

Majorons in the Sky and in the Lab

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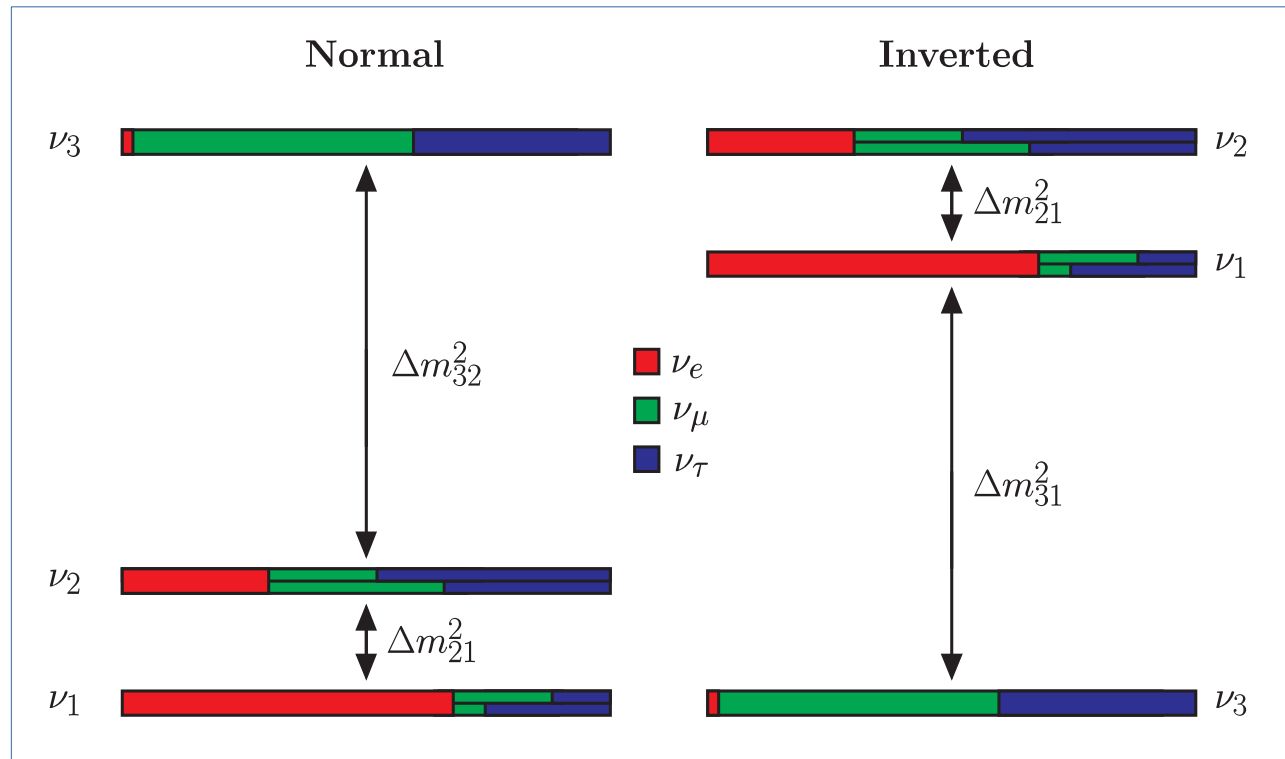
9/17/2020



UNIVERSITY
of
VIRGINIA


Neutrinos have masses and mix

- Mass splittings ✓
- Angles ✓
- Phase(s) ✗
- Ordering ✗
- Mass scale ✗
- Dirac vs. Majorana ✗
- Mass origin ✗




Majoronic seesaw


- SM + 3 singlets N_R + new scalar $\sigma = (f + \sigma^0 + iJ)/\sqrt{2}$.



Lepton number breaking scale



Heavy scalar



Majoron

[Chikashige, Mohapatra, Peccei, '81; Schechter, Valle, '82]

- Break $U(1)_L$ spontaneously:

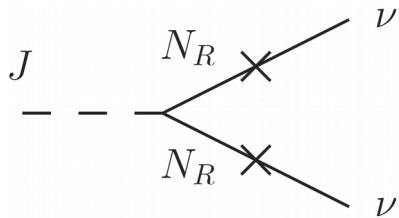
$$\begin{aligned}
 \mathcal{L} &= - \underbrace{\bar{L}yHN_R}_{m_D} - \frac{1}{2} \underbrace{\bar{N}_R^c \kappa \sigma N_R}_{M_R} + \text{h.c.} \\
 m_D &= \frac{y}{\sqrt{2}} v & M_R &= \frac{\kappa f}{\sqrt{2}}
 \end{aligned}
 \quad \longrightarrow \quad
 \begin{pmatrix} 0 & m_D \\ m_D^T & M_R \end{pmatrix}$$

- For $M_R \gg m_D$: $M_\nu \simeq -m_D M_R^{-1} m_D^T$

$$\simeq 1\text{eV} \left(\frac{m_D}{100\text{GeV}} \right)^2 \left(\frac{10^{13}\text{GeV}}{M_R} \right).$$

Majoron couplings

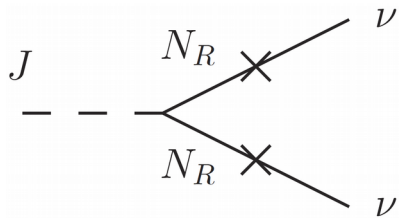
- Tree-level coupling only to neutrinos:



$$\frac{iJ}{2f} \bar{\nu}_\alpha^c \gamma_5 (m_D M_R^{-1} m_D^T)^*_{\alpha\beta} \nu_\beta = -\frac{iJ}{2f} \sum_k \bar{\nu}_k \gamma_5 m_k \nu_k$$

Majoron couplings

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- Assume *Pseudo*-Goldstone Majoron: $m_j \neq 0$.

[Rothstein, Babu, Seckel, '93]

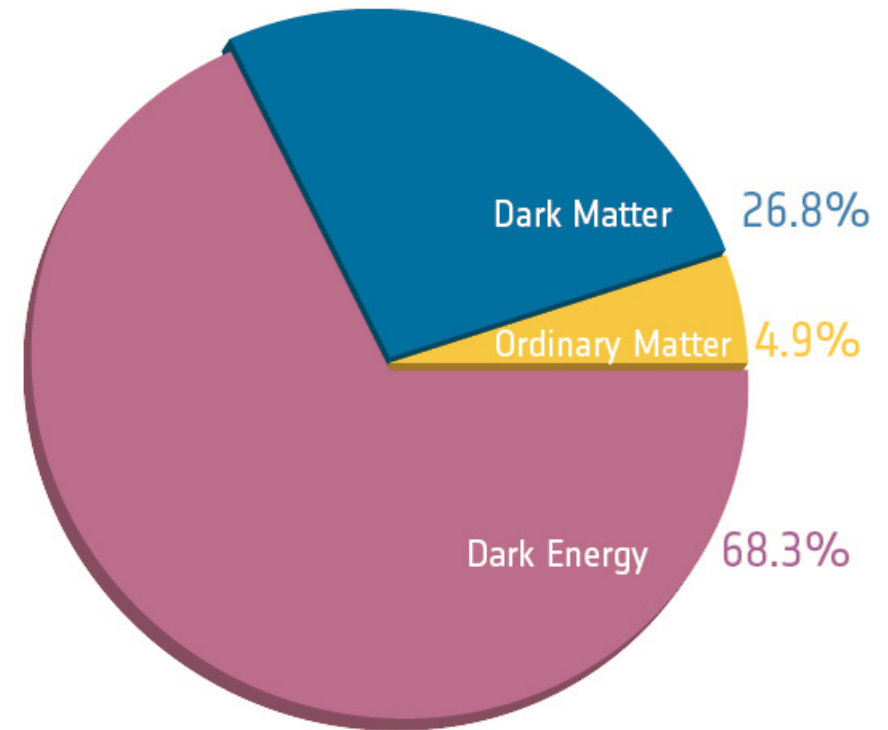
- Long lifetime \rightarrow Dark matter!

[Berezinsky, Valle '93; Lattanzi, Valle '07; Bazzocchi et al, '08; Queiroz, Sinha, '14]

$$\tau(J \rightarrow \nu\nu) \simeq \tau_{\text{Universe}} \left(\frac{\text{MeV}}{m_j} \right) \left(\frac{f}{10^8 \text{GeV}} \right)^2 \left(\frac{10^{-3} \text{eV}^2}{\sum_k m_k^2} \right)$$

Dark matter abundance

- Freeze out via $\lambda JJ\bar{H}H$:
 - $m_J \sim m_h/2$,
 - $m_J > 400$ GeV.



Dark matter abundance

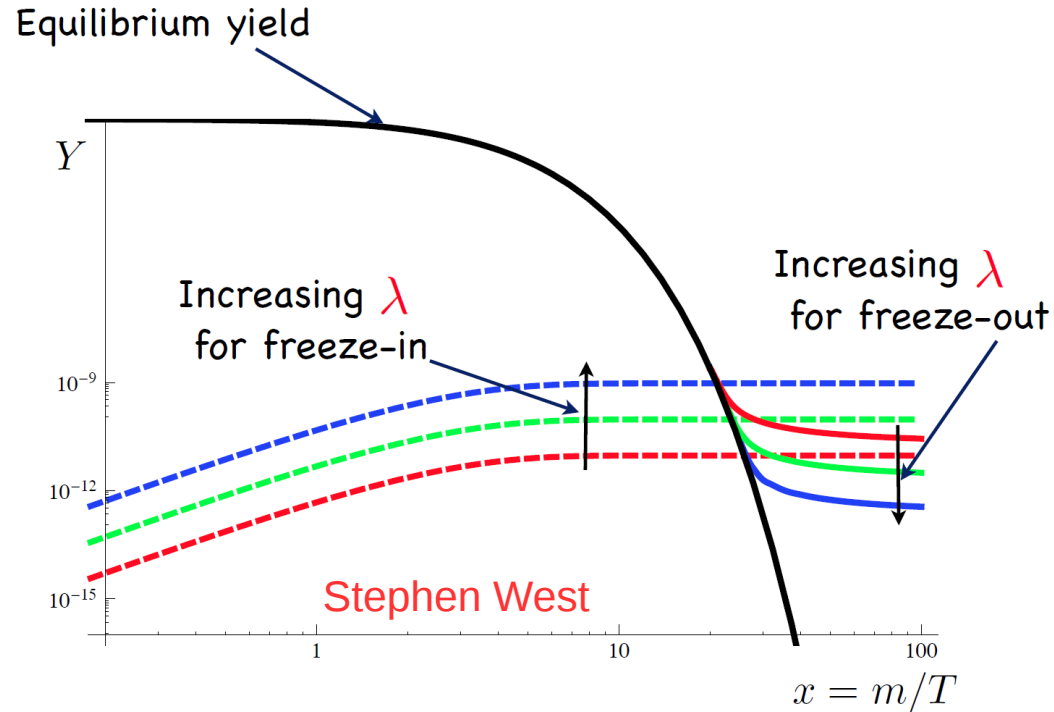
- **Freeze out** via $\lambda JJ\bar{H}\bar{H}$:
 - $m_J \sim m_h/2$,
 - $m_J > 400 \text{ GeV}$.

- **Freeze in:**

$$\Omega_J \propto m_J \Gamma(h \rightarrow JJ)$$

$$\Rightarrow m_J \simeq \left(\frac{10^{-10}}{\lambda} \right)^2 \text{ MeV.}$$

[McDonald, '02; Hall, Jedamzik, March-Russell, West '10; Frigerio, Hambye, Masso, '11]



Lyman- α excludes $m_J < 12 \text{ keV}$!
 Use different mechanism:
JH, Teresi, 1706.09909, 1709.07283.

Indirect detection

$$\tau(J \rightarrow \nu\nu) \simeq \tau_{\text{Universe}} \left(\frac{\text{MeV}}{m_J} \right) \left(\frac{f}{10^8 \text{GeV}} \right)^2 \left(\frac{10^{-3} \text{eV}^2}{\sum_k m_k^2} \right)$$

- General limit from DM \rightarrow invisible: $\tau \gtrsim 10 \times \tau_{\text{Universe}}$.

[Audren, Lesgourgues, Mangano, Serpico, Tram, '14]

- Can we observe the **neutrino lines**?

- $m_J > 10 \text{ TeV}$: **No**. Dominant decay is $J \rightarrow \nu\nu h(h)$.

- ▶ no line! [Dudas, Mambrini, Olive, '15]

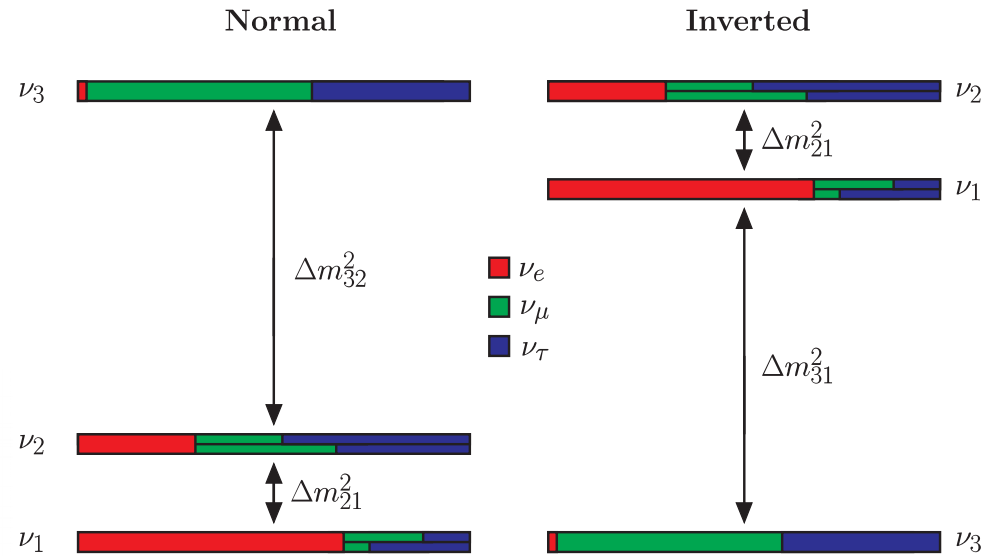
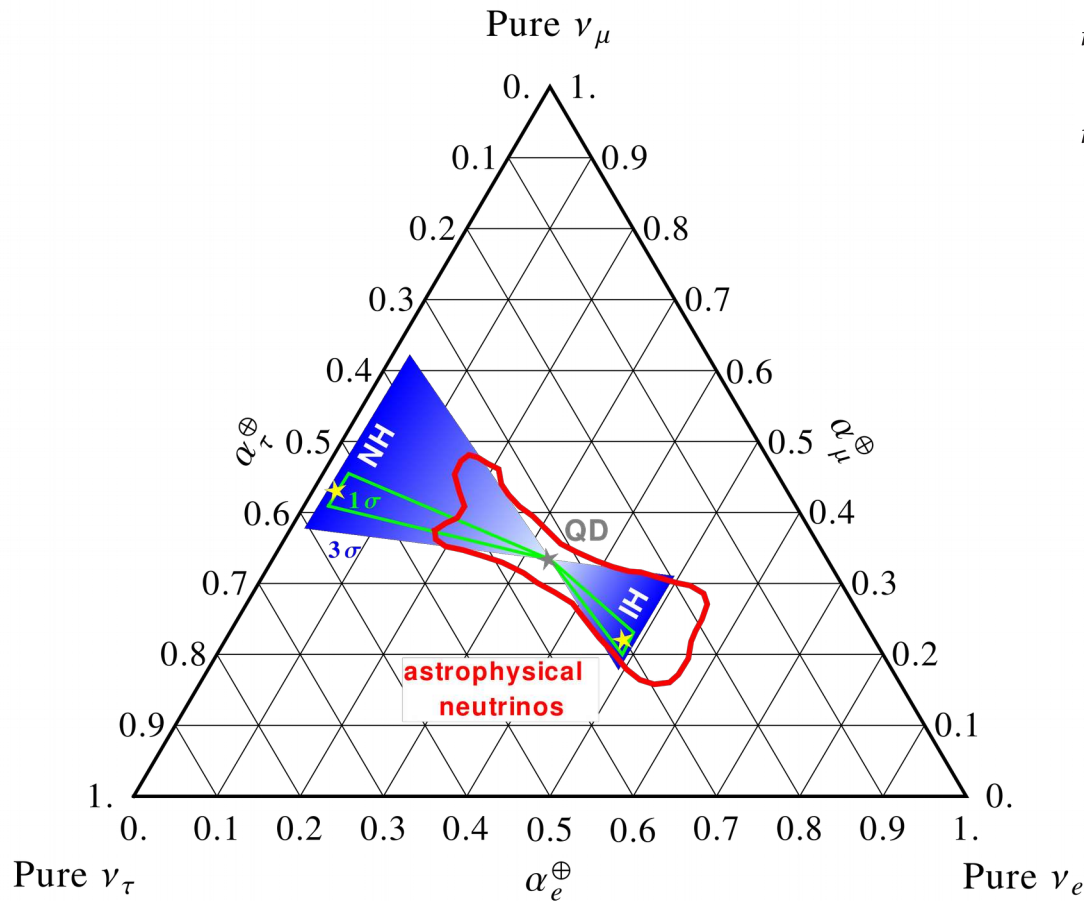
- Also want to avoid electroweak Bremsstrahlung.

