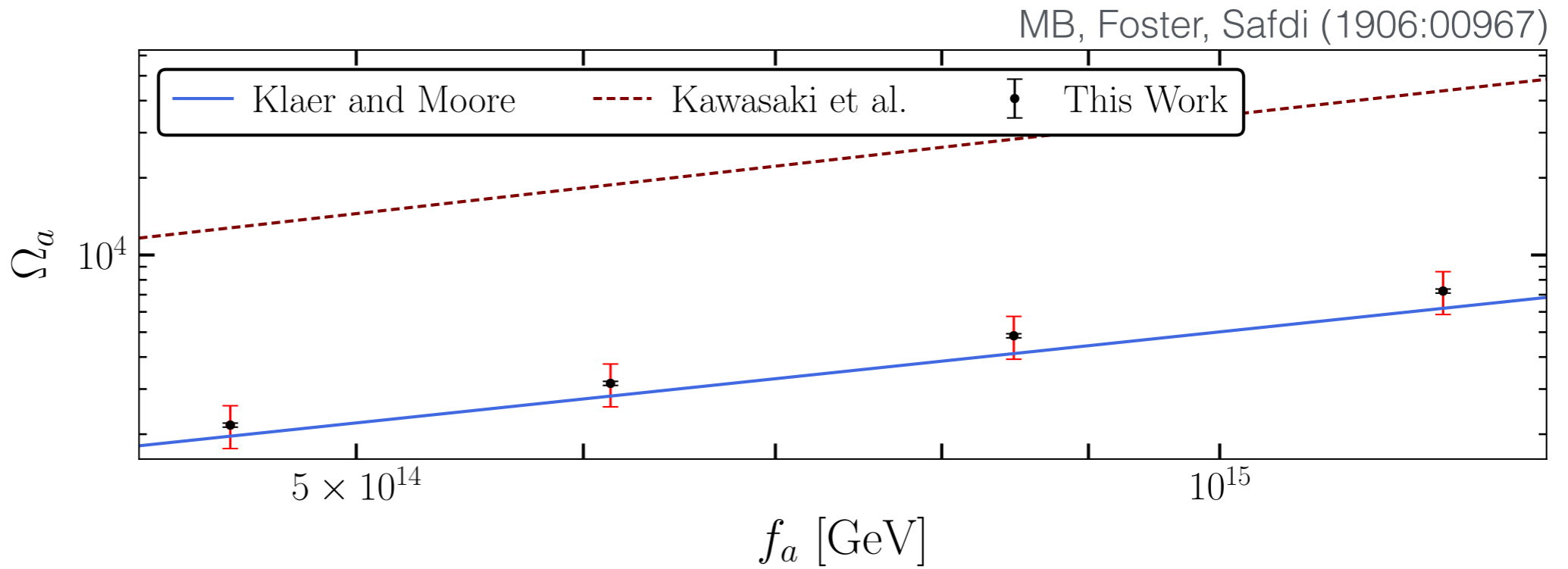
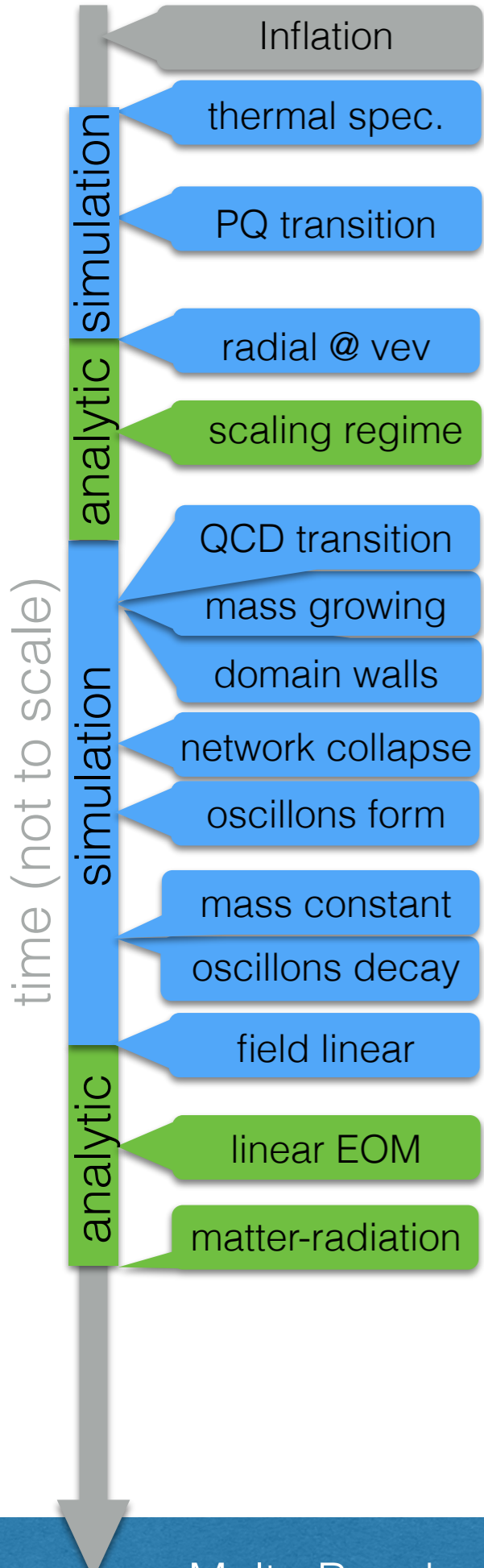
with  $n=6.68$  from lattice simulations

**Expected:**  $\alpha = (n + 6)/(n + 4) \approx 1.187$ .

**Simulation:**  $\alpha = 1.24 \pm 0.04$ .

**Leads to 31% uncertainty on axion mass**

# Sources of Uncertainties on the Axion Mass



In particular oscillons make it impossible to simulate at low breaking scales. Extrapolations needed:

