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Anomaly Free U(1)'s For Fermion Masses and Leptogenesis

Based on works: *Phys.Rev.D* 106 (2022) 11, 115002 (Z.T.)
(*arXiv: 2209.14404*)
arXiv: 2307.???? (A. Achelashvili, Z.T.)



July 18, 2023

**High Energy Seminar
Department of Physics,
OSU, Stillwater**

Outline

- Intro: Shortcomings, Problems & Puzzles of SM → *New Physics*
- New $U(1)_{\text{Flavor}}$ model proposed:
 - Non-anomalous flavor sym. with economical setup → texture zeros ;
 - several successful charged fermion mass patterns emerged
 - Interesting pattern for neutrino masses & mixings - predictive neutrino sector – *inverted hierarchical*
- Resonant Leptogenesis (by \sim TeV scale RHNs)
- Summary

Some shortcomings / puzzles of SM:

Within the SM

- Hierarchies of Ch. fermion masses / mixings
- Neutrino oscillations masses / mixings - unexplained
- Needed amount of the baryon asymmetry can't be generated

...

- Charged fermion masses & mixings

Observed Noticeable Hierarchies:

$$\lambda_t \sim 1, \quad \lambda_u : \lambda_c : \lambda_t \sim \lambda^8 : \lambda^4 : 1$$

$$\lambda_b \sim \lambda_\tau \sim \frac{m_b}{m_t}, \quad \lambda_d : \lambda_s : \lambda_b \sim \lambda^4 : \lambda^2$$

With $\lambda=0.2$

$$\lambda_e : \lambda_\mu : \lambda_\tau \sim \lambda^5 : \lambda^2 : 1$$

$$V_{us} \approx \lambda, \quad V_{cb} \approx \lambda^2, \quad V_{ub} = \lambda^4 - \lambda^3$$

What is origin of these hierarchies?

Is there any relation or sum rule?

Why three families?

Within SM no answer to these questions...

Extension With Flavor Symmetry

Flavor symmetry G_F distinguishing families can explain hierarchies

Simplest possibility: $G_F = U(1)_F$ (Froggatt, Nielsen'79)

$$U(1)_F : \quad \phi_i \rightarrow e^{iQ(\phi_i)} \phi_i$$

$$Q(F_i) = n_i, \quad Q(F_i^c) = \bar{n}_i, \quad Q(H) = 0, \quad Q(X) = -1$$

← **'flavon'**

With $n_i + \bar{n}_j \neq 0$: coupling ~~$F_i F_j^c H$~~ forbidden!

$$\left(\frac{X}{M_*} \right)^{n_i + \bar{n}_j} F_i F_j^c H \longrightarrow \epsilon^{n_i + \bar{n}_j} F_i F_j^c H \quad \rightarrow \text{Suppressed couplings emerge}$$

$$\frac{\langle X \rangle}{M_*} \equiv \epsilon \ll 1 \quad M_* \quad \text{- cut off scale (simplest possibility } M_* \sim M_{\text{Pl}})$$

Several/multiple flavons also can be considered

Possible candidates for flavor $U(1)_F$

- Global $U(1)_F$ is unattractive:

- Spont. breaking \rightarrow pseudo-Goldstones (phen. difficulties)

- Explicit breaking \rightarrow against the 'rules' (selection criteria?)

Do gravity, non-perturbative effects respect global symmetries?
Trustful setting?

- Local $U(1)_F$:

Models with gauged $U(1)_F$ are highly constrained
due to anomaly cancellation condition

SM is anomaly free; But extra flavor $U(1)_F$ requires
additional care

-- Anomalous $U(1)$ (of stringy origin)

(Dine, Seiberg, Witten'87)

GS mechanism for anomaly cancellation.

Conditions:
$$\frac{A_{YY1}}{2k_Y} = \frac{A_{221}}{k_2} = \frac{A_{331}}{k_3} = \frac{A_{111}}{3k_1} = \frac{A_{GG1}}{24}$$

Anomaly coefficients: (Gravity) $^2 \cdot U(1)_F : A_{GG1} = \text{Tr}[Q_{U(1)_F}]$

$$U(1)_Y^2 \cdot U(1)_F : A_{YY1} = \sum_i Q_Y^2(i) Q_{U(1)_F}(i)$$

$$SU(1)_L^2 \cdot U(1)_F : A_{221} = \sum_i T_2(i) Q_{U(1)_F}(i) , \dots$$

String Unification conds:
$$k_i g_i^2 = k_1 g_A^2 = 2g_{st}^2$$

- • Anomalous $U(1)_F$ as flavor symmetry \rightarrow successful fermion hierarchies

(Ibanez, Ross'94;
Binetruy, Ramond'95;
Jain, Shrock'95 ...)

-- Anomaly free $U(1)_F$ [not of 'stringy origin'] --

- Earlier Works

- Within MSSM, some anom. free $U(1)_F$'s with successful $Y_{U,D,E}$
(Dudas, Pokorski, Savoy, hp/9504292)
- Within MSSM & $SU(5)$ GUT, some examples/models of anom. free $U(1)_F$'s
(Mu-Chun Chen, et al, ph/0612017, 0801.0248)

Within $SU(5)$ GUT: Z.T. PRD 87, 075026 ; PLB 706, 398-405
based on unified GUT+ $U(1)$ -part of flavor

Within GUTs become more non-trivial [multiplet's charges related]