[Kachelriess, Serpico, '07; Bell, Dent, Jacques, Weiler, '08; Queiroz, Yaguna, Weniger, '16]

- For $\text{MeV} < m_J < 100 \text{ GeV}$: **Yes!**

Flavor of J $\rightarrow \nu_k \nu_k$

Mass eigenstates \rightarrow no oscillations!



Flavor ratios:

$$\alpha_e : \alpha_\mu : \alpha_\tau$$

$$\text{NH} : 0.03 : 0.43 : 0.54 ,$$

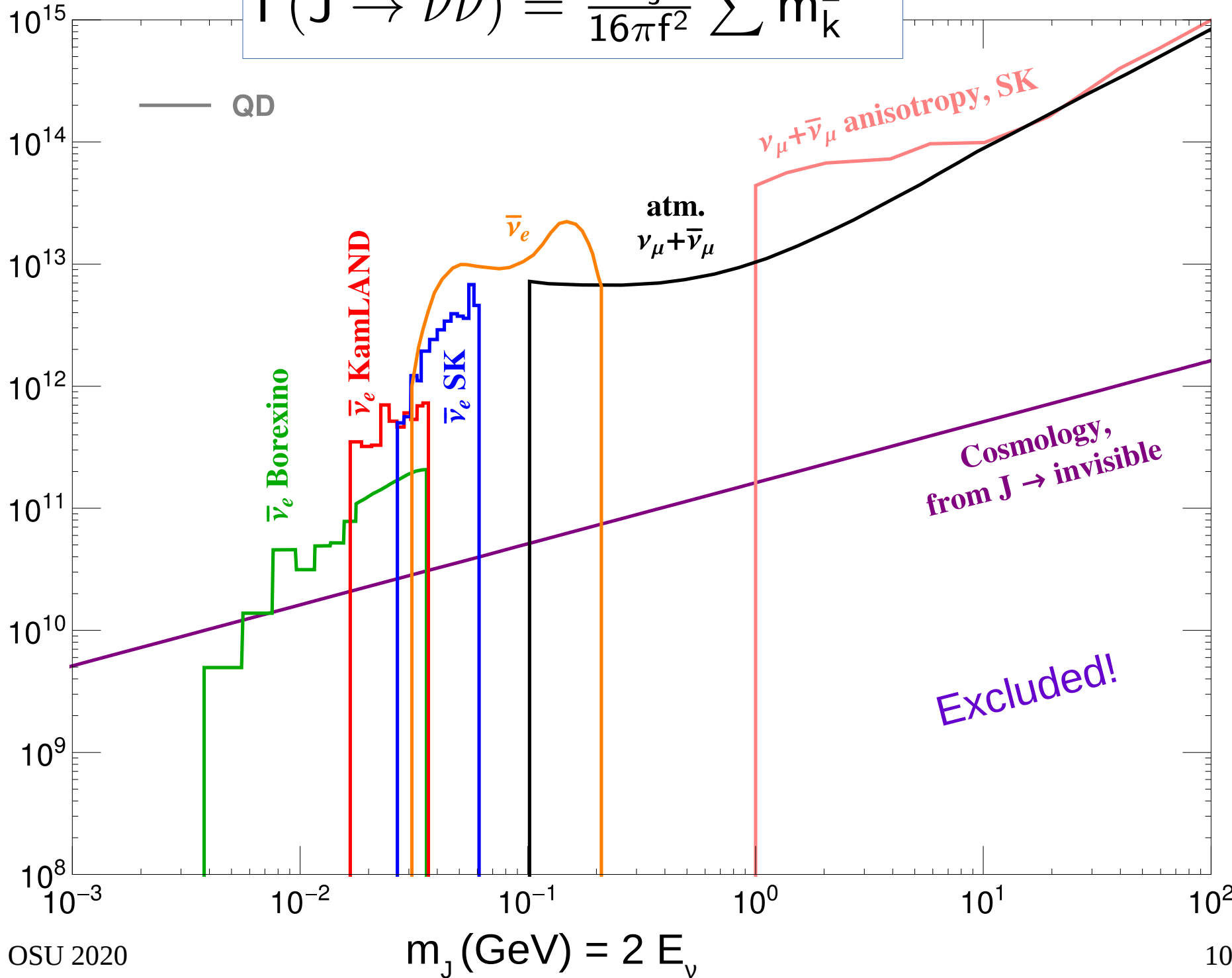
$$\text{IH} : 0.48 : 0.22 : 0.30 ,$$

$$\text{QD} : 0.33 : 0.33 : 0.33 .$$

[JH, Garcia-Cely, 1701.07209, JHEP '17]

$$\Gamma(J \rightarrow \nu\nu) = \frac{m_J}{16\pi f^2} \sum m_k^2$$

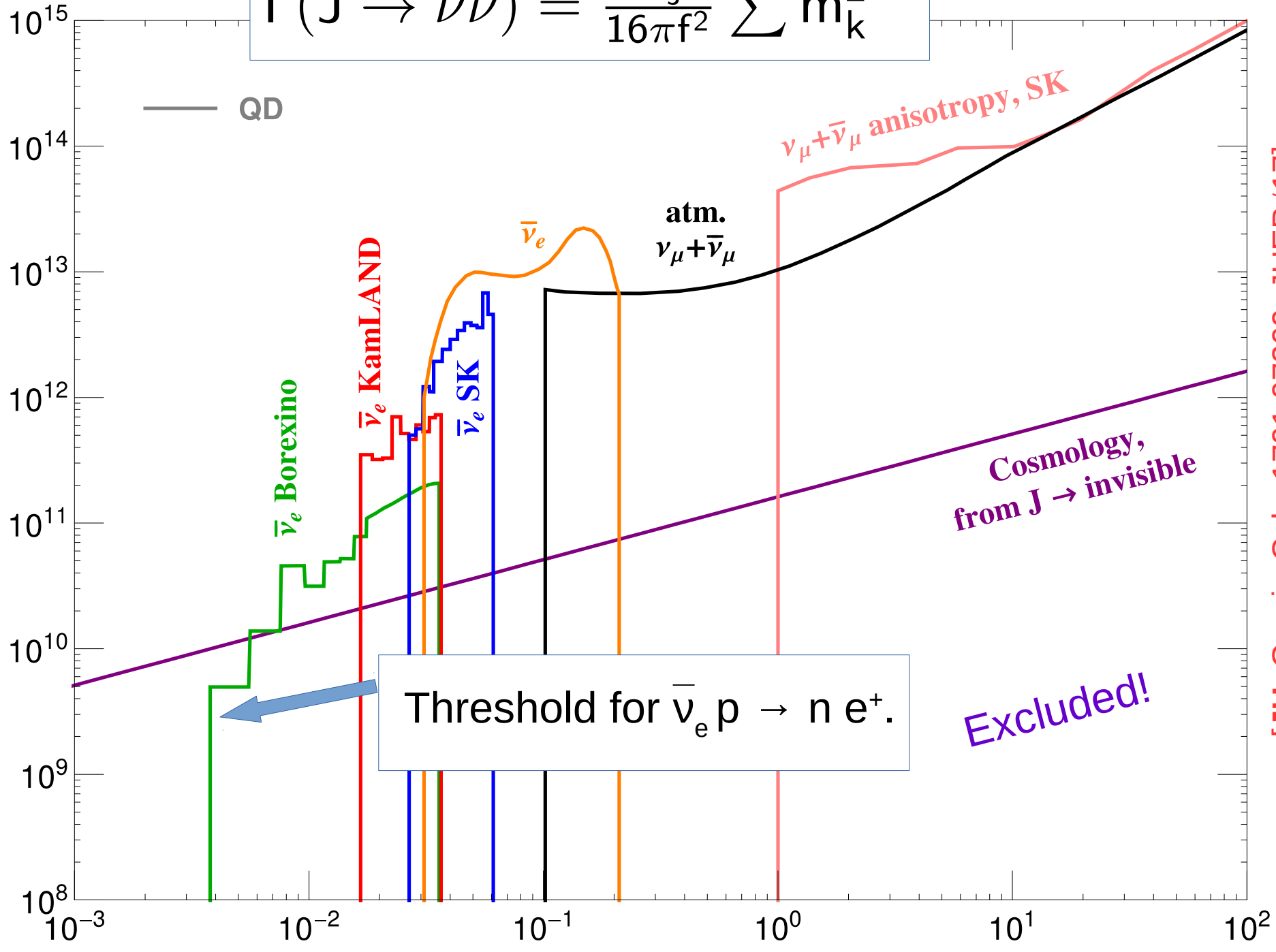
Lower limit on breaking scale f (GeV)



[JH, Garcia-Cely, 1701.07209, JHEP '17]

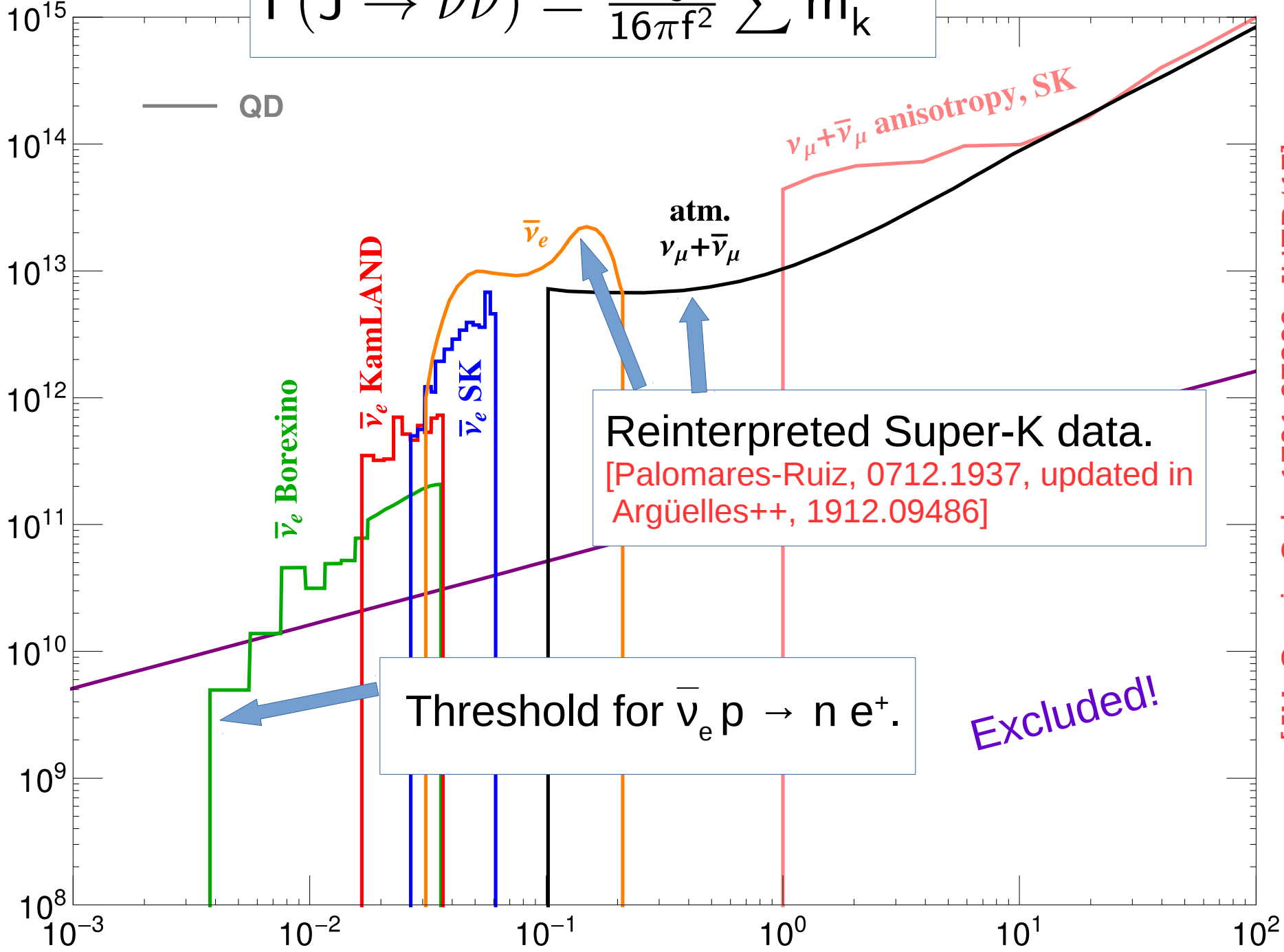
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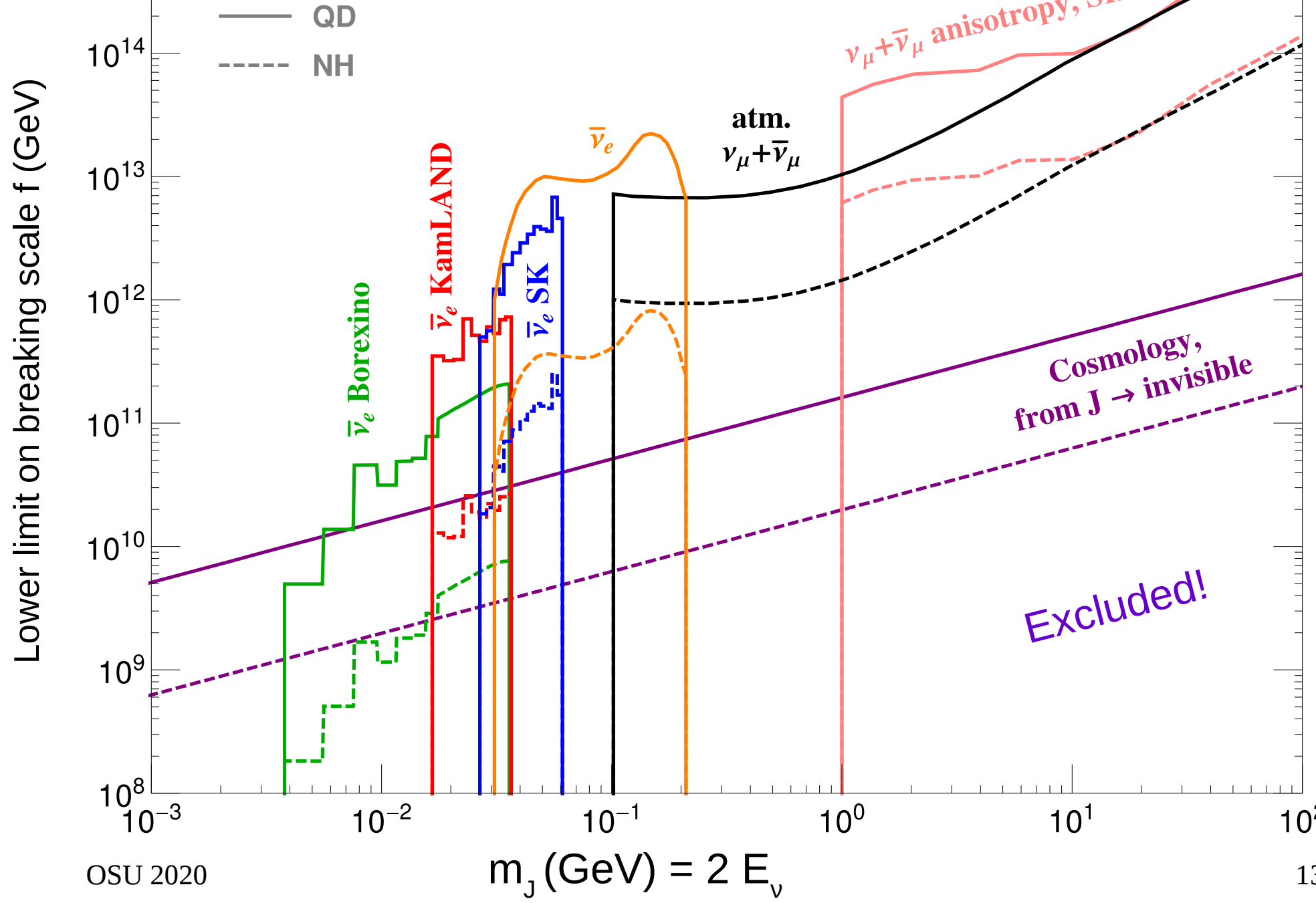