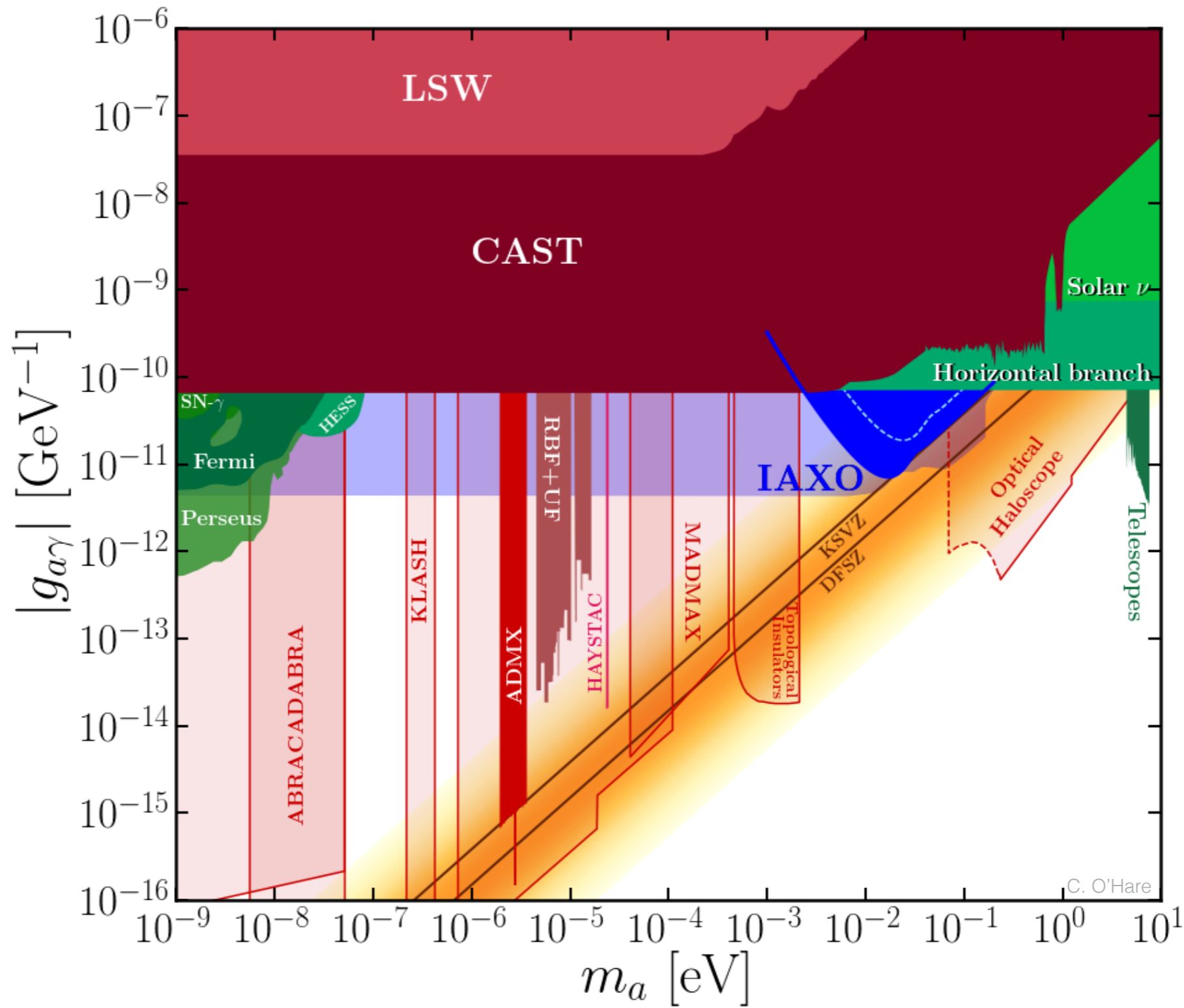
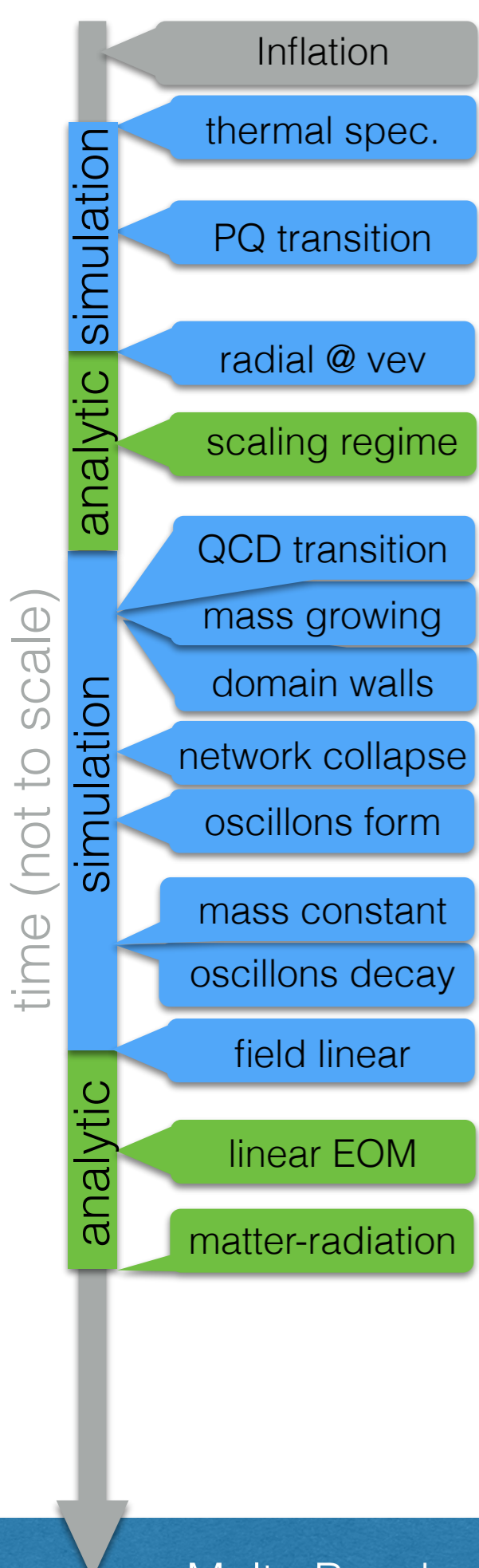
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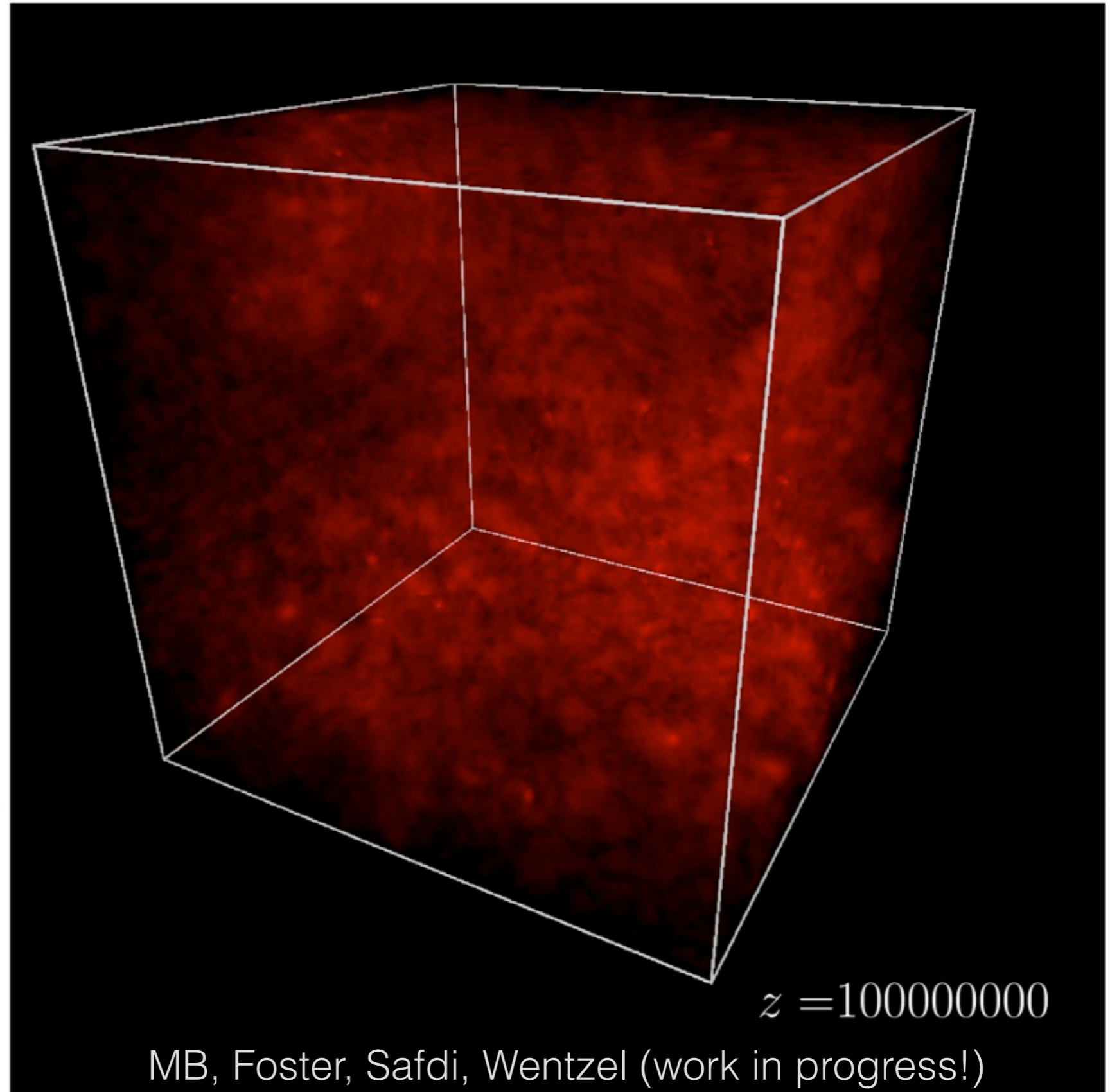
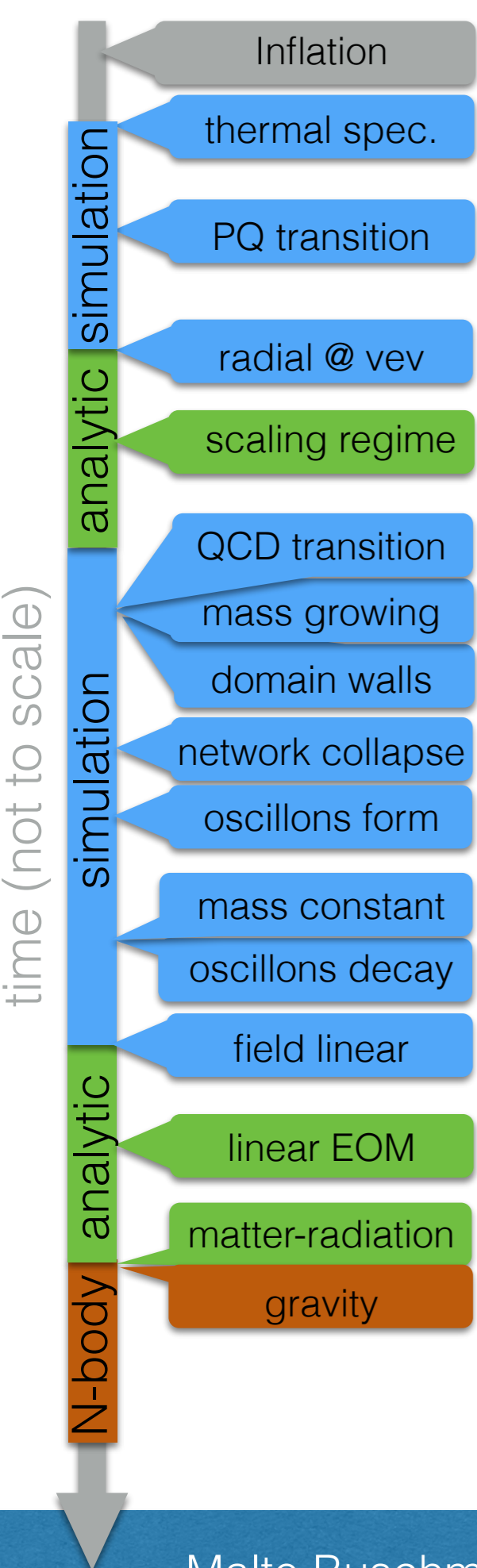
Could be as high as 8.2!