Challenge to find simple anom. free $U(1)_F \times G_{GUT}$

Let's start by $U(1)_F \times G_{SM} \dots$

Search Anomaly Free $U(1) \leftarrow$ embedding In Non-Abelian group

1): $10[0] + 5^*[0]$

2): $10[\alpha] + 5^*[-3\alpha] + 1[5\alpha]$

3): $10[\beta] + 5^*[\beta] + 1[\beta] + 5[-2\beta] + 5'^*[-2\beta] + 1'[4\beta]$

Finding 2) via $SO(10) \rightarrow SU(5) \times U(1)''$: $16 = 10[1] + 5^*[-3] + 1[5]$
(Flipped $SU(5)$ type) $10 = 5[-2] + 5^*[2]$

Finding 3) via $E_6 \rightarrow SO(10) \times U(1)' \rightarrow SU(5) \times U(1)'$:

$$27 = 16[1] + 10[-2] + 1'[4] =$$

$$10[1] + 5^*[1] + 1[1] + 5[-2] + 5'^*[-2] + 1'[4]$$

Finding 2) + 3): Also possible Superposition of $U(1)'$ and $U(1)''$

All other findings, such as E_7 , E_8 , $SU(N > 6)$ give extra $SU(5)$ states

Superposition of $U(1)'$ and $U(1)''$: $Q_{\text{sup}}=aY'+bY''$

Three Types of Charge selection Emerge:

A: $10_0+5^*_0$

B: $10_a + 5^*_{-3a} + 15_a$

C: $10_{a+b} + 5^*_{a-3b} + 1_{a+5b} + 5_{-2a-2b} + 5'_{-2a+2b} + 1'_{4a}$

One family can have A-type Charges, another one B-type, etc.

Acceptable combinations:

ABB

BBB

ABC

BBC

For example, **ABB**: $10_0 + 5^*_0$

$$10_\alpha + 5^{*-3}_\alpha + 15_\alpha$$

$$10_{\alpha'} + 5^{*-3}_{\alpha'} + 15_{\alpha'}$$

$$H_q + H^{*-q}$$

Some selection rules ('guide'):

AAB: rejected because of two 10 's same 0 -charge

ACC: rejected for two 5 -plets

In case of **ABB**, α and α' should be related

$$\alpha/\alpha' = m/n, \text{ to avoid two } U(1)\text{s}$$

Classify acceptable up type quark mass matrices...

Within GUTs charges of fermion states related →

→ Constrains & No much textures

Challenge to find simple anom. free $U(1)_F \times G_{GUT}$

Let's start by $U(1)_F \times G_{SM} \dots$

Model: SM Extension with $U(1)_F$

$U(1)_F$ - gauge symmetry

X - scalar (flavon– the SM singlet), for $U(1)_F$ breaking

$N_{1,2,\dots}$ - SM singlet fermions – RHN's

$G_{SM} = SU(3)_c \times SU(2)_L \times U(1)_Y$ non-trivial states

just those of SM Higgs doublet φ

three families of matter $\{q, u^c, d^c, l, e^c\}_{i=1,2,3}$

Anomaly Constrain

- SM Anomalies are intact (i.e. vanish)

Other anomalies (direct $U(1)_F$ & mixed) must vanish:

$$(U(1)_F)^3 : \quad A_{111} = \sum_i Q_i^3$$

$$U(1)_Y \times (U(1)_F)^2 : \quad A_{Y11} = \sum_i Y_i Q_i^2$$

$$(U(1)_Y)^2 \times U(1)_F : \quad A_{YY1} = \sum_i Y_i^2 Q_i$$

$$(SU(2)_L)^2 \times U(1)_F : \quad A_{221} = \sum_i [Q_i(l_i) + 3Q_i(q_i)]$$

$$(SU(3)_c)^2 \times U(1)_F : \quad A_{331} = \sum_i [2Q_i(q_i) + Q_i(u_i^c) + Q_i(d_i^c)]$$

$$(\text{Gravity})^2 \times U(1)_F : \quad A_{GG1} = \sum_i Q_i$$

anomaly free $U(1)$'s

a) hypercharge symmetry $U(1)_Y$

b) with RHN's $N_{1,2,\dots}$ gauged $(B - L)$

Family dependent $U(1)_Y$ and (B-L) and/or their superpositions

$$\bar{a}_i Y(f) + \bar{b}_i Q_{B-L}(f)$$

Automatically anomaly free

1) By requiring top quark renormalizable Yukawa coupling

$$\lambda_t \sim 1$$

→ also bottom and tau Yukawas allowed at renormalizable level – expectancy $\lambda_b, \lambda_\tau \sim 1$

2) only with \bar{a}_i, \bar{b}_i No much/desirable texture zeros.

Drawbacks:

Modification:

$$Q_i(f) = \bar{a}_i Y(f) + \bar{b}_i Q_{B-L}(f) + \Delta Q_i(f)$$

Such that: anomalies $A_{YY1}, A_{221}, A_{331}, A_{GG1}$ stay intact.

Four RHNs - $N_{1,2,3,4}$ **and**

$$\Delta Q_i(q) = \bar{q}_3 \{0, 1, -1\} + \bar{q}_8 \{1, 1, -2\}$$

$$\Delta Q_i(u^c) = \bar{u}_3 \{0, 1, -1\} + \bar{u}_8 \{1, 1, -2\}$$

$$\Delta Q_i(d^c) = \bar{d}_3 \{1, -1, 0\} + \bar{d}_8 \{1, 1, -2\}$$

$$\Delta Q_i(l) = \bar{l}_3 \{1, -1, 0\} + \bar{l}_8 \{1, 1, -2\} ,$$

$$\Delta Q_i(e^c) = 0 ,$$

$$\Delta Q_i(N) = \bar{n} \{1, 1, 1, -3\} .$$

will be enough for