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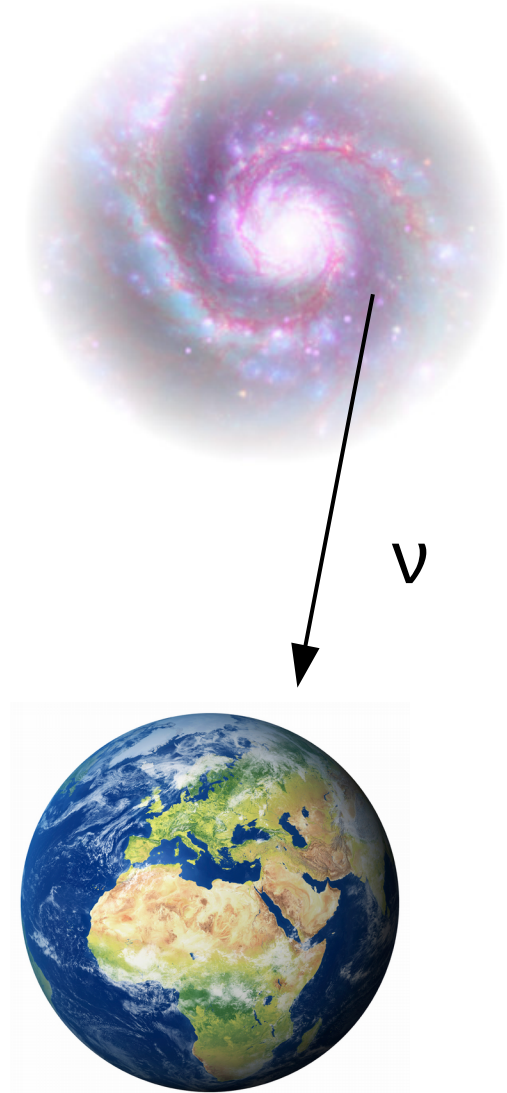


[JH, Garcia-Cely, 1701.07209, JHEP '17]

Look for neutrinos from light DM!

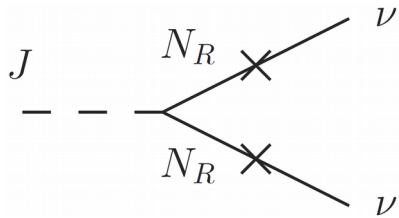
- ν lines detectable down to **MeV**.
- For free in searches for diffuse supernova neutrino background.
- Borexino = indirect DM detector!
- Darwin, Hyper-K, JUNO, ... = indirect DM detectors.
- DM $\rightarrow \nu$ easily dominant channel, no SU(2) argument as for multi-TeV DM.

[El Aisati, Garcia-Cely, Hambye, Vanderheyden, 1706.06600]



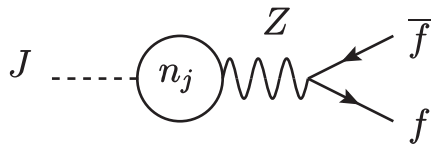
Majoron couplings

- Tree-level coupling only to neutrinos:

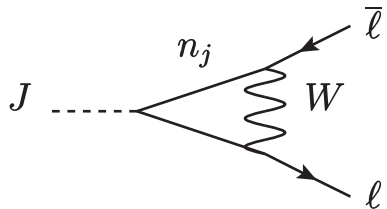


$$\frac{iJ}{2f} \bar{\nu}_\alpha^c \gamma_5 (m_D M_R^{-1} m_D^T)_{\alpha\beta}^* \nu_\beta = -\frac{iJ}{2f} \sum_k \bar{\nu}_k \gamma_5 m_k \nu_k$$

- One loop:



$$\frac{iJ}{f} \bar{f} \gamma_5 f \frac{m_f T_3^f}{8\pi^2 v^2} \text{tr} \left(m_D m_D^\dagger \right)$$

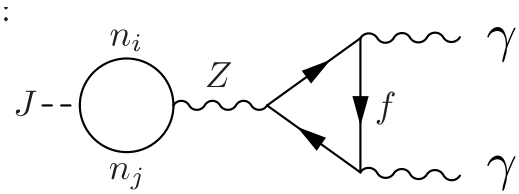


$$\frac{iJ}{f} \bar{l}_\alpha \left(\frac{m_\beta}{8\pi^2 v^2} P_R - \frac{m_\alpha}{8\pi^2 v^2} P_L \right) l_\beta \left(m_D m_D^\dagger \right)_{\alpha\beta}$$

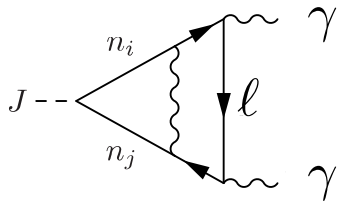


Off-diagonal!

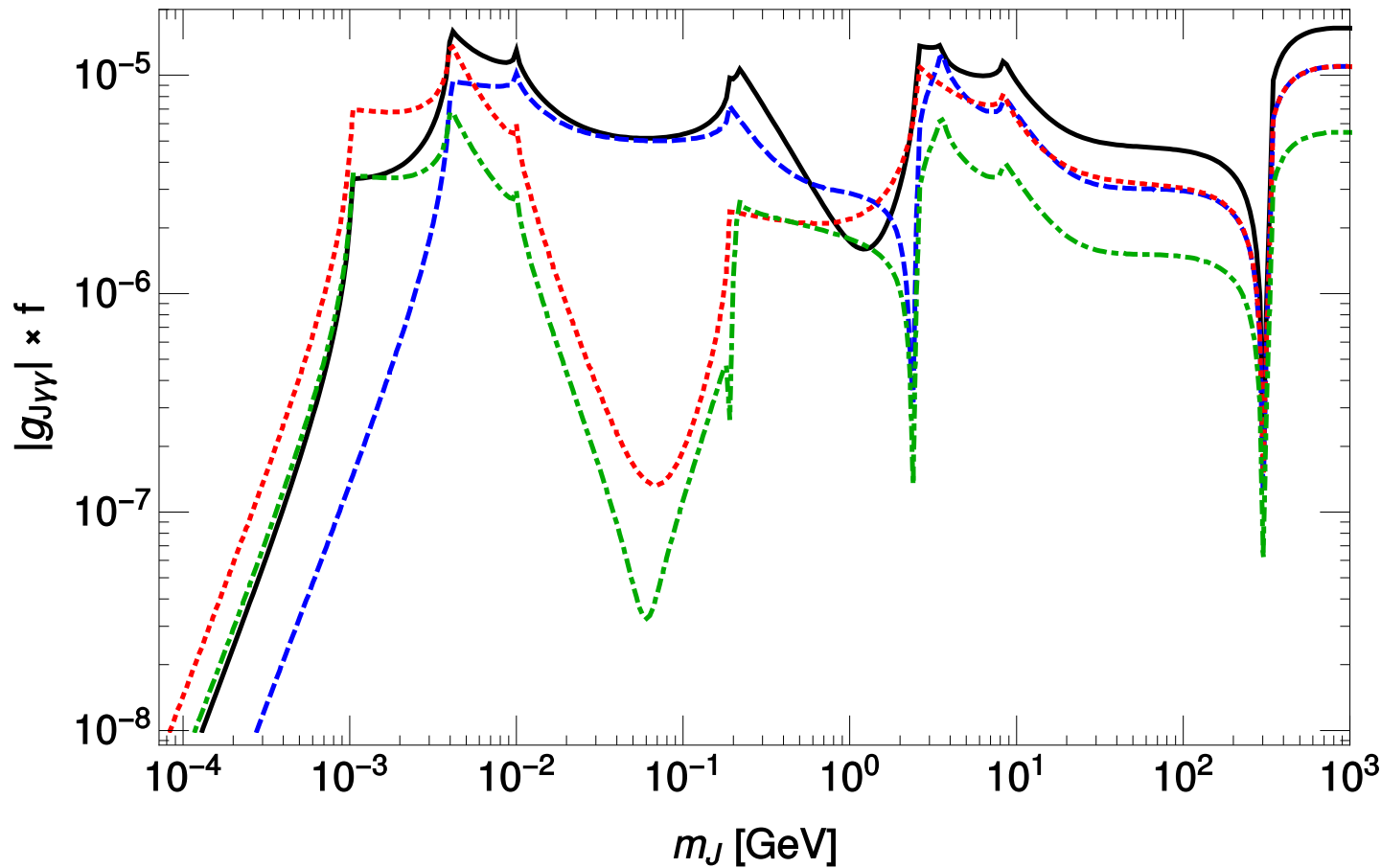
[JH, Garcia-Cely, JHEP '17; see also Pilaftsis '94]



$$= \frac{\alpha}{8\pi^3 v^2 f} \text{tr}(m_D m_D^\dagger) \sum_f N_c^f Q_f^2 T_3^f h\left(\frac{m_J^2}{4m_f^2}\right)$$



$$= \frac{\alpha}{8\pi^3 v^2 f} \sum_\ell (m_D m_D^\dagger)_{\ell\ell} h\left(\frac{m_J^2}{4m_\ell^2}\right)$$



- $(m_D m_D^\dagger)_{ij} = (100 \text{ GeV})^2$
- - - $(m_D m_D^\dagger)_{\tau\tau} = 0$
- ⋯ $(m_D m_D^\dagger)_{ee} = 0$
- · - $(m_D m_D^\dagger)_{ee} = (m_D m_D^\dagger)_{\tau\tau} = 0$

[JH, Patel, PRD '19]

Loop induced $J \rightarrow \gamma\gamma, \bar{q}q, \bar{\ell}\ell'$

- Tree-level J couplings $\propto M_\nu$ while loop level $\propto m_D m_D^\dagger$.
- One-to-one mapping: $\{m_D, M_R\} \leftrightarrow \{M_\nu, m_D m_D^\dagger\}$.

[Davidson, Ibarra, hep-ph/0104076]

- Loop couplings contain unknown seesaw parameters!

$J \rightarrow \gamma\gamma, \bar{q}q, \bar{\ell}\ell'$ are *complementary* to $\nu\nu$ channel!

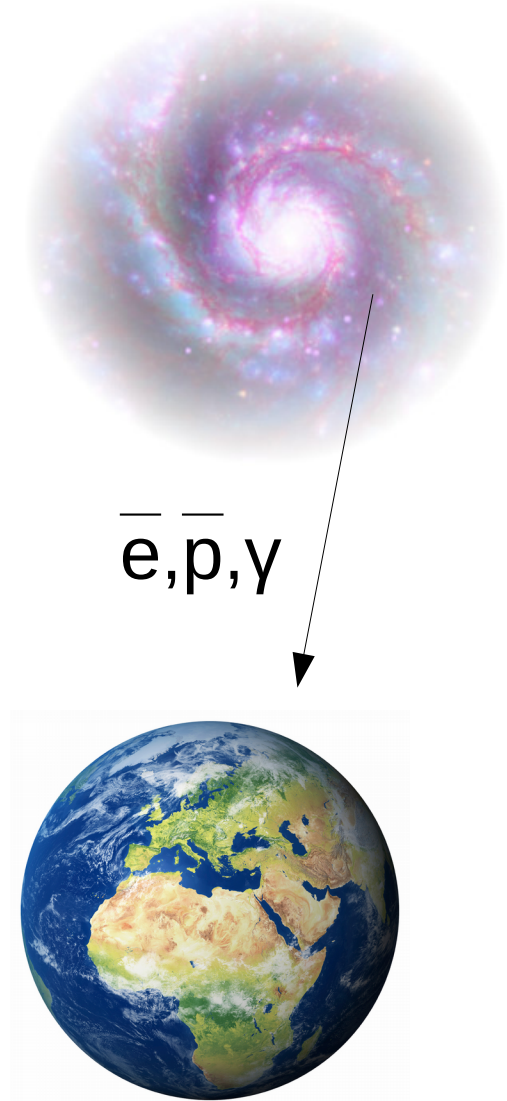
- One generation: $K \equiv \frac{m_D m_D^\dagger}{v f} \sim \frac{m_\nu M_R}{v f} \sim 10^{-13} M_R / f$.

[Chikashige, Mohapatra, Peccei, '81; Pilaftsis '94]

Indirect detection II

$$\Gamma(J \rightarrow \bar{f}f) \propto m_f^2 \mathcal{O}(K^2)$$

- DM \rightarrow $\tau\tau$, bb , tt , ... give
 - continuous γ spectrum:
Integral, Fermi-LAT.
 - anti-protons and positrons:
PAMELA, AMS-02.
- DM decay around $z \sim 1000$:
 - modification of CMB.
[Slatyer, Wu, 1610.06933]
 - independent of DM profile.
- DM $\rightarrow \gamma\gamma$ gives lines.