We rerun simulation with 8.2 (in 2D)

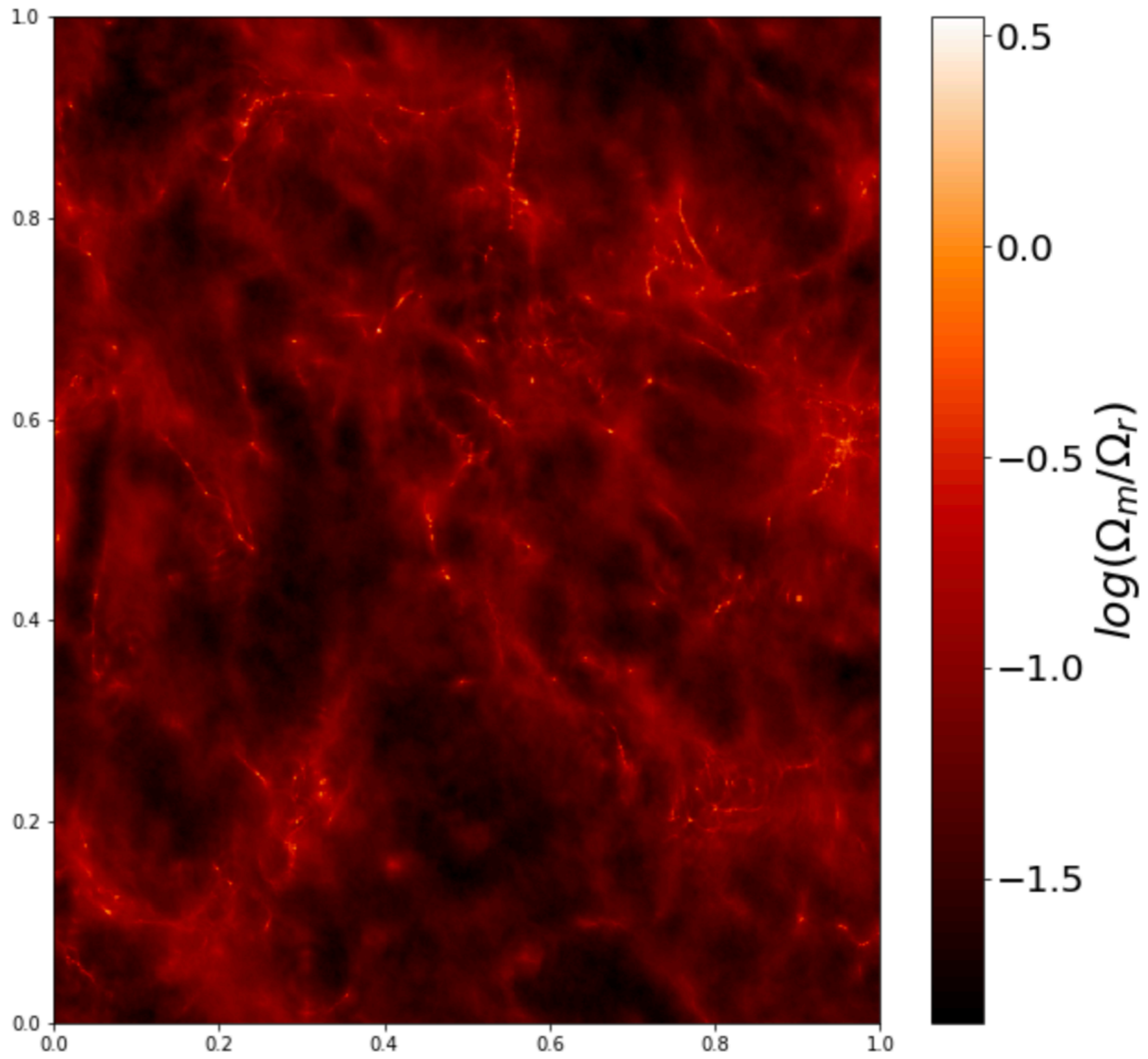
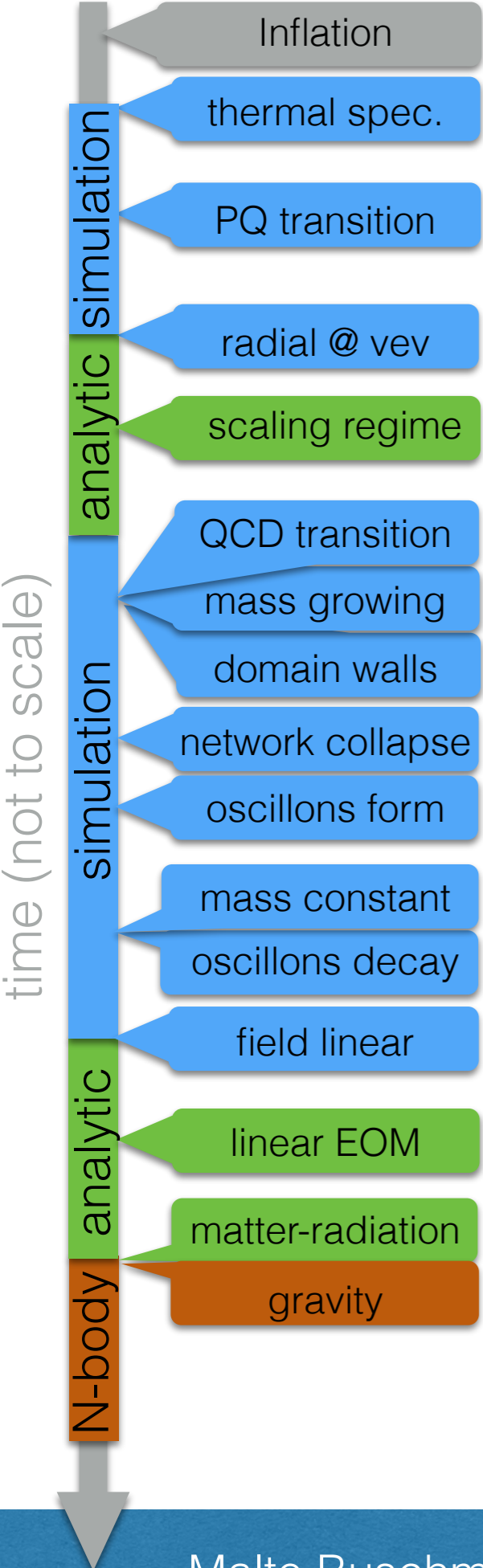
**Leads to 27% uncertainty on axion mass**



# Halos collapse further under gravity



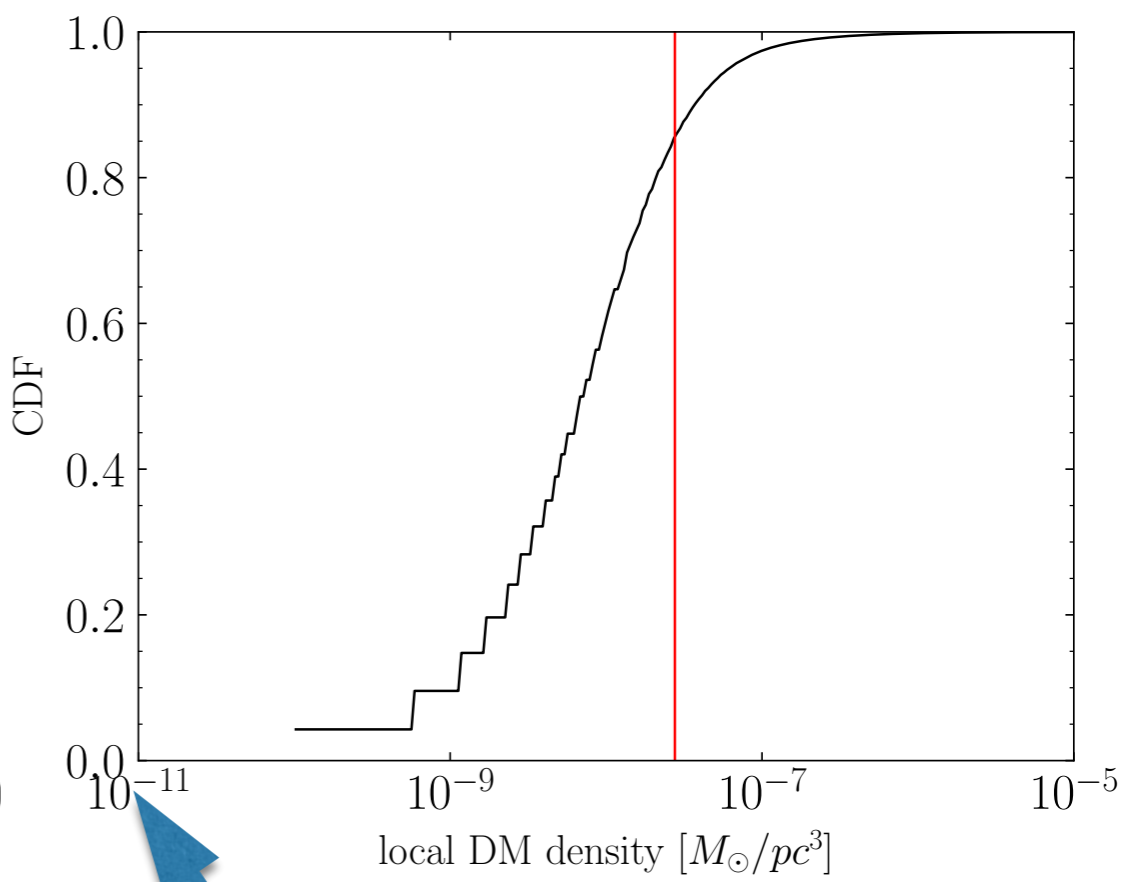
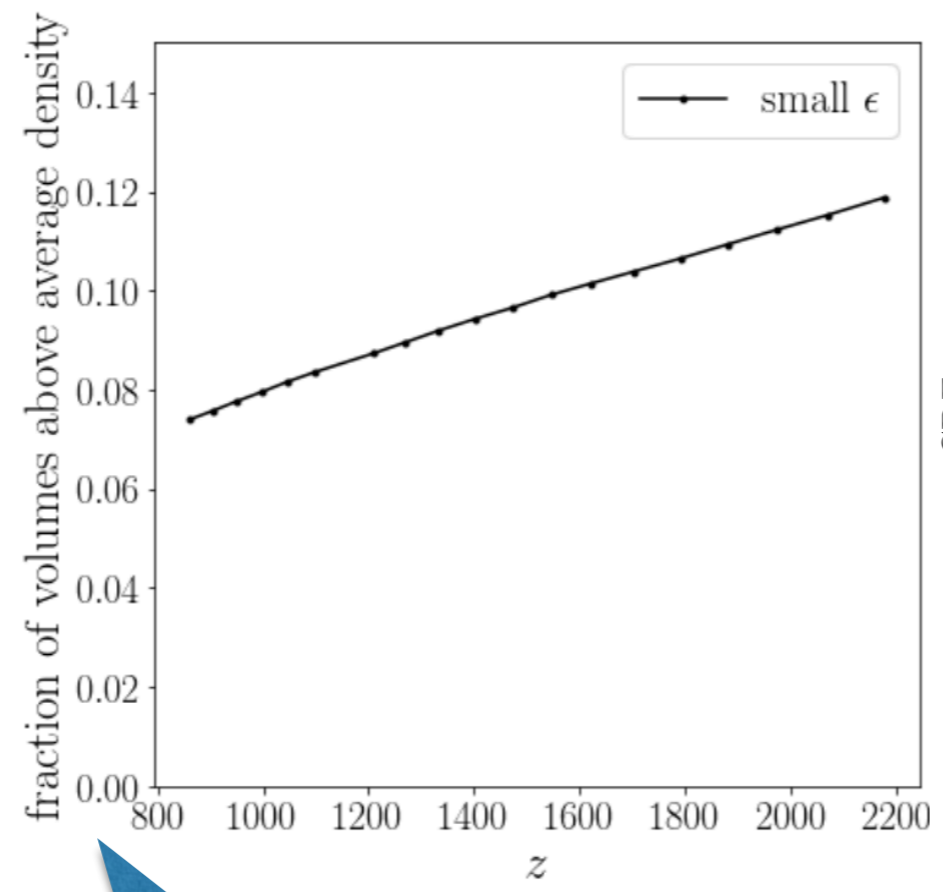
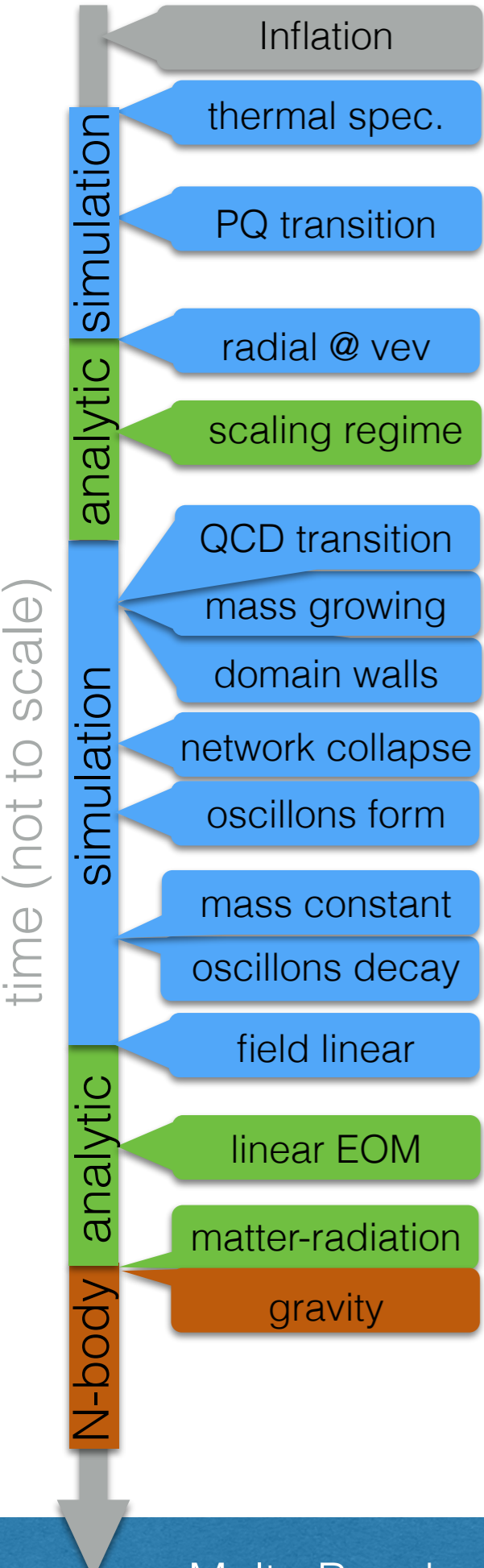
# Halos collapse further under gravity