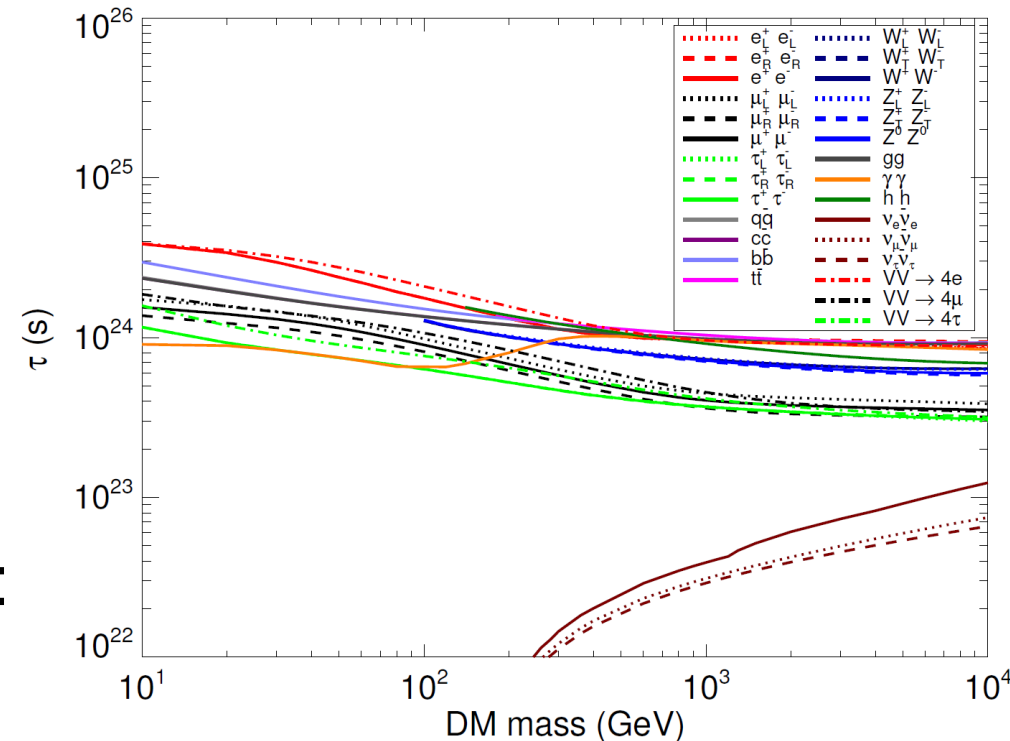
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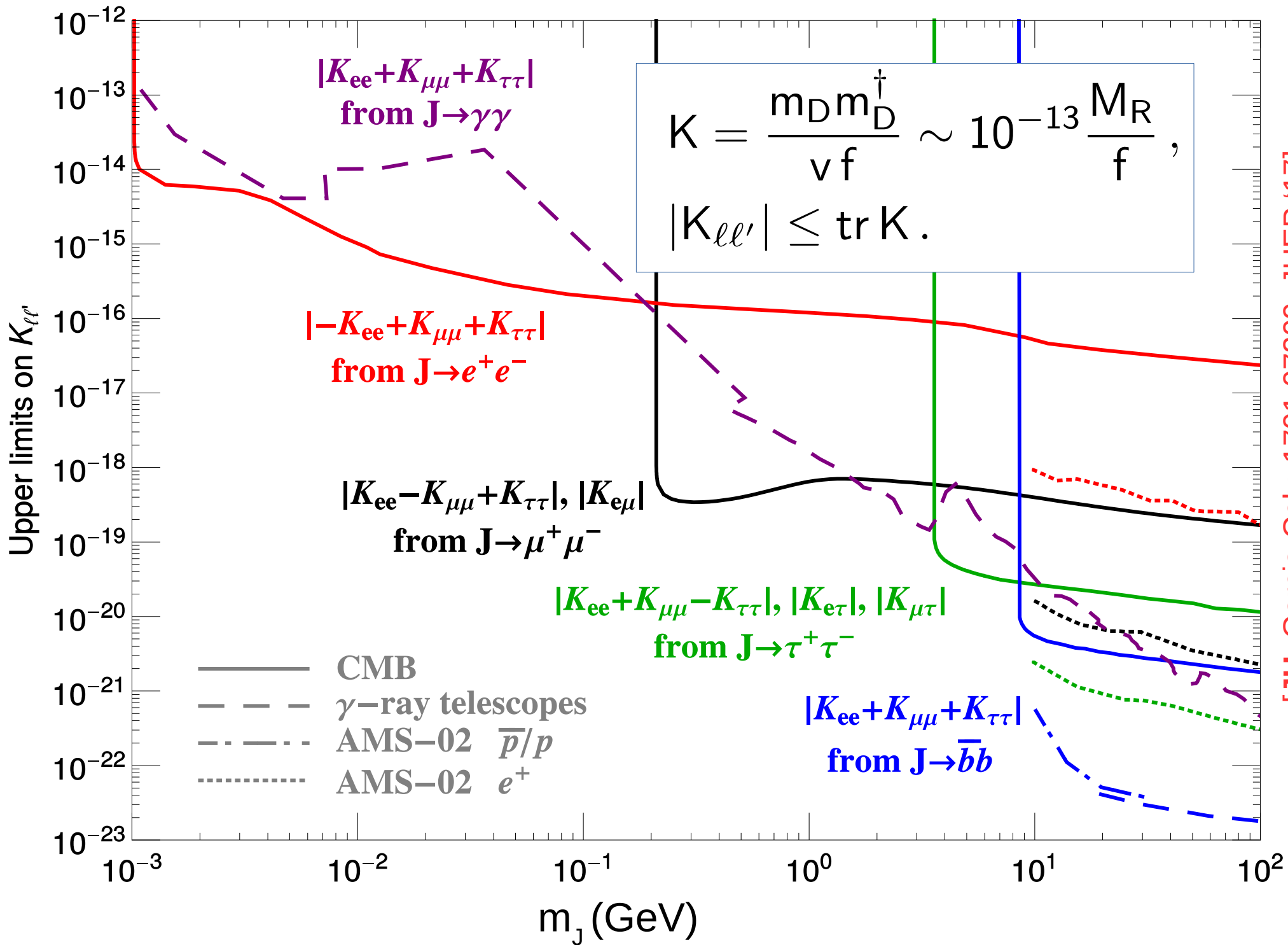
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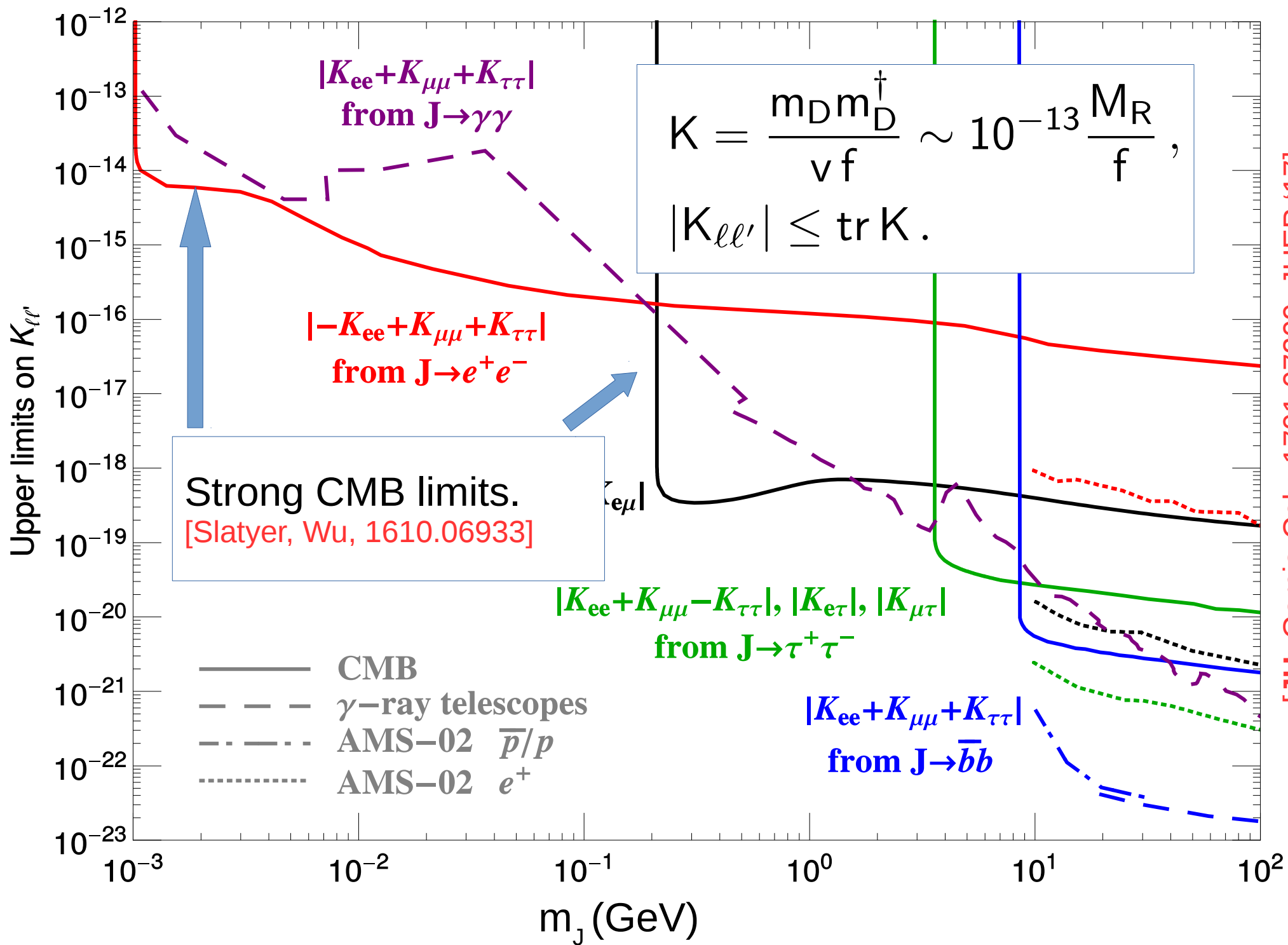
- DM $\rightarrow \tau\tau, bb, tt, \dots$ give
 - continuous γ spectrum: Integral, Fermi-LAT.
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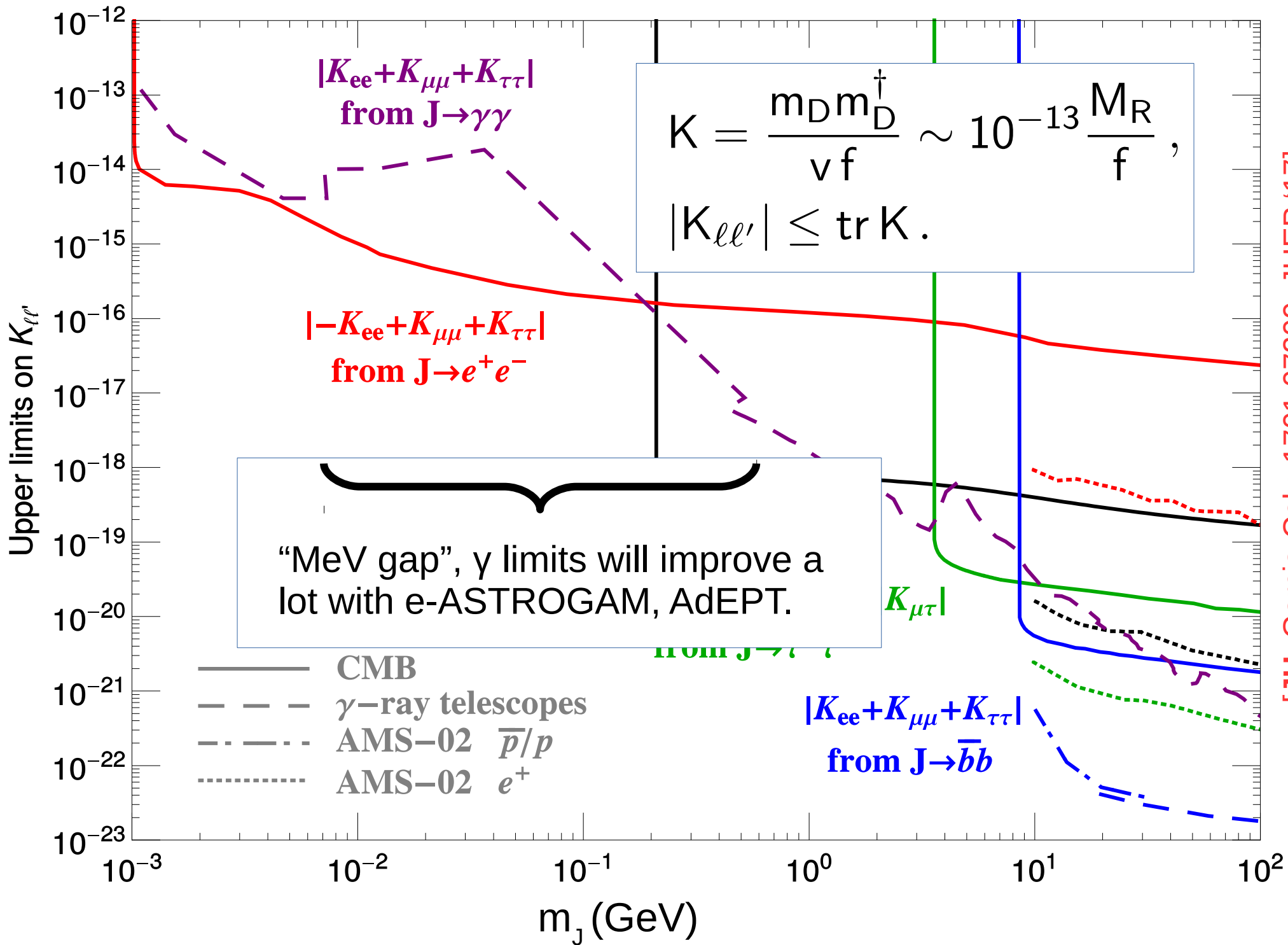
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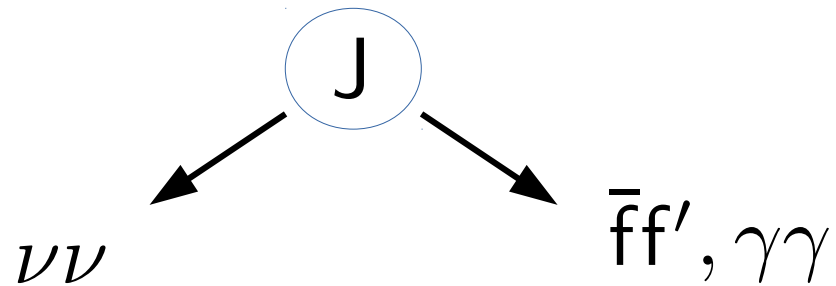






Is it possible to detect dark matter via **neutrinos** and **not** gamma-rays or anti-matter?

Yes!



depends on

$$M_\nu \simeq -m_D M_R^{-1} m_D^T.$$

depends on

$$m_D m_D^\dagger.$$

Independent / Complementary!

Majoron = DM

- Naturally light, long-lived DM candidate.
- Indirect detection possible:
 - $\text{MeV} < m_j$: $J \rightarrow \nu\nu, \gamma\gamma, \bar{f}f$.
 - $\text{keV} < m_j < \text{MeV}$: $J \rightarrow \gamma\gamma$. Maybe warm DM.

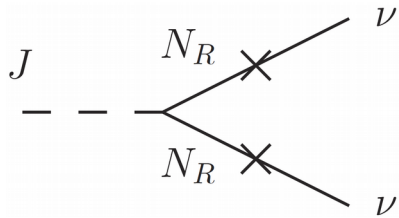
[JH, Teresi, 1706.09909, 1709.07283]

Majoron \neq DM

- Increase couplings to produce J in lab.
- Measure seesaw parameters.

Majoron couplings

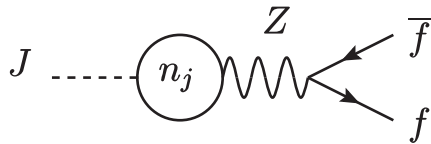
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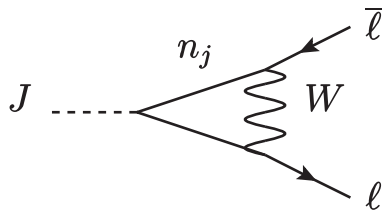
$$\frac{iJ}{2f} \bar{\nu}_\alpha^c \gamma_5 (m_D M_R^{-1} m_D^T)_{\alpha\beta}^* \nu_\beta = - \underbrace{\frac{iJ}{2f} \sum_k \bar{\nu}_k \gamma_5 m_k \nu_k}_{}$$

Too small for lab

- One loop:



$$\frac{iJ}{f} \bar{f} \gamma_5 f \frac{m_f T_3^f}{8\pi^2 v^2} \text{tr} \left(m_D m_D^\dagger \right)$$



$$\frac{iJ}{f} \bar{l}_\alpha \left(\frac{m_\beta}{8\pi^2 v^2} P_R - \frac{m_\alpha}{8\pi^2 v^2} P_L \right) l_\beta \left(m_D m_D^\dagger \right)_{\alpha\beta}$$



Off-diagonal!

[JH, Garcia-Cely, JHEP '17; see also Pilaftsis '94]

Properties

- Crucial observation: the two matrices are independent!

$$\{m_D, M_R\} \leftrightarrow \{M_\nu = -m_D M_R^{-1} m_D^T, m_D m_D^\dagger\}.$$

[Davidson, Ibarra, JHEP '01]

- $J\bar{\ell}\ell'$ coupling can be *large* and of **arbitrary structure**.
- Similar couplings arise for familons or flavor Z'.

[Wilczek, '82; Reiss, '82; Grinstein, Preskill, Wise, 85; ...]

- Experimental signature depends on J decay channel:

$$\ell \rightarrow \ell' J, \quad J \rightarrow \text{inv}, \underbrace{\ell'' \ell''', \gamma\gamma, \dots}$$

[JH, Rodejohann, PLB '18;
Bauer et al., PRL '20;
Cornella et al., JHEP '20]

[$\mu \rightarrow e J, J \rightarrow \gamma\gamma$:
MEG, 2005.00339]

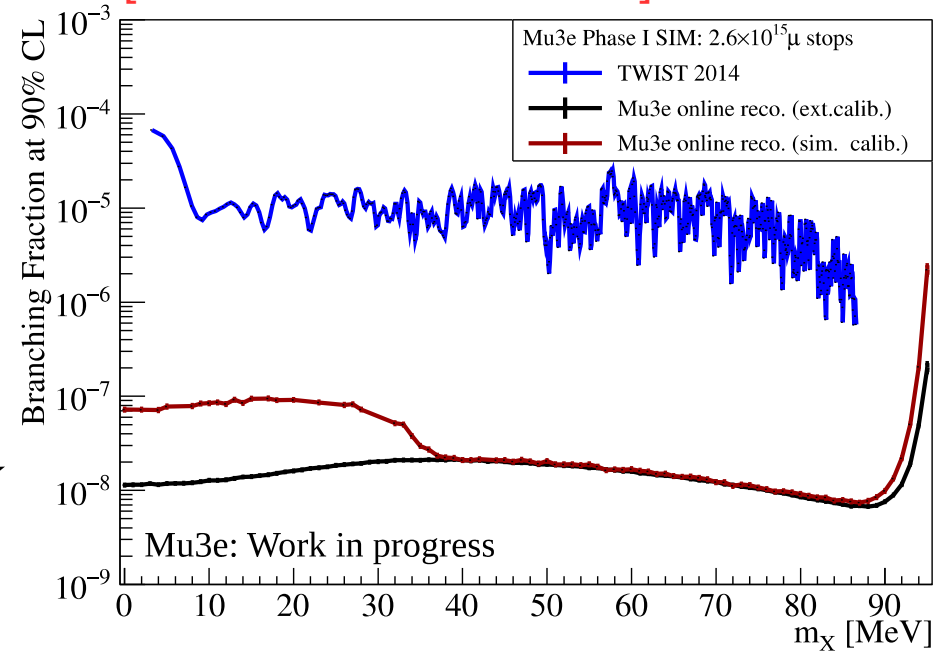
$\mu \rightarrow e J$

- Electron *line* on top of Michel spectrum.
- Good prospects @ Mu3e.
- In progress: signal in $\mu \rightarrow e$ conversion exps. COMET, Mu2e(-II).
 - Many muons!
 - Nuclear recoil: E_e up to m_μ .
 - Suppression of tail...

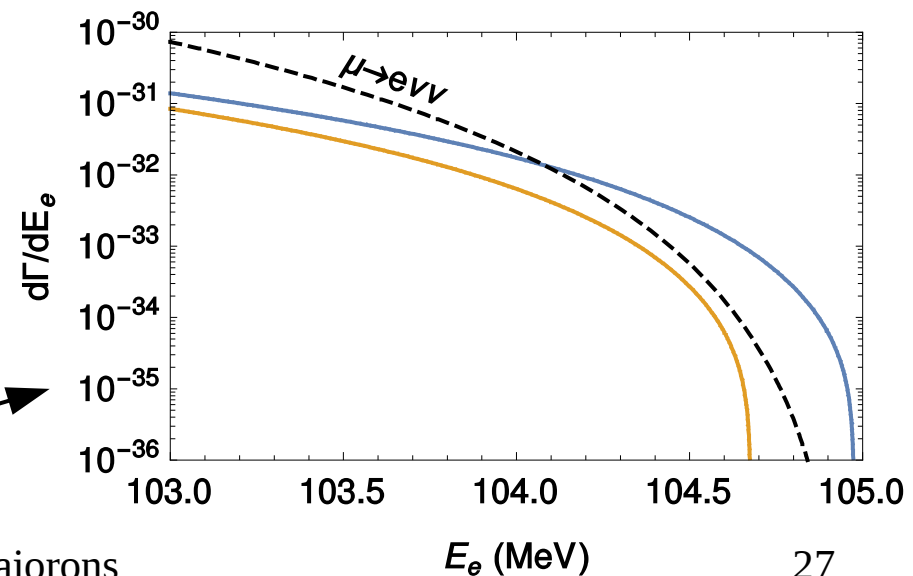
[Garcia i Tormo++, PRD '11;
Uesaka, 2005.07894]

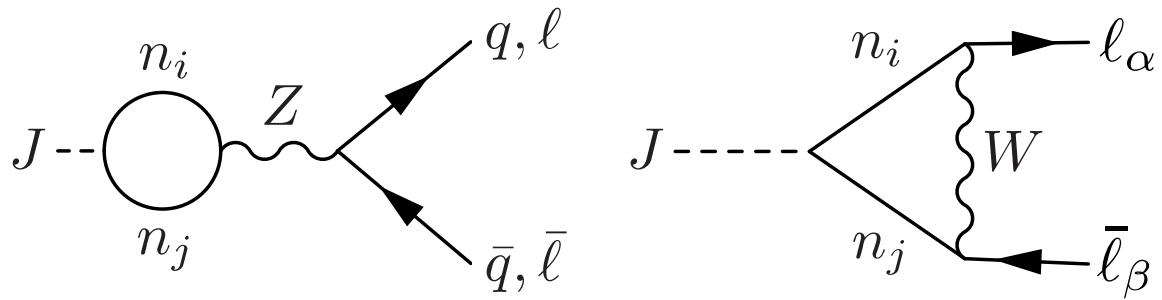
[JH++, Mu2e-II Snowmass LOI]

[Perrevoort, 1812.00741]



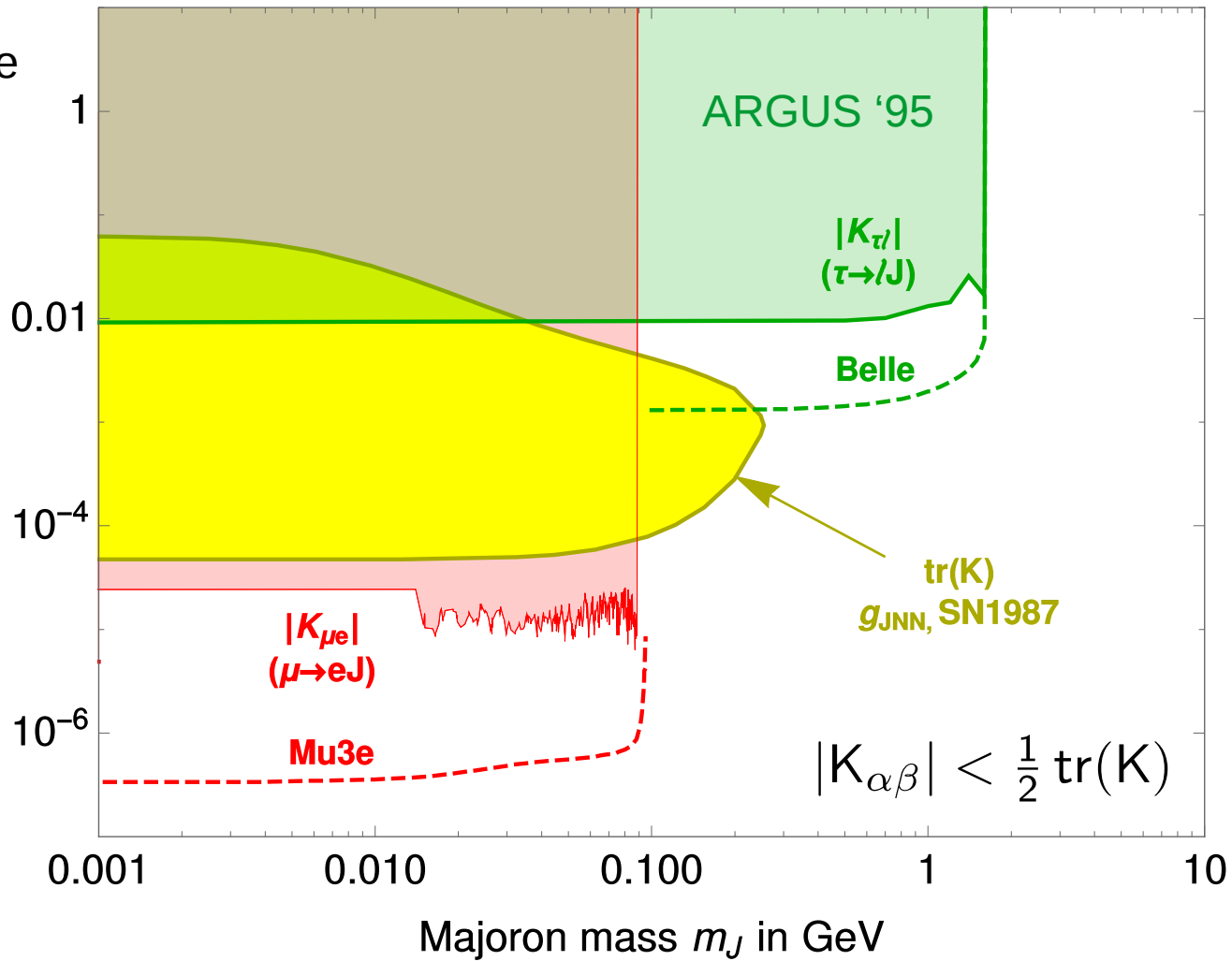
— $\mu \rightarrow eX$, $BR(\mu \rightarrow eX) = 5 \times 10^{-5}$, $m_X = 0$
 — $\mu \rightarrow eX$, $BR(\mu \rightarrow eX) = 5 \times 10^{-5}$, $m_X = 0.3$ MeV





Limit on effective coupling

$$K \equiv \frac{m_D m_D^\dagger}{f v}$$



[JH, Garcia-Cely, JHEP '17]

$$M_R = f = 1 \text{ TeV}$$

$$(m_D m_D^\dagger)_{e\mu} = [(m_D m_D^\dagger)_{ee} (m_D m_D^\dagger)_{\mu\mu}]^{1/2}$$

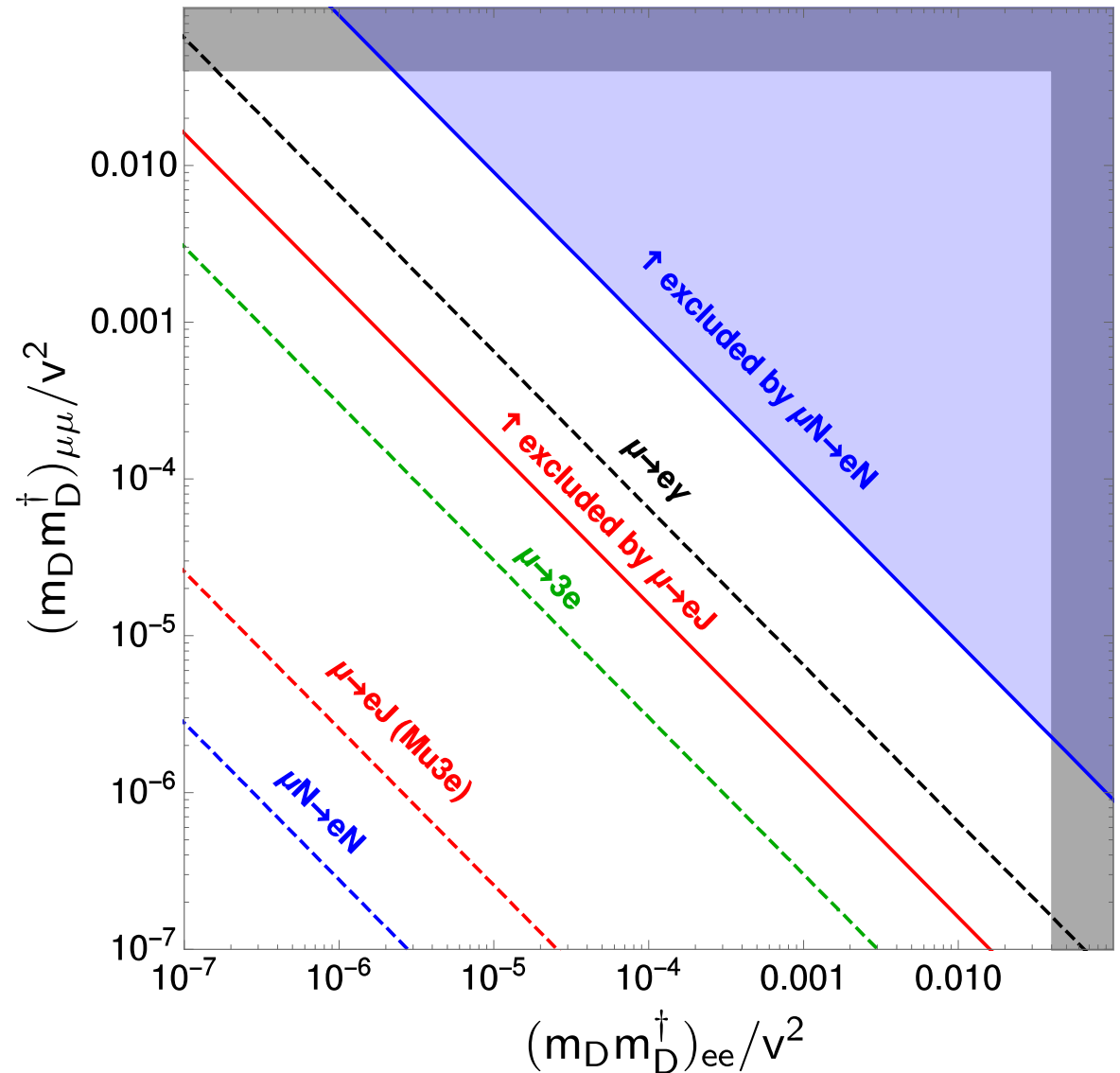
- Comparison of Majoron and non-Majoron limits.

[from Coy & Frigerio, PRD '19]

- $m_D M_R^{-2} m_D^\dagger$ vs. $\frac{m_D m_D^\dagger}{f}$.
- Sterile neutrinos modify EWPD & LFV.

$$\frac{\Gamma(\ell \rightarrow \ell' \gamma)}{\Gamma(\ell \rightarrow \ell' J)} \simeq 2\pi\alpha \frac{m_\ell^2}{M_R^2} \frac{f^2}{M_R^2}.$$

- Majoron wins for $f \sim M_R$.
- $\ell \rightarrow \ell' + J$ possible!
- Together with LFV in μ ?



[JH, Patel, PRD '19]