MB, Foster, Safdi, Wentzel (work in progress!)



# Are we sitting in a void?



Probability of Earth being at location with a more-than-average DM density

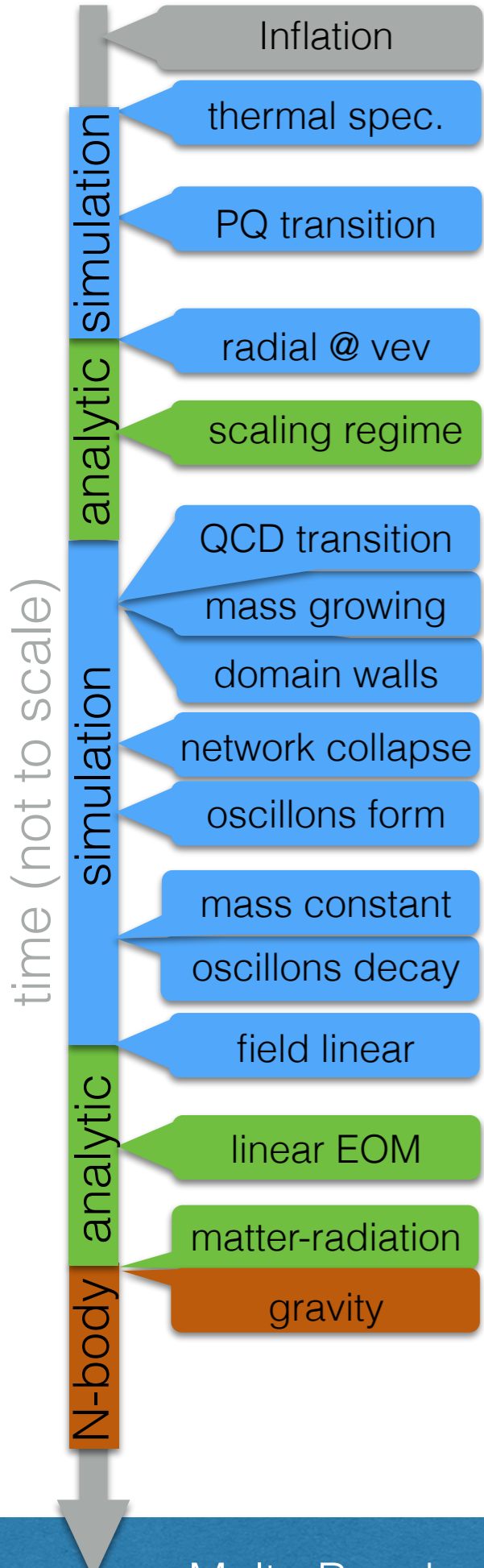


Probability of Earth being at location with a particular DM density or less

**Experiments like ADMX might not be able to detect a QCD axion in a post-inflationary scenario!**

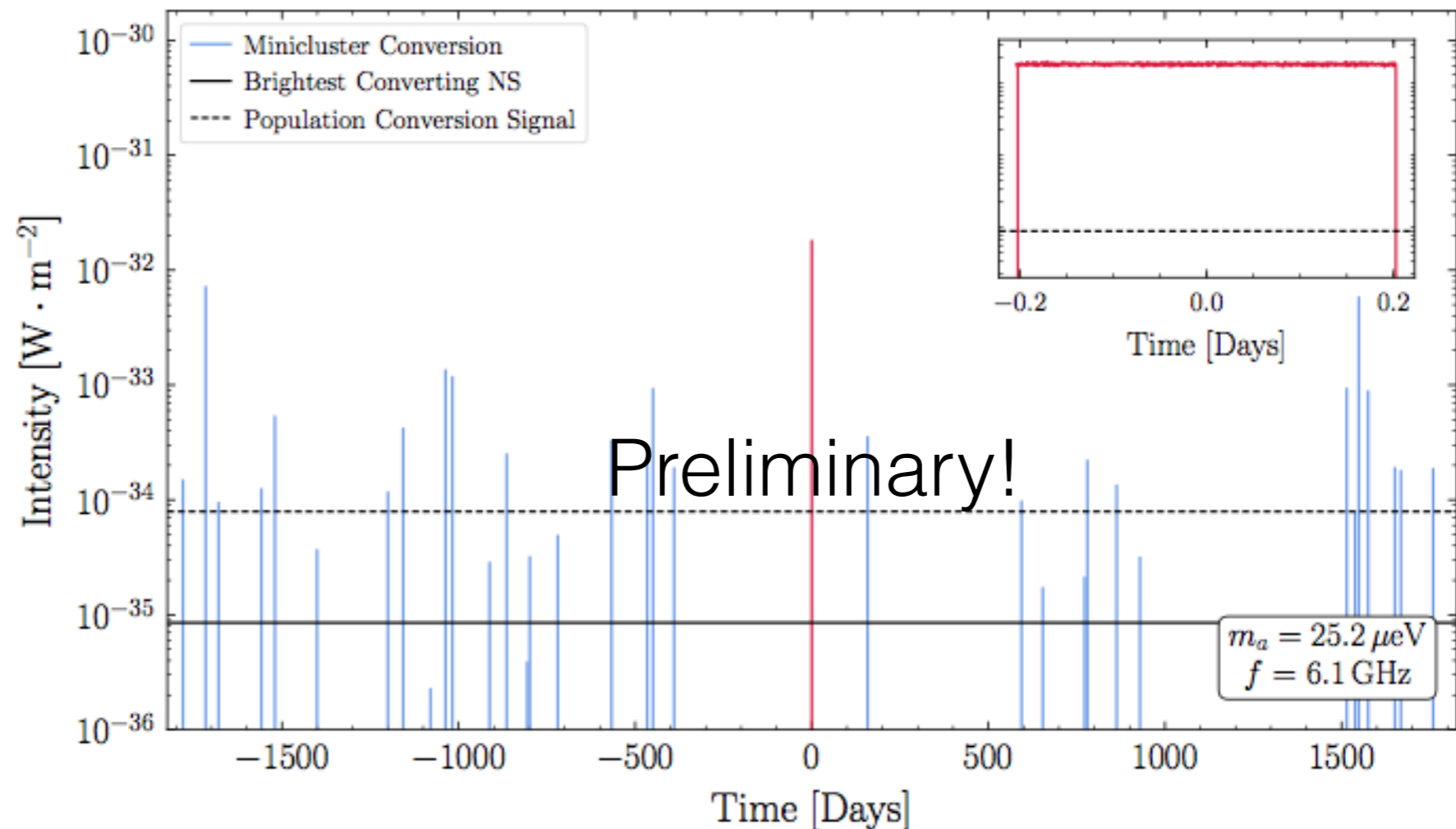
MB, Foster, Safdi, Wentzel (work in progress!)