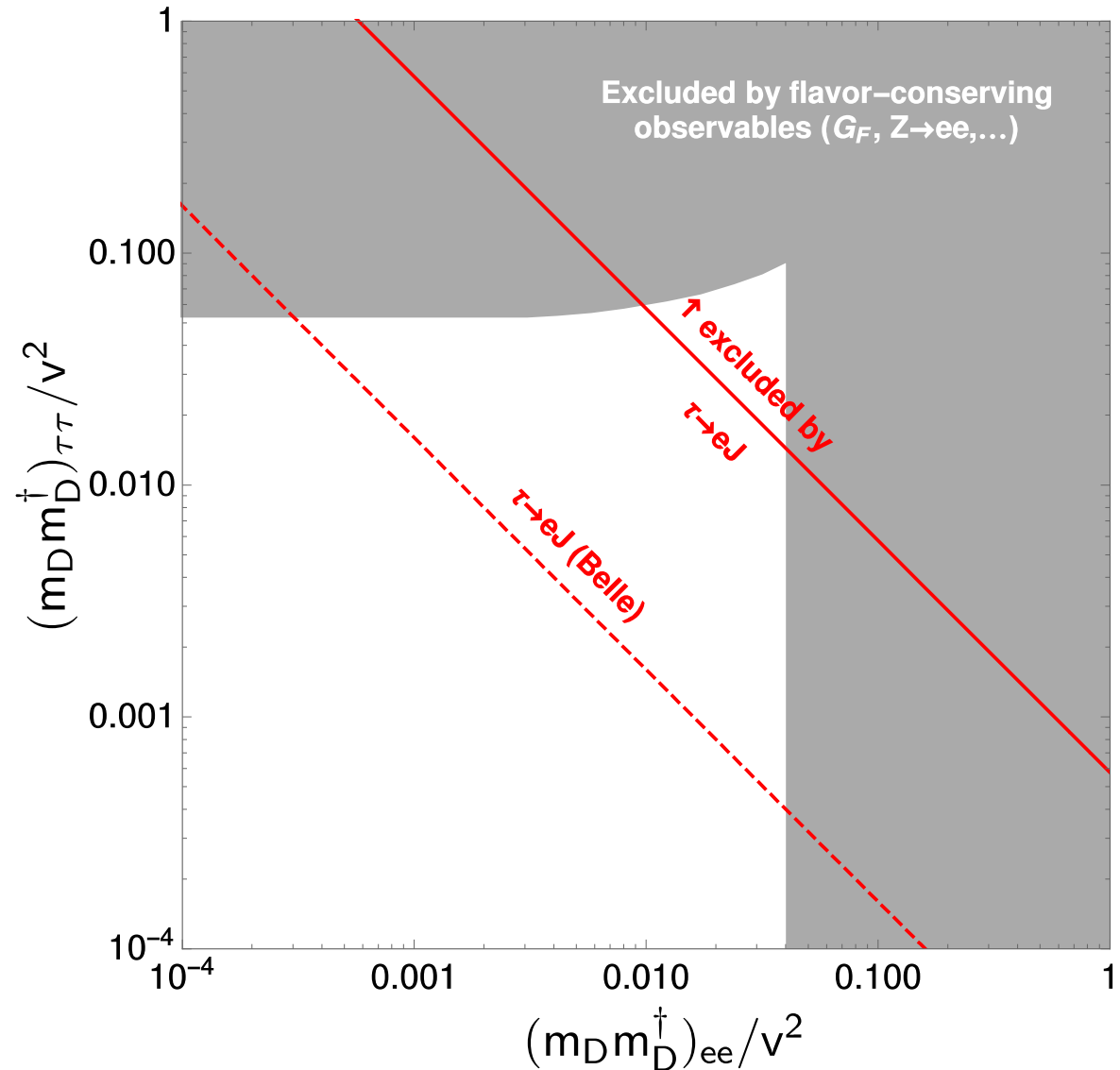
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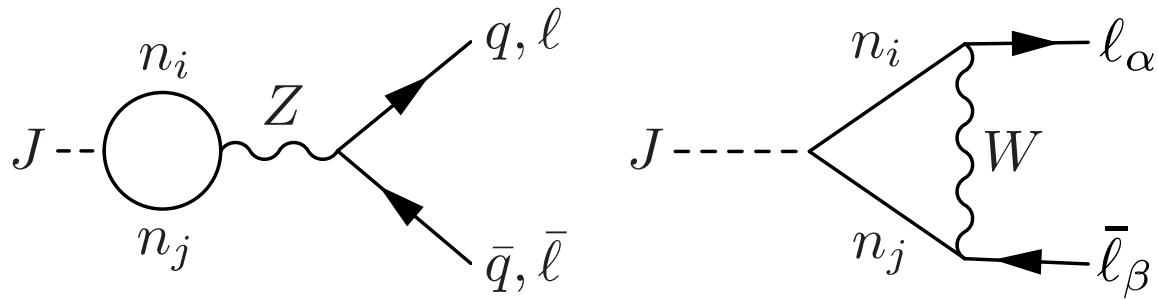
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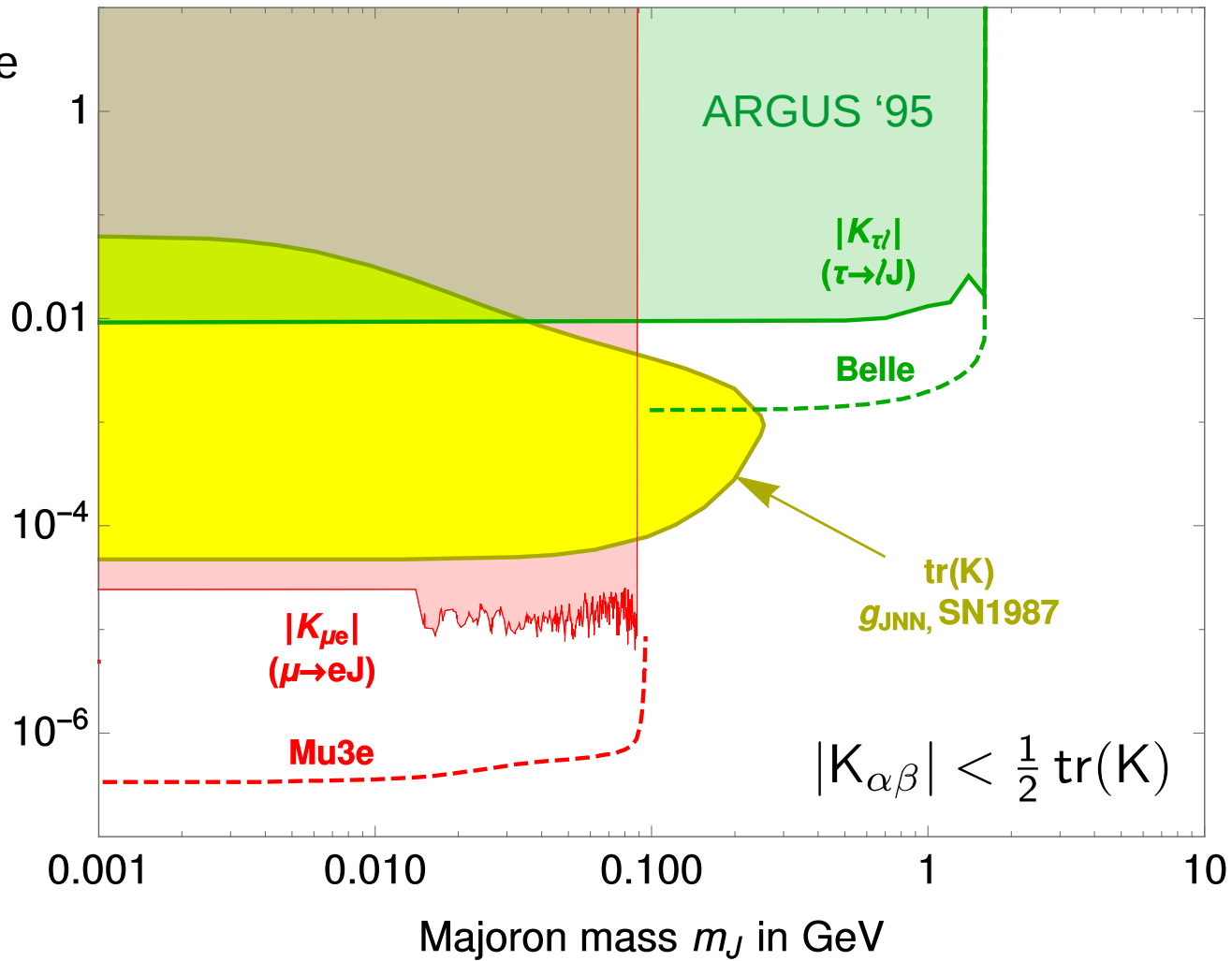


[JH, Patel, PRD '19]

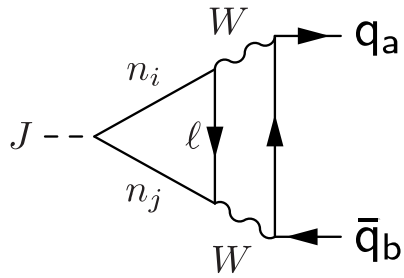


Limit on effective coupling

$$K \equiv \frac{m_D m_D^\dagger}{f v}$$



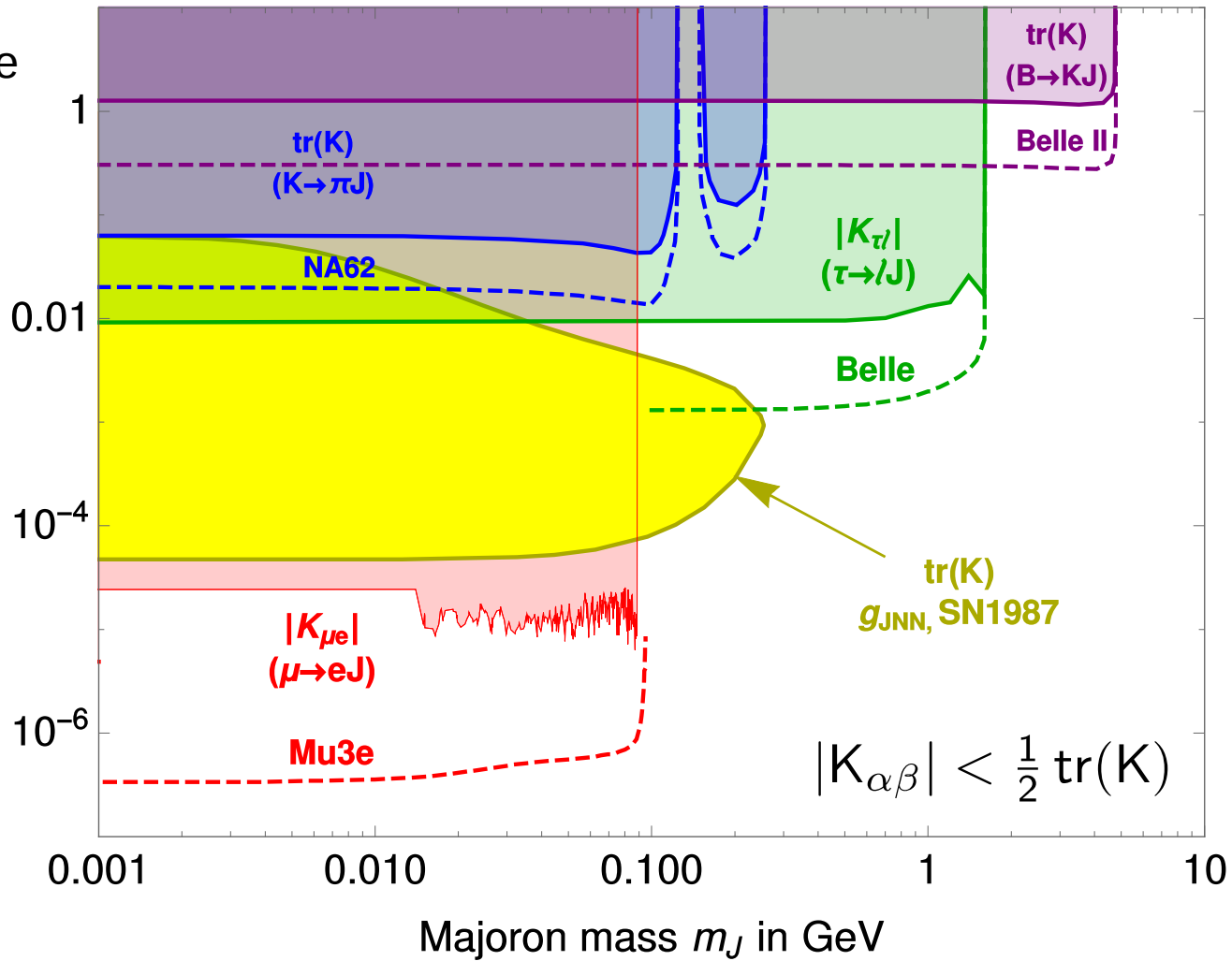
[JH, Garcia-Cely, JHEP '17]



$$\simeq \frac{\text{tr}(m_D \log(\frac{M_R}{m_W}) m_D^\dagger)}{128\pi^4 v^4 f} iJ \bar{d}_R M_d V_q^\dagger M_u^2 V_q d_L$$

Limit on effective coupling

$$K \equiv \frac{m_D m_D^\dagger}{f v}$$

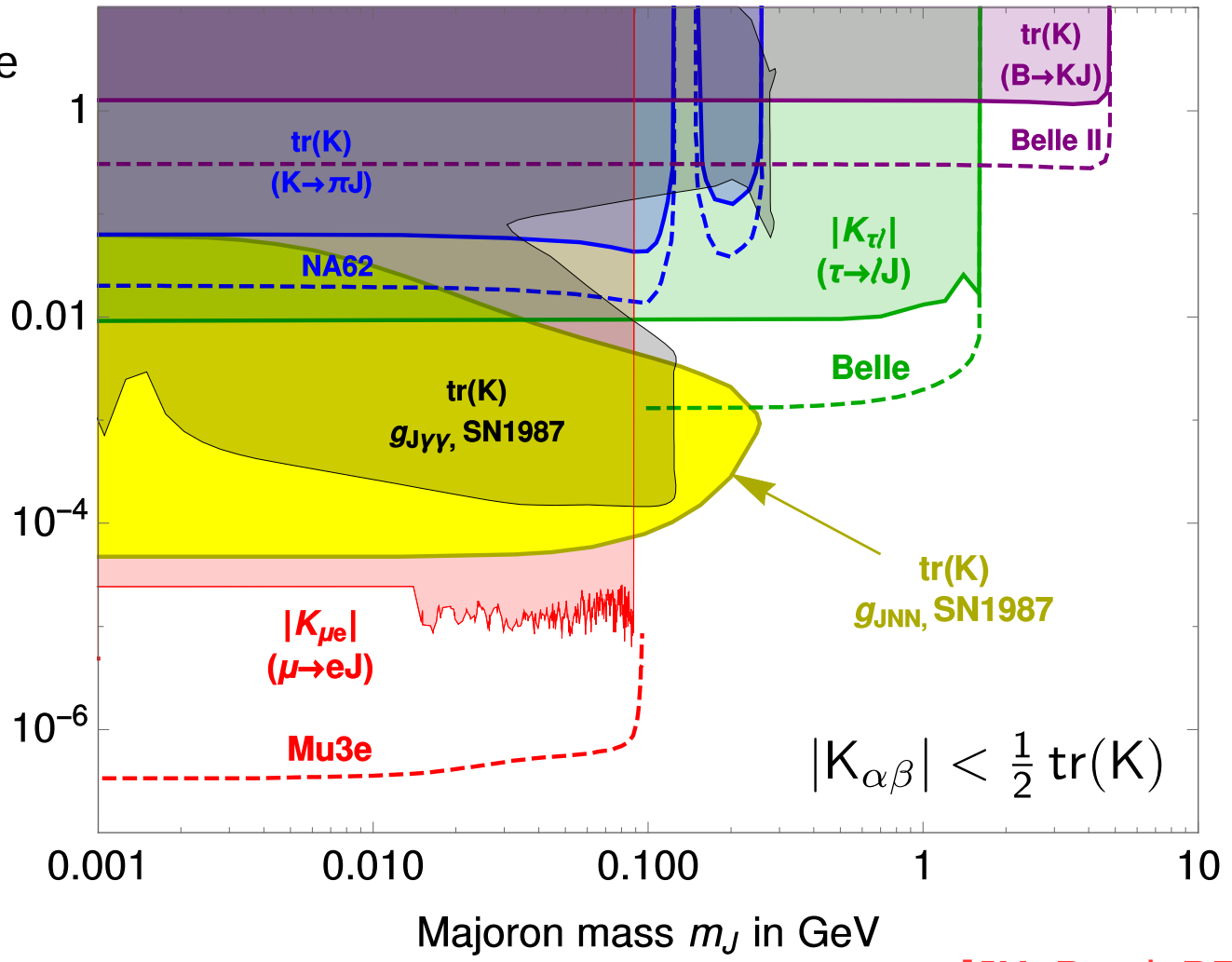


[JH, Patel, PRD '19]

$$\begin{array}{c}
 : \\
 \begin{array}{c}
 n_i \\
 \circlearrowleft \\
 n_j
 \end{array}
 \end{array}
 \begin{array}{c}
 \text{---} J \\
 \text{---} Z \\
 \text{---} f \\
 \text{---} \gamma \\
 \text{---} \gamma
 \end{array}
 \approx \frac{\alpha}{8\pi^3 v^2 f} \text{tr}(m_D m_D^\dagger) \sum_f N_c^f Q_f^2 T_3^f h\left(\frac{m_J^2}{4m_f^2}\right) + \dots$$

Limit on effective coupling

$$K \equiv \frac{m_D m_D^\dagger}{f v}$$



[JH, Patel, PRD '19]

Summary

- Majoron = simple axion-like particle connected to seesaw.
- Seesaw parameters encoded in **loop** couplings (J_{ff} & J_{yy}).
- In the sky:
 - $DM \rightarrow \nu\nu$ @ JUNO, DUNE, Hyper-K, DARWIN,...
 - $DM \rightarrow \gamma\gamma, \bar{\ell}\ell', \bar{q}q$ @ Fermi, CTA, e-ASTROGAM,...
- In the lab:
 - One loop: $\ell \rightarrow \ell' + J$ @ MEG, Mu3e, Mu2e, Belle II,...
 - Two loops: $K \rightarrow \pi J, B \rightarrow K J$ @ NA62, Belle II, LHCb.
- Next step: add prompt/displaced/delayed vertices, $J \rightarrow SM$.

Always look out for lines!

Backup

Pseudo-Goldstone

- Spontaneous global U(1) breaking gives $m_J = 0$.
- Non-zero mass from:

- Breaking by gravity, e.g. wormholes,

$$m_J \sim M_{\text{Pl}} \exp \left[-\mathcal{O}(M_{\text{Pl}}/f) \right].$$

[Alonso, Urbano, 1706.07415]

- Anomalies, e.g. if $U(1)_{\text{B-L}} = U(1)_{\text{PQ}}$.

[Mohapatra, Senjanovic '83; Langacker, Peccei, Yanagida '86; SMASH '16]

- Explicit breaking, e.g. $\Delta V = \frac{1}{2} m_J^2 J^2$.

$\mu \rightarrow e J$ with $J \rightarrow$ invisible

- TWIST, '15: limits on different anisotropies.
- Chiral coupling $\bar{\mu} P_L e J$ suppresses sensitivity!

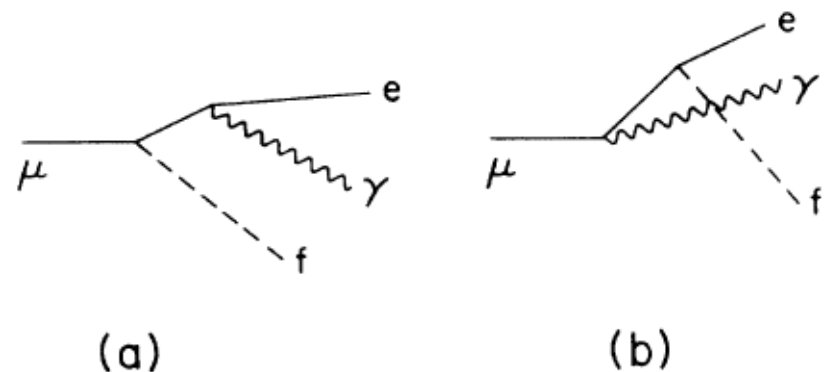
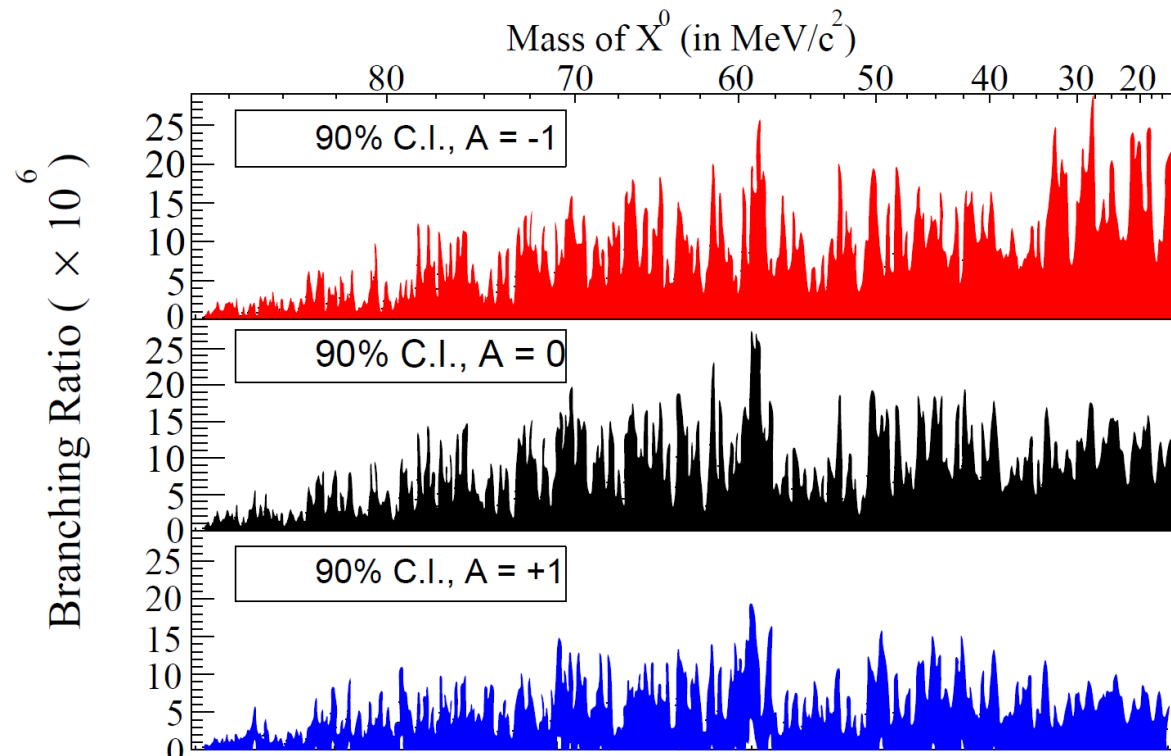
[JH, Garcia-Cely, 1701.07209]

- Bremsstrahlung is competitive: $\mu \rightarrow e J \gamma$.

[Goldman et al, '87]

- Approximate limit

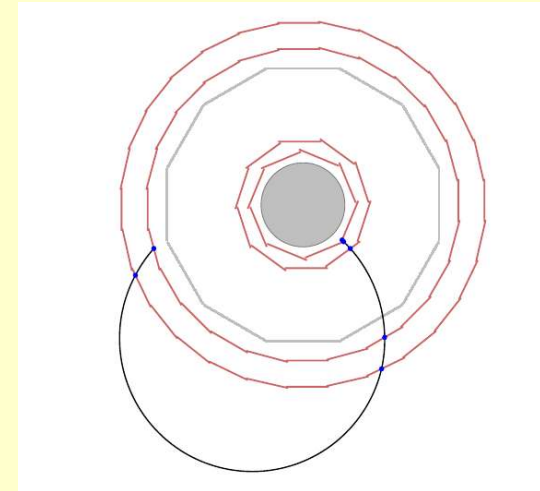
$$\frac{|(m_D m_D^\dagger)_{\mu e}|}{v f} \lesssim 10^{-5}.$$



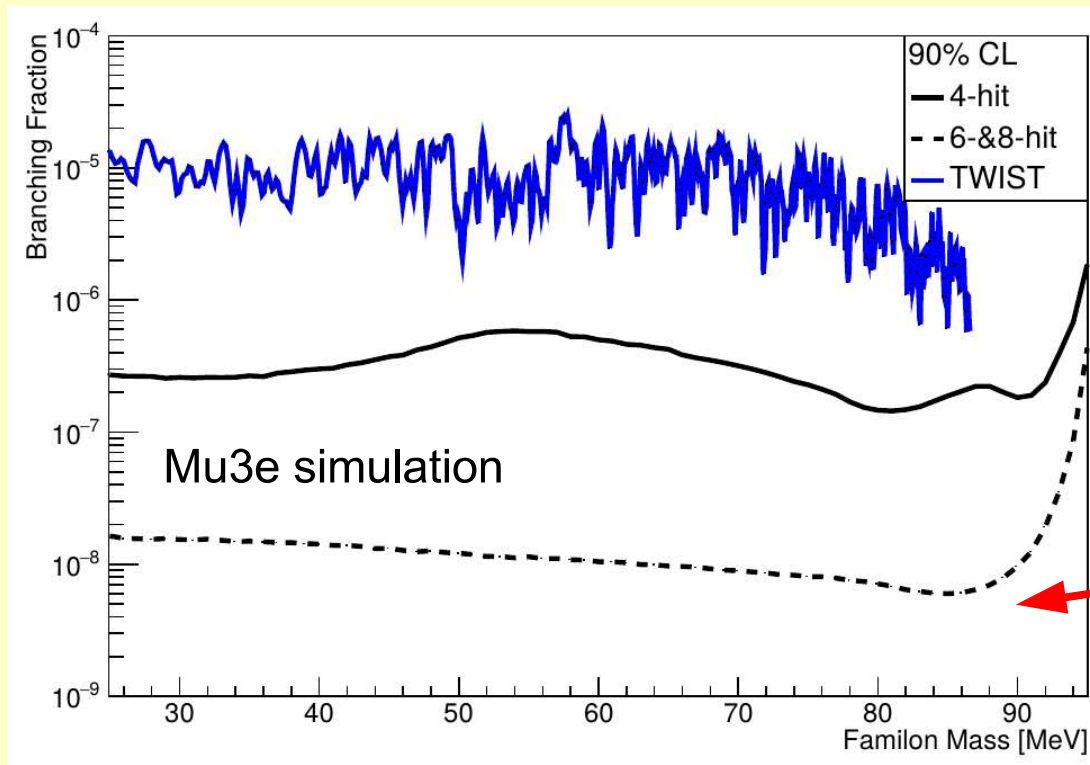


Searches for $\mu \rightarrow e X$ with Mu3e

- Full reconstruction of all Michel decays is a big challenge for data acquisition
- $B(\mu \rightarrow e X) \sim 10^{-8}$ at 90 % CL



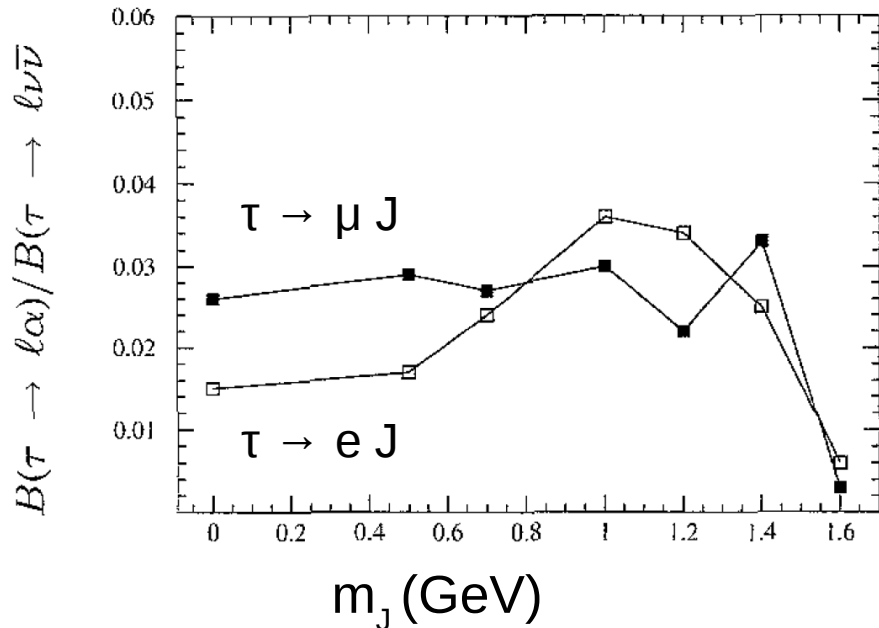
recurling track in Mu3e



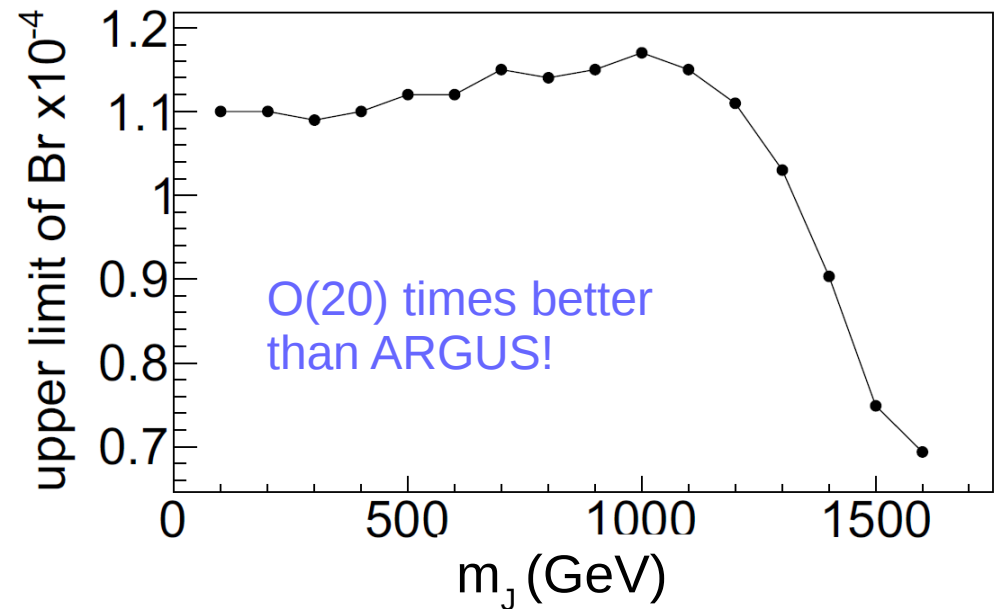
required full reconstruction of “recurlers”

$\tau \rightarrow \ell J$ with $J \rightarrow$ invisible

- ARGUS, '95; 5e5 taus.



- Belle, '16 prelim.; 1e9 taus.



- Also interesting for LFV Z'.

[JH, 1602.03810; Altmannshofer et al, 1607.06832]

- Improvement with Belle II.

$$\frac{|(m_D m_D^\dagger)_{\tau e}|}{v f} \lesssim 6 \times 10^{-3},$$

$$\frac{|(m_D m_D^\dagger)_{\tau \mu}|}{v f} \lesssim 9 \times 10^{-3}.$$

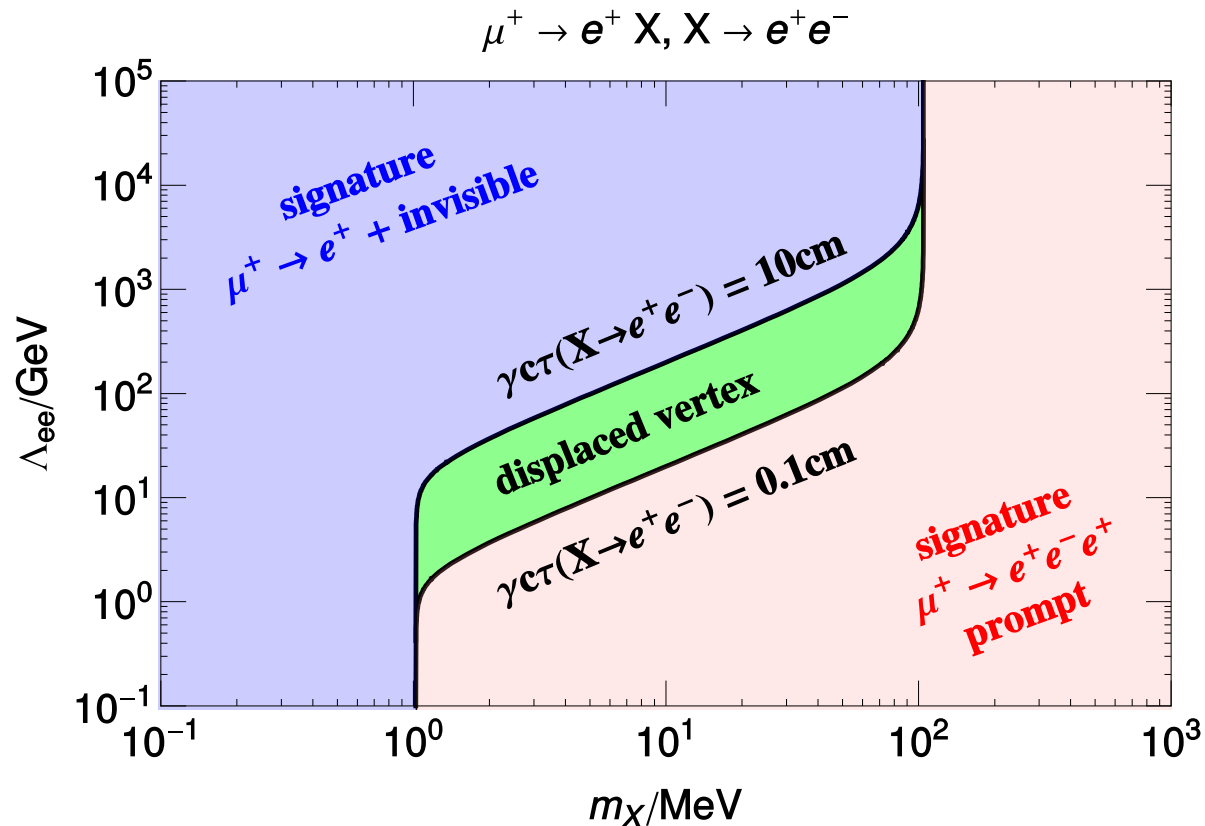
$\mu \rightarrow e X$ with $X \rightarrow$ visible

- Take $X \bar{e} y_5 e m_e / \Lambda_{ee}$.
- Decay length determines signature.
- Displaced vertex gives new observable.