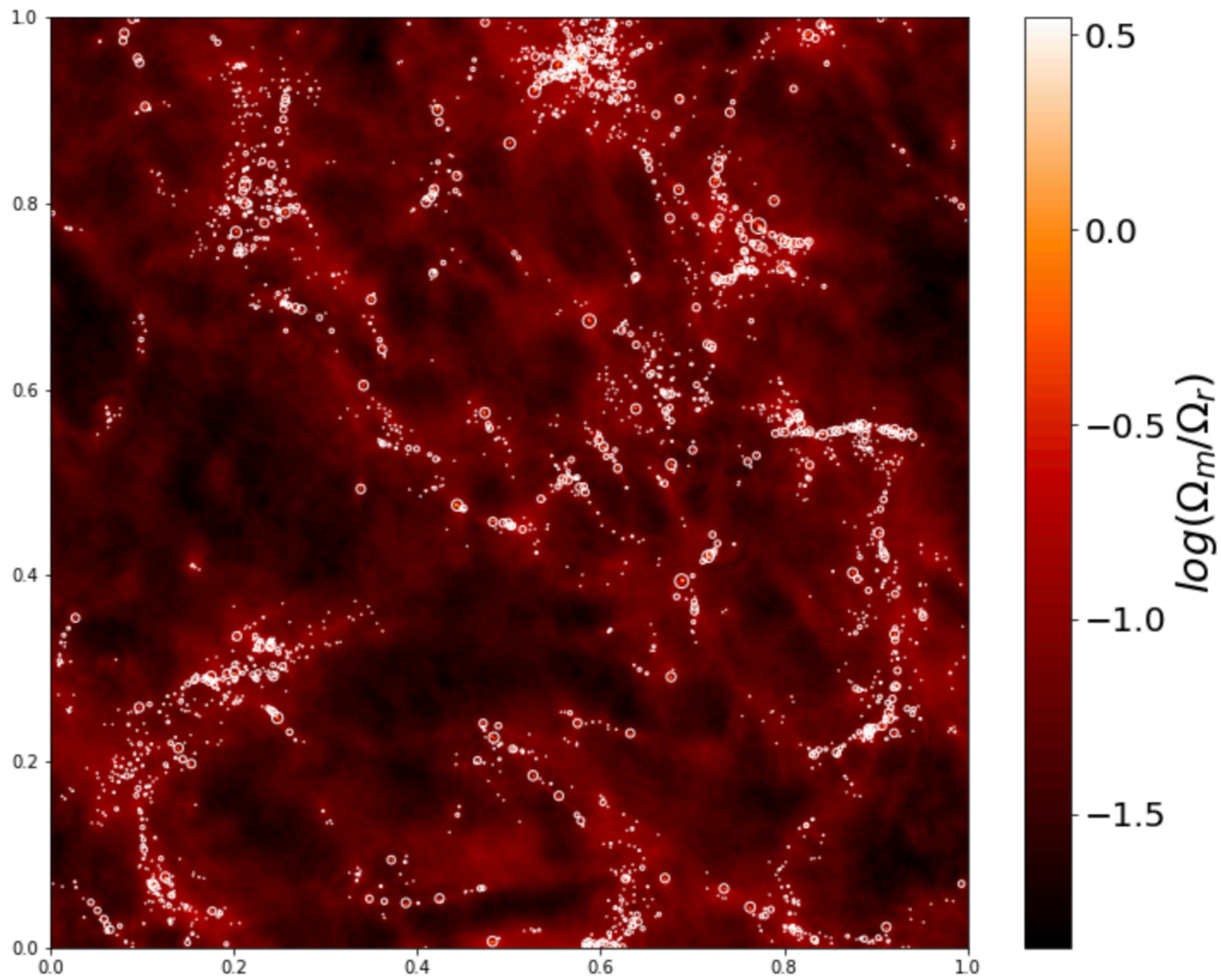
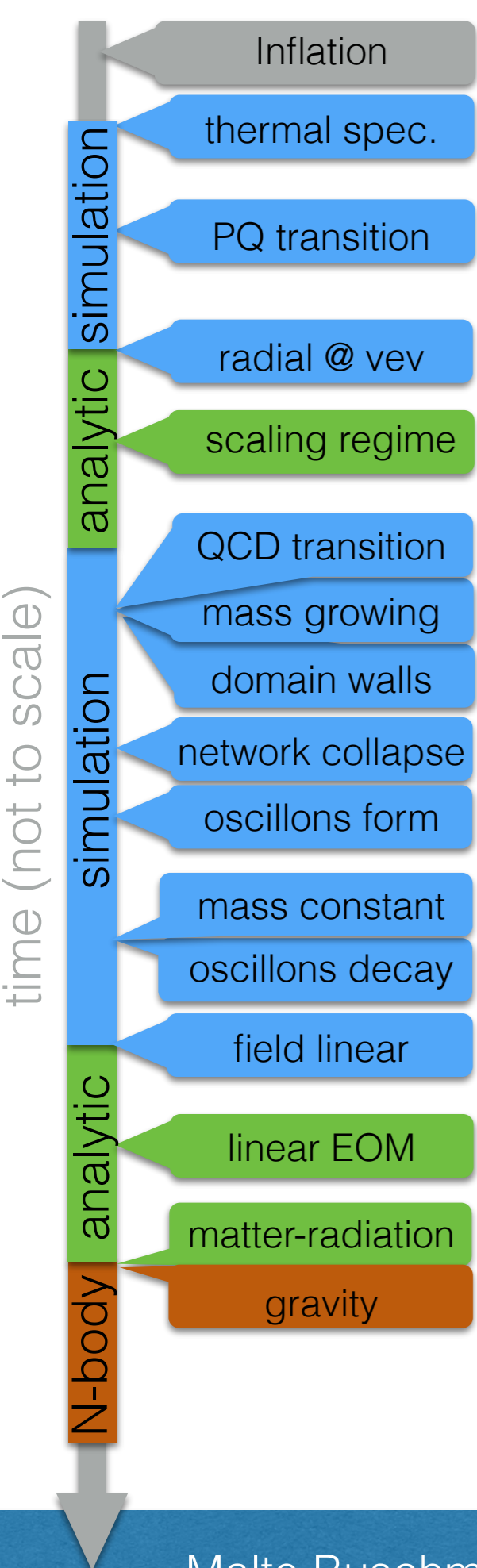
# Radio signals from Neutron Stars



Axions convert to radio photons in magnetic field of neutron star

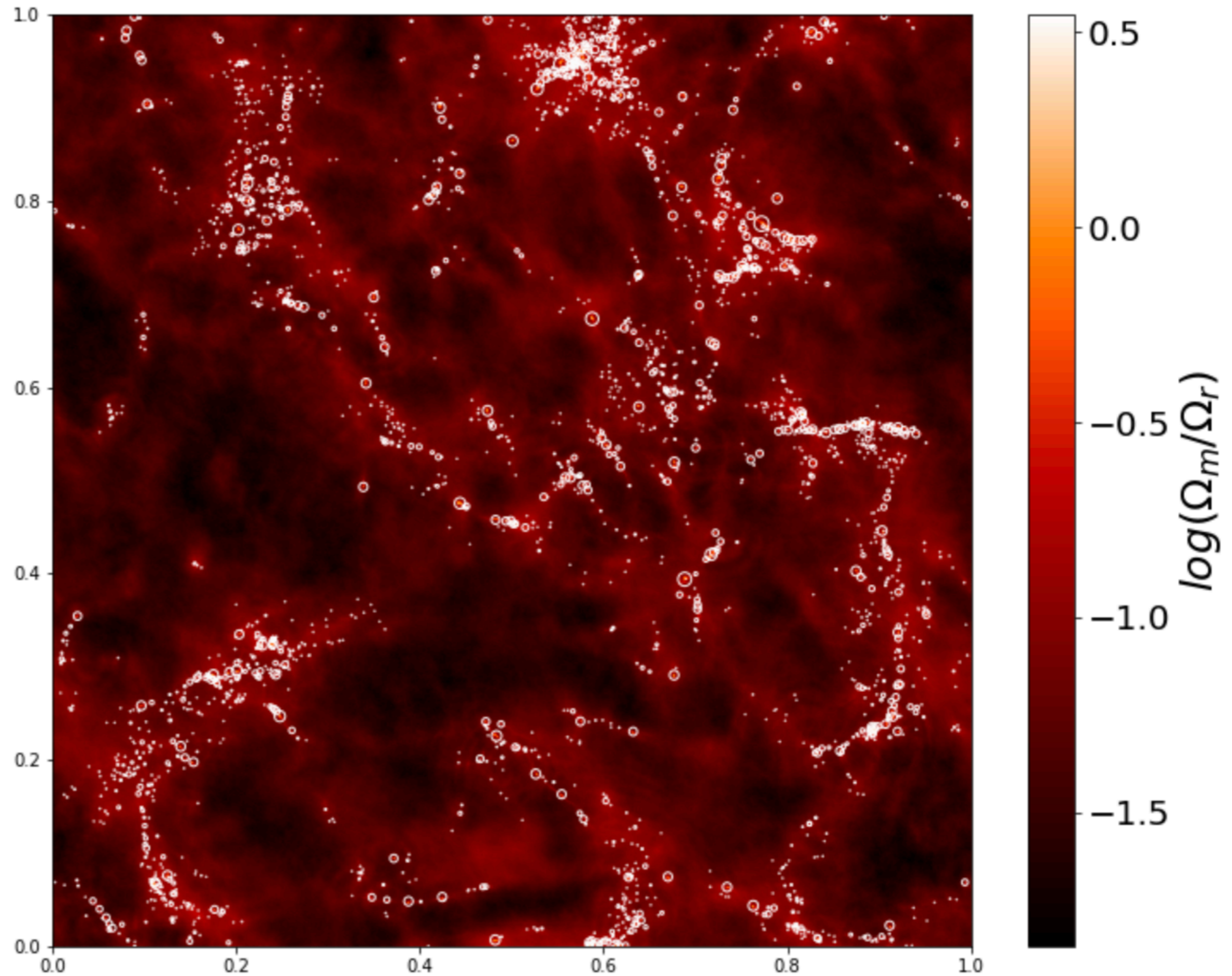
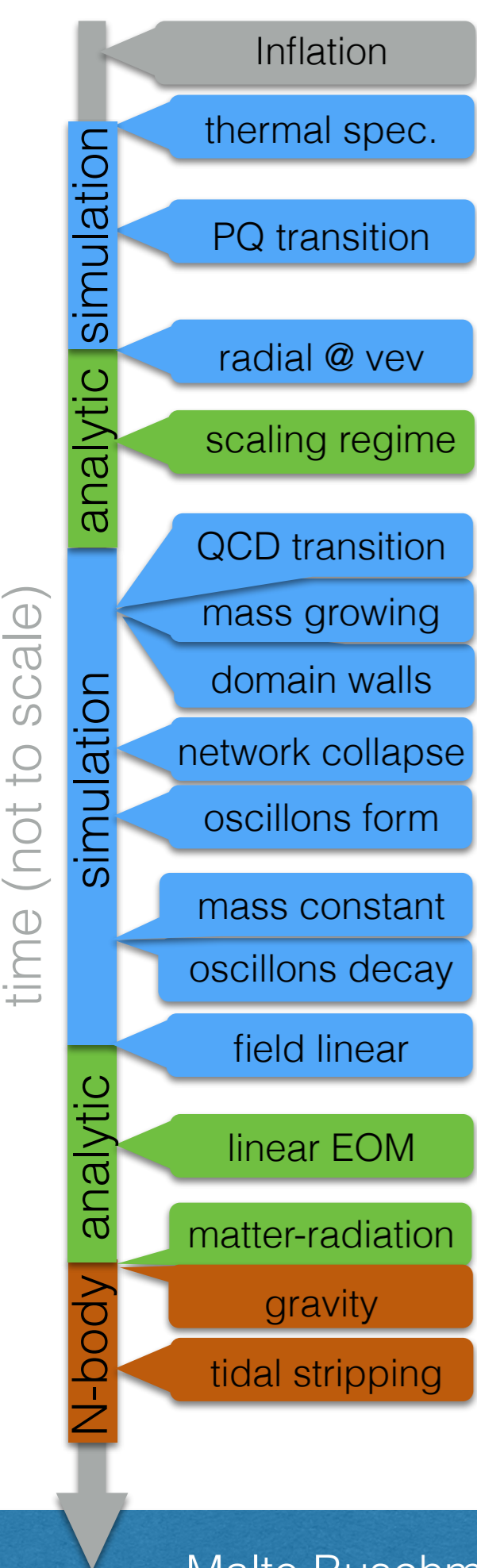
Large peak in flux when neutron star moves through an axion minihalo!





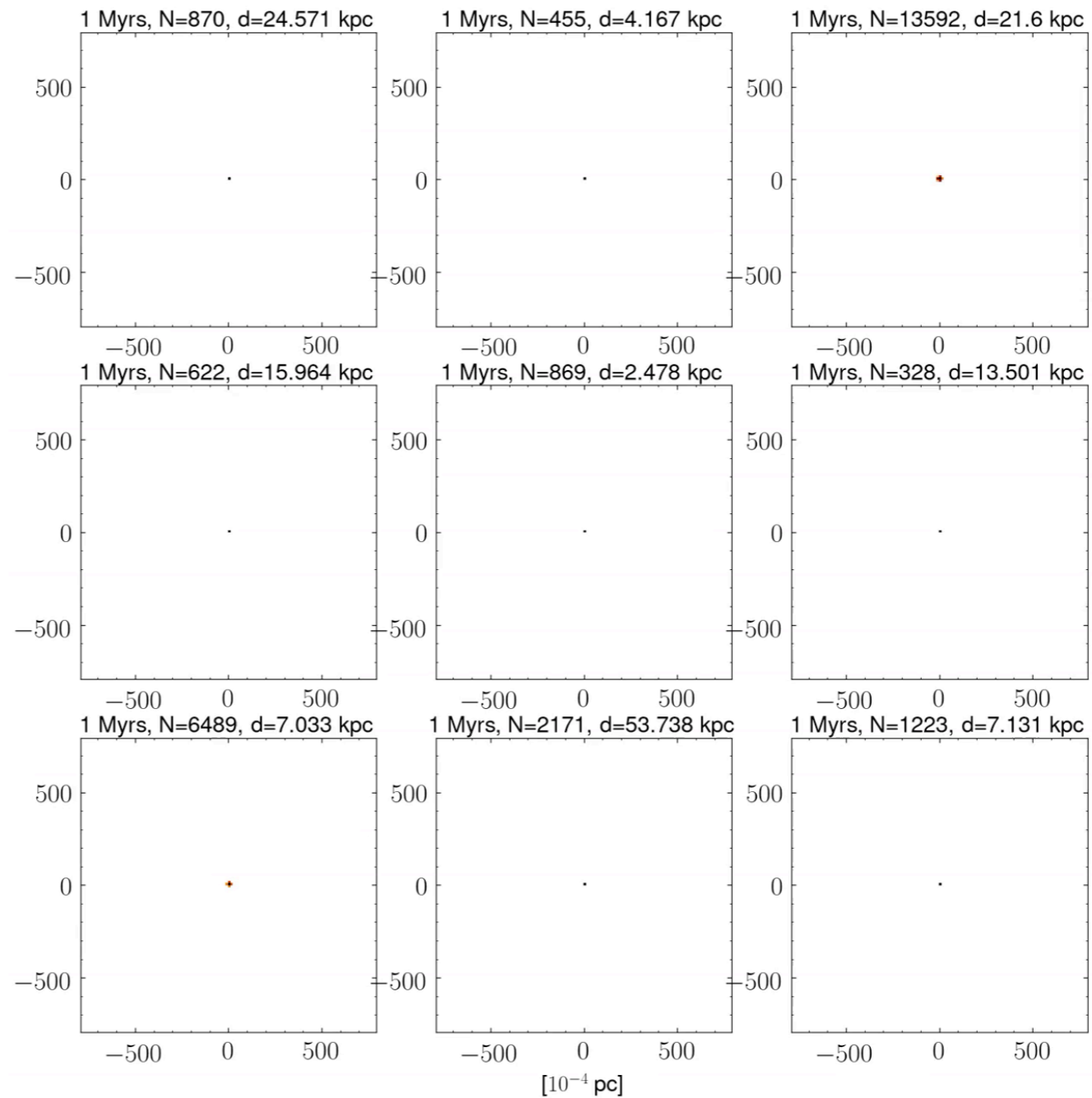
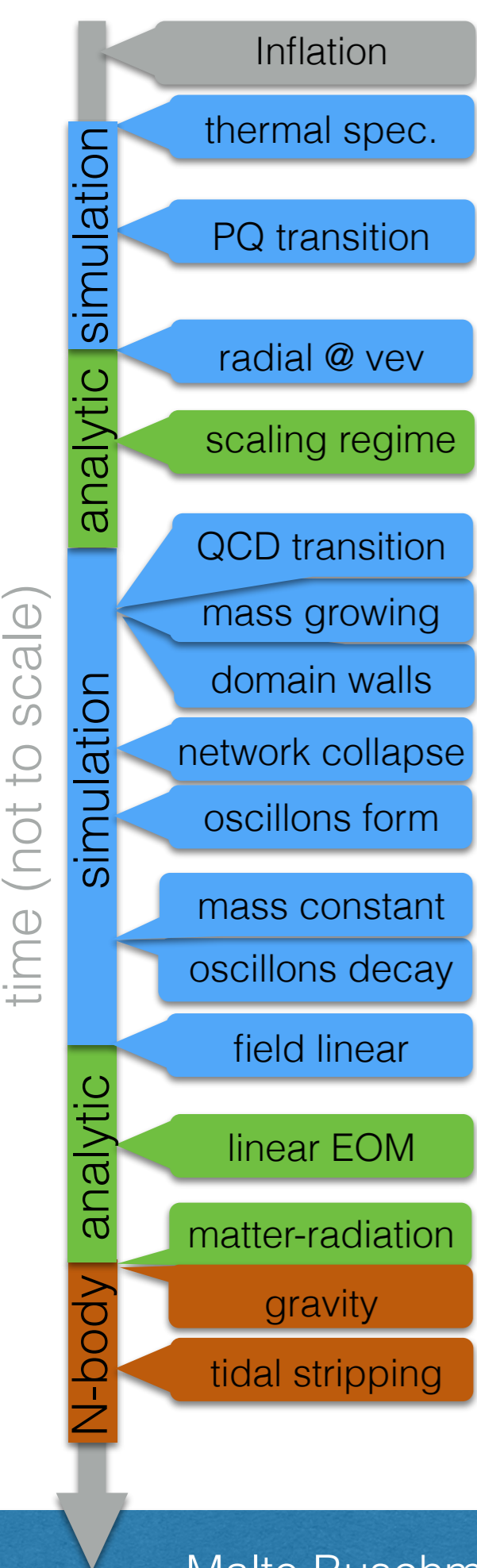
MB, Foster, Safdi, Wentzel (work in progress!)