[JH, Rodejohann, PLB '18]

- Muon at rest:

$$\gamma c \tau \simeq \frac{\pi m_\mu \Lambda_{ee}^2}{m_e^2 m_X^2} \simeq 2.5 \text{ cm} \left(\frac{\Lambda_{ee}}{100 \text{ GeV}} \right)^2 \left(\frac{10 \text{ MeV}}{m_X} \right)^2.$$

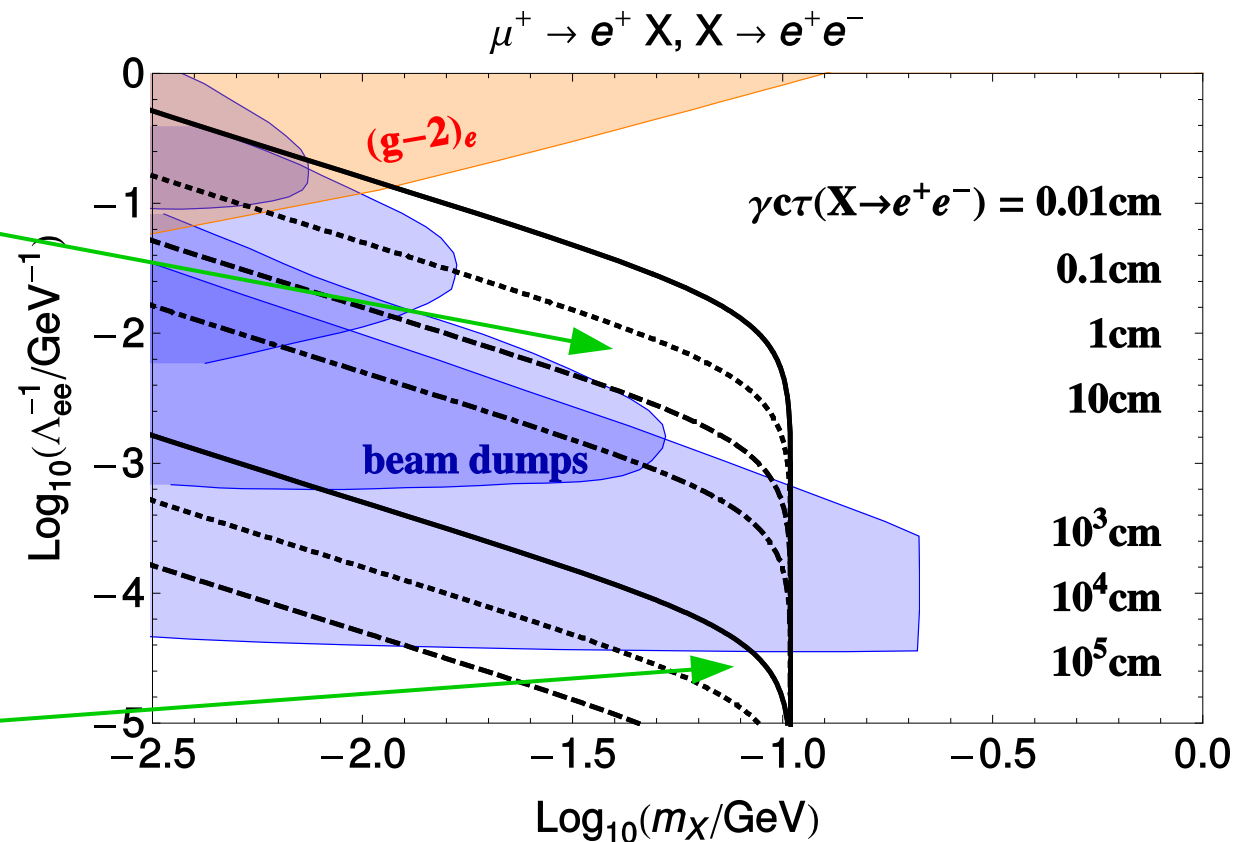


Sub-GeV X with ee coupling allowed?

$\mu \rightarrow e X$ with $X \rightarrow \bar{e}e$

[JH, Rodejohann, PLB '18]

- Decay length typically below cm. \Rightarrow looks prompt.
- Below beam dump: $\Lambda_{ee} > 30$ TeV; mostly invisible, but some DV!



$$\text{BR}(\mu \rightarrow eX) \text{BR}(X \rightarrow ee) (1 - P(l_{\text{dec}}))$$

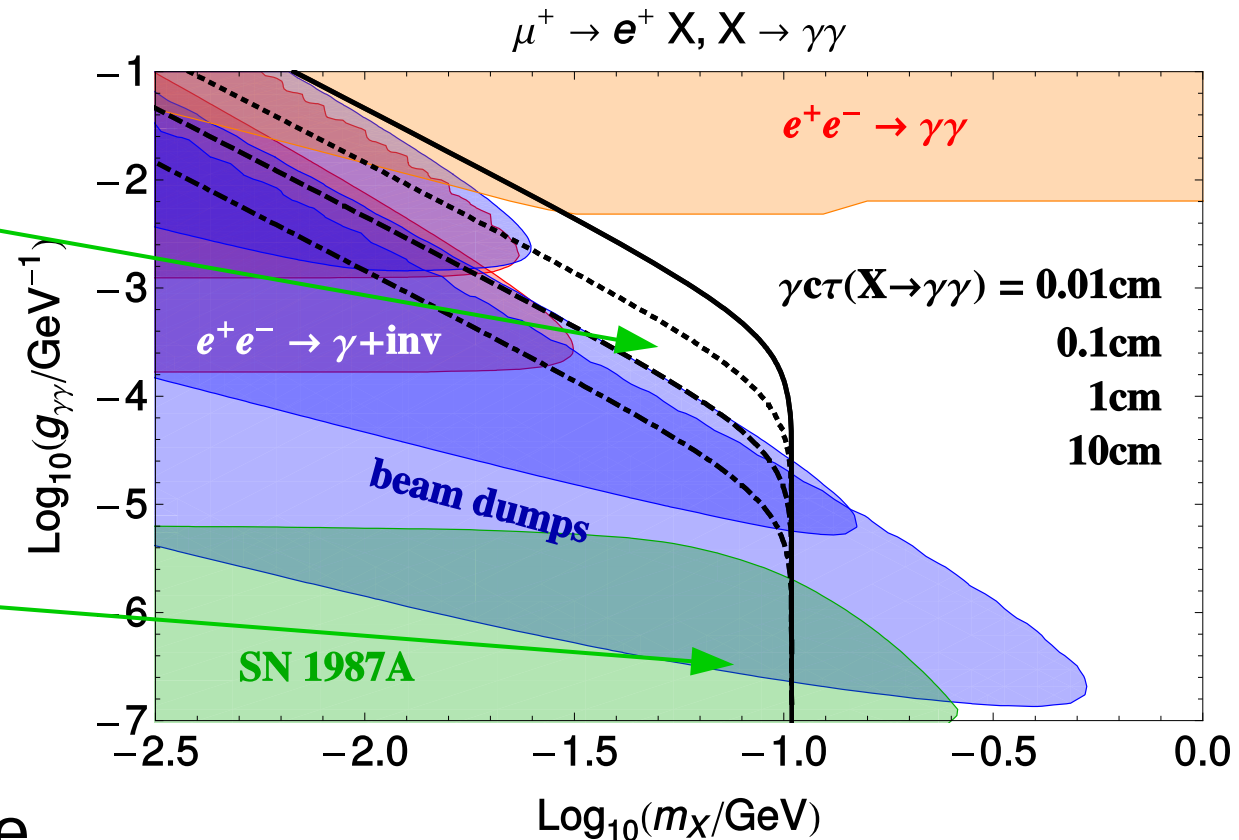
$$\simeq \text{BR}(\mu \rightarrow eX) \frac{l_{\text{dec}}}{\gamma_{\text{CT}}}$$

Possible in Mu3e!

$\mu \rightarrow e X$ with $X \rightarrow \gamma\gamma$

[JH, Rodejohann, PLB '18]

- Decay length always below cm. \Rightarrow looks prompt.
- Below beam dump: supernova constraints!
- Prompt channel still interesting, maybe MEG(II) or Mu3e extension?



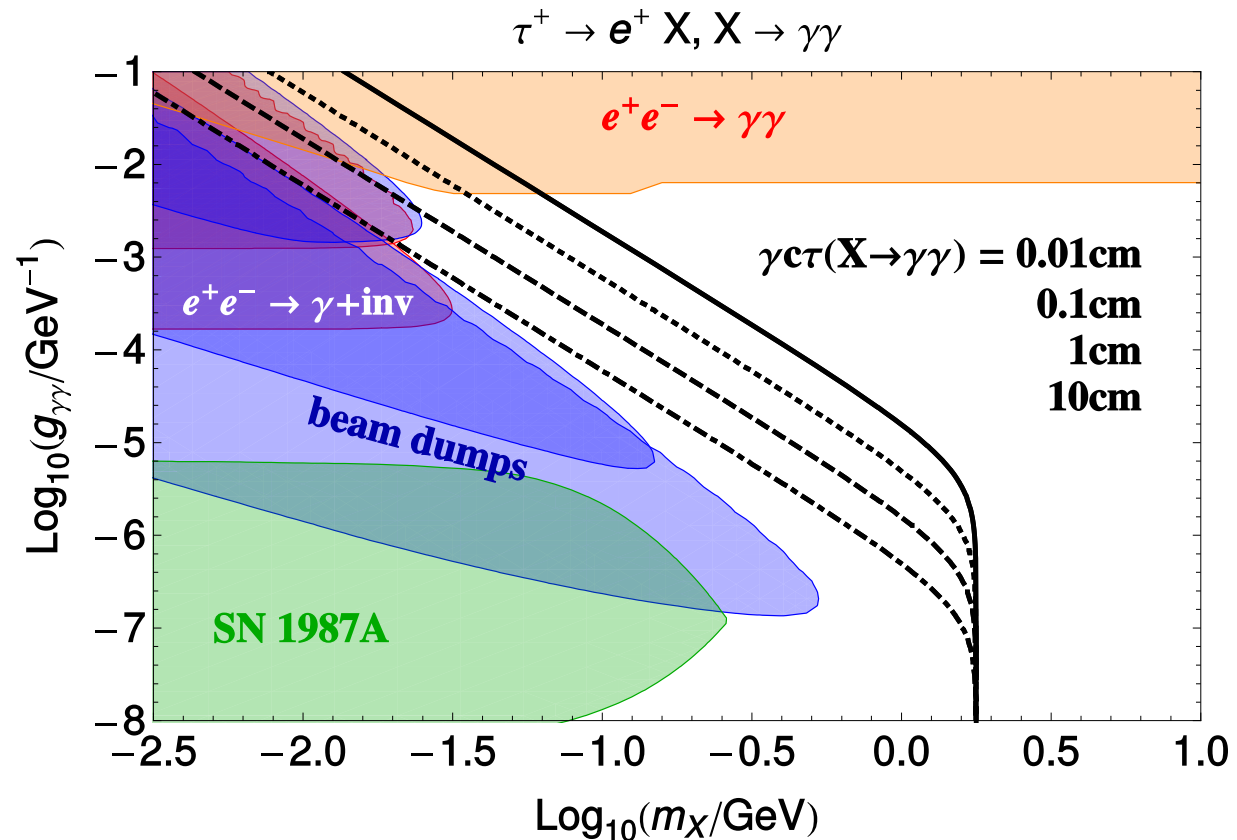
[Limits: Dolan et al, JHEP '17]

Muons difficult, taus easier.

$\tau \rightarrow e X$ with $X \rightarrow$ visible

[JH, Rodejohann, PLB '18]

- Tau at rest, higher X boost.
- Arbitrary decay lengths possible.
- Similar for $X \rightarrow ee, \mu\mu, \mu e$.
- Worthwhile in LHCb and Belle (II).



[Limits: Dolan et al, JHEP '17]

New signatures from light physics!

Quark Flavor Phenomenology of the QCD Axion

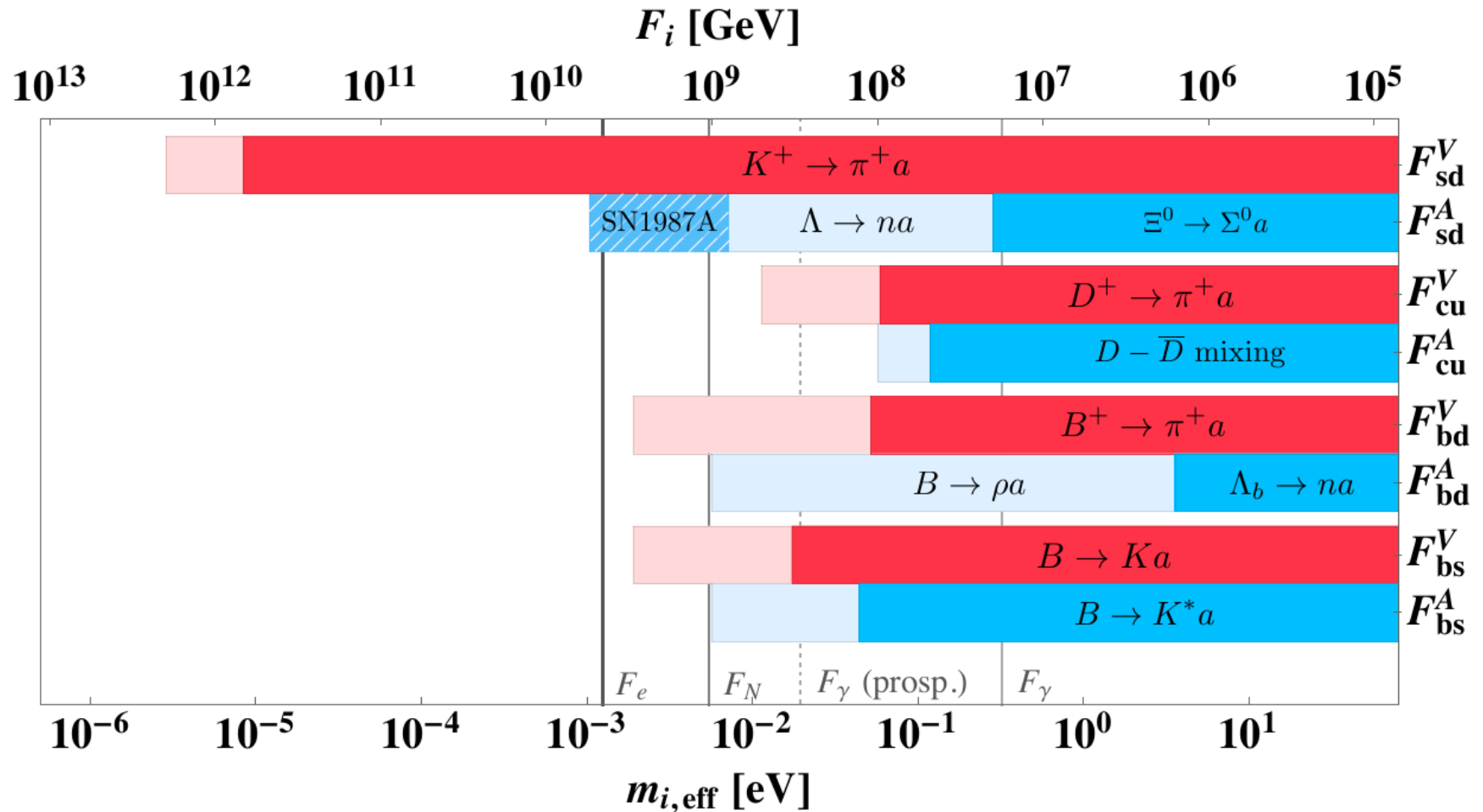


FIG. 4. Summary of the most important bounds for the different flavor sectors and for vectorial (red) and axial-vectorial (blue) couplings. On the lower axis we indicate the corresponding values for the effective axion mass defined by $m_{i,eff} \equiv 4.69 \text{ eV} \times 10^6 \text{ GeV}/F_i$. Also shown as vertical gray lines are the bounds on axion couplings to electrons F_e (95%CL), nucleons F_N , and photons F_γ (95%CL), see Section [V](#) for details.

[Camalich, Pospelov, Vuong, Ziegler, Zupan, 2002.04623]