# Halos are tidally disrupted in Milky Way potential



MB, Foster, Safdi, Wentzel (work in progress!)

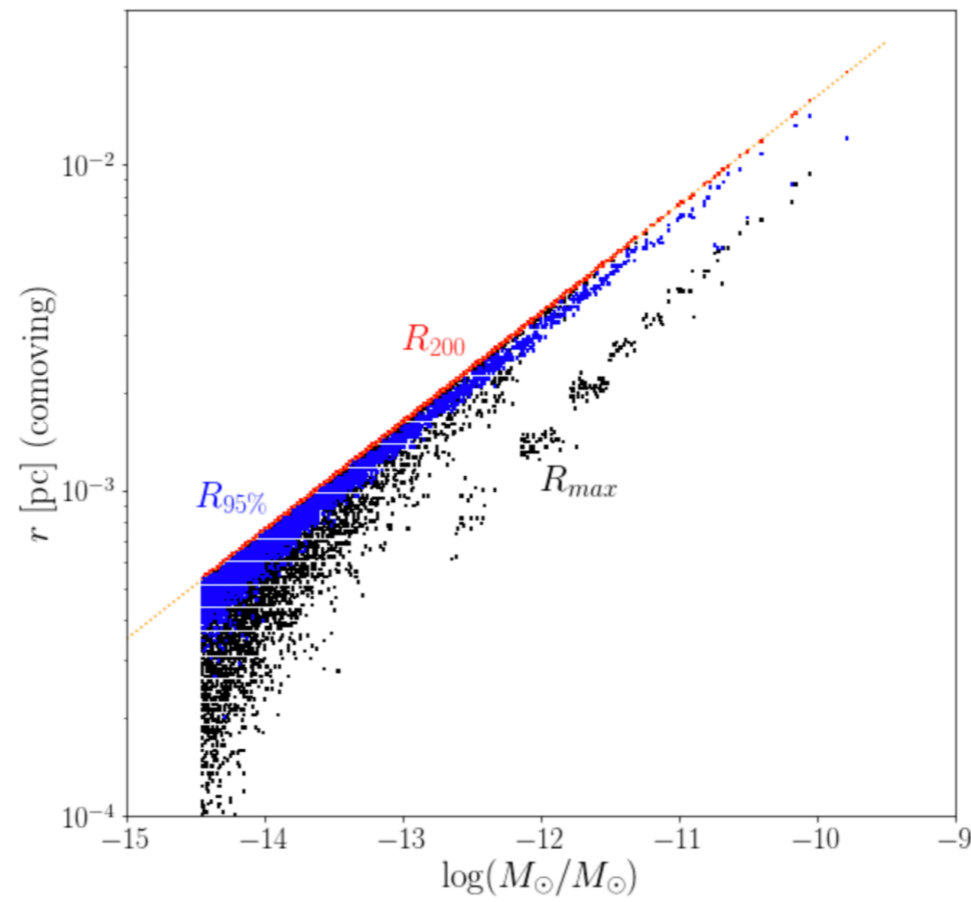
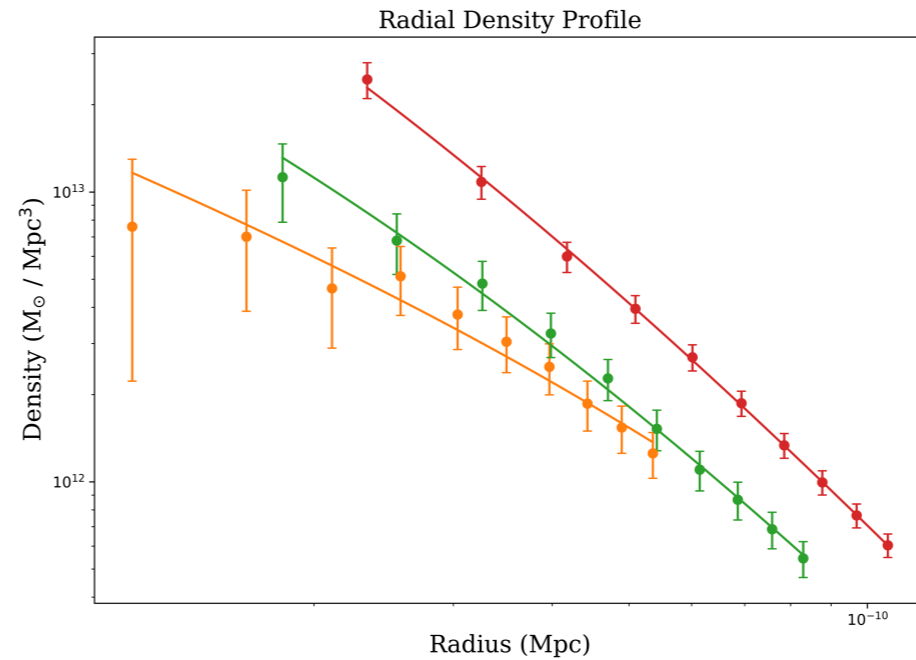
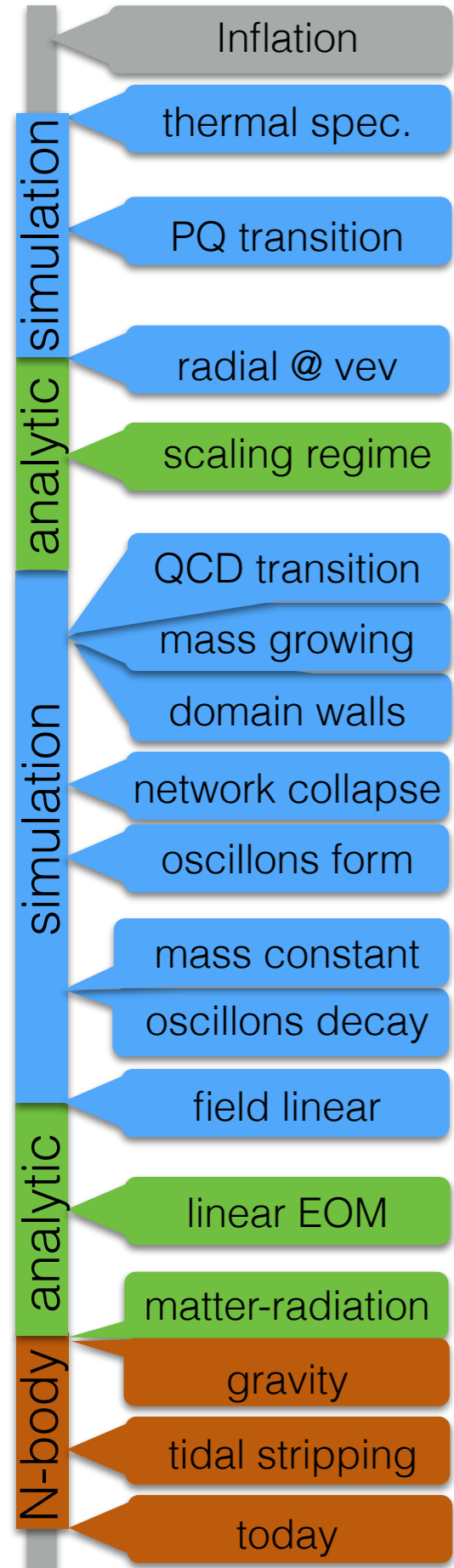
# Halos are tidally disrupted in Milky Way potential



MB, Foster, Safdi, Wentzel (work in progress!)

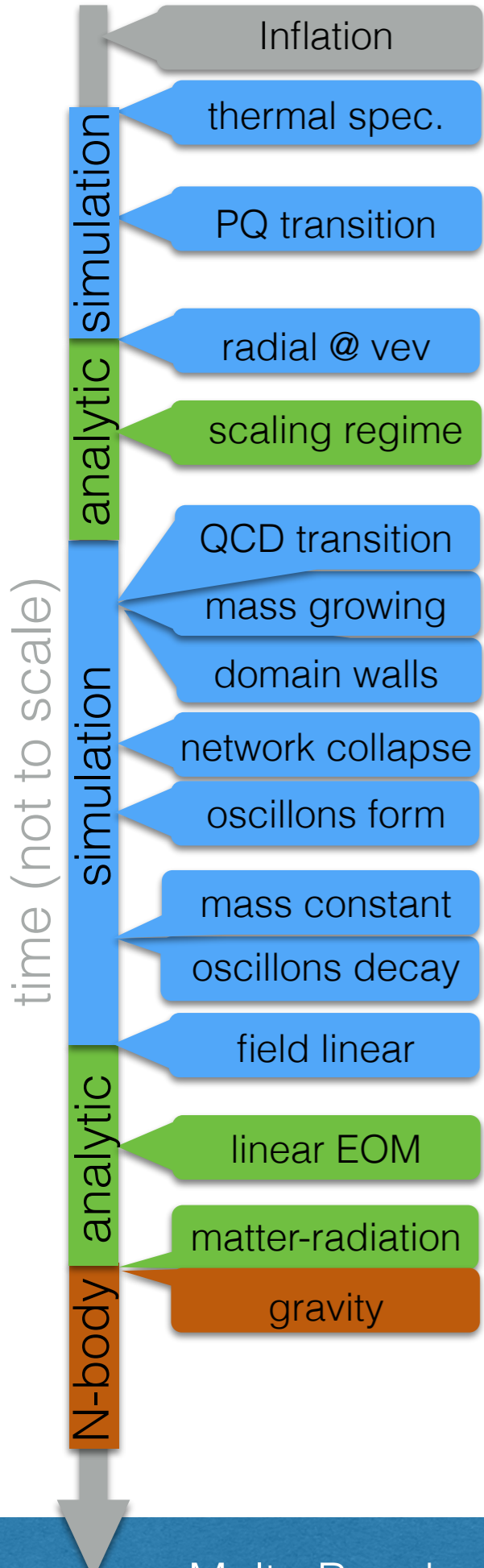
# Characterizing radial profiles and halo mass functions

time (not to scale)



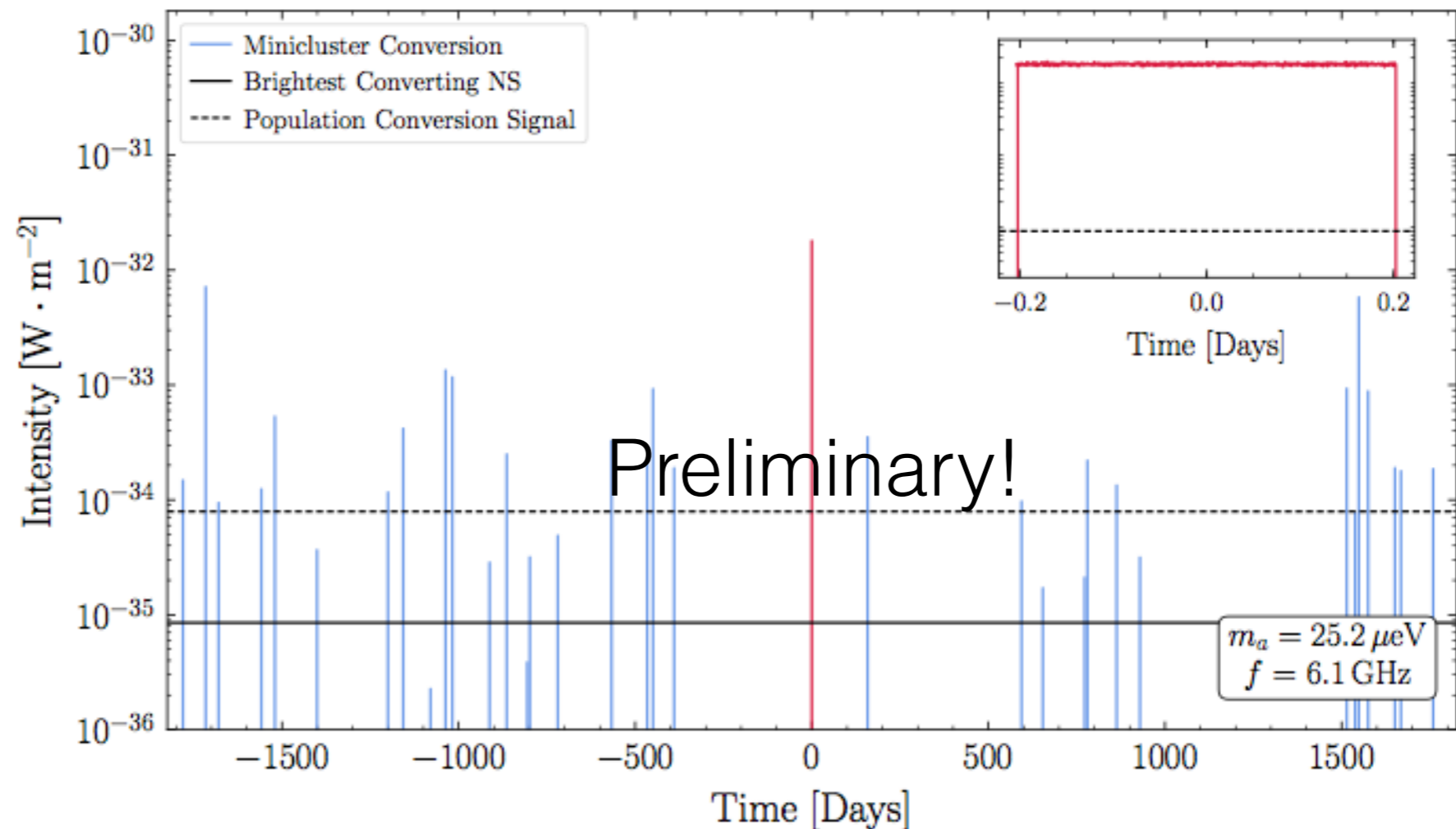
MB, Foster, Safdi, Wentzel (work in progress!)

# Radio signals from Neutron Stars

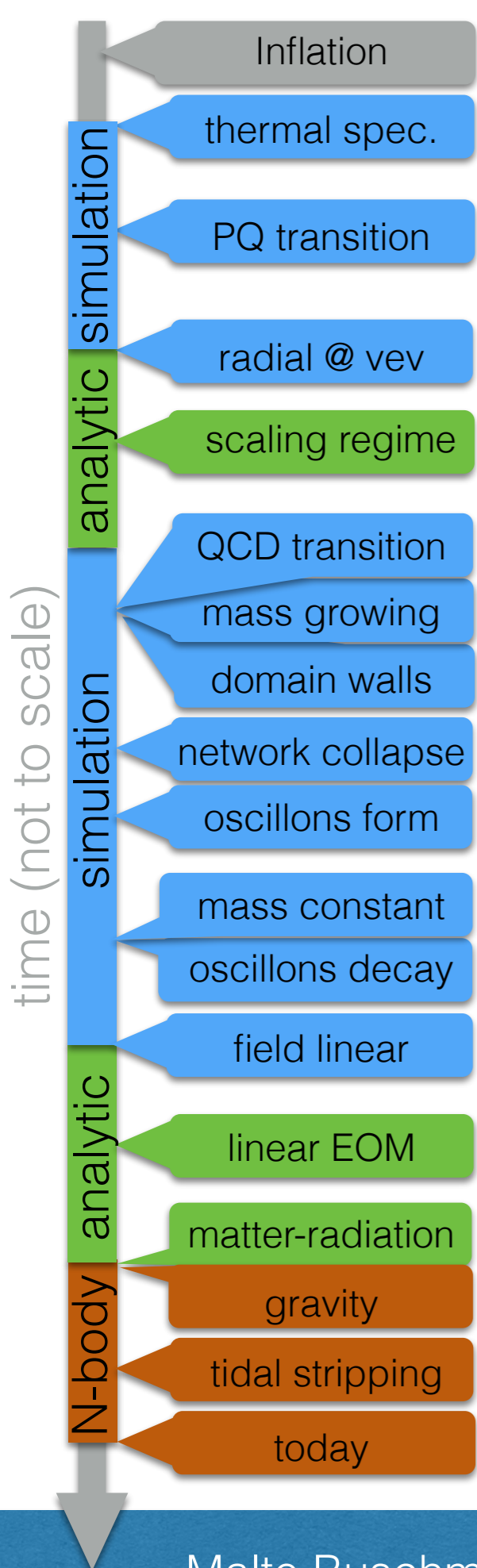


Axions convert to radio photons in magnetic field of neutron star

Large peak in flux when neutron star moves through an axion minihalo!



# Summary



- Assumption: PQ symmetry broken after inflation

- We performed simulations through the PQ and QCD phase transition to matter-radiation equality

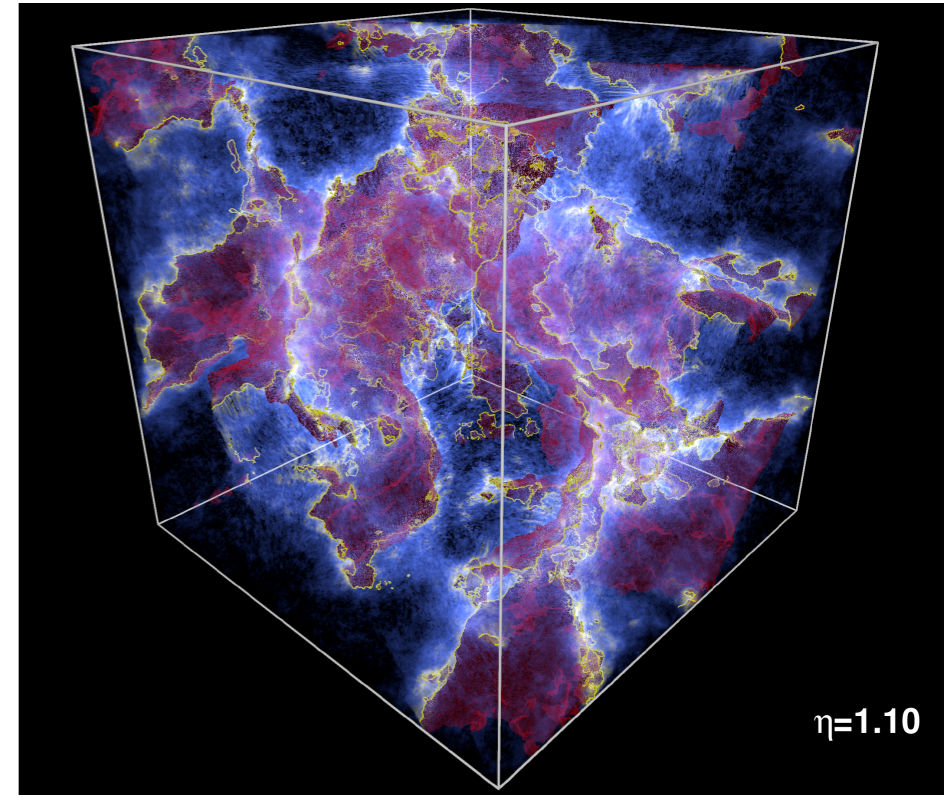
- N-body simulations until Milky Way forms

- Simulated tidal stripping

- Identified minihalo mass spectrum  
Typical mass:  $10^{-10}$  solar masses

- Determined the axion mass that reproduces the correct relic abundance:  $m_a = 25.2 \pm 11.0 \mu\text{eV}$

- We are most likely sitting in a DM void (bad news for e.g ADMX)  
But: We can look for signals of minihalo - NS collision!







Thank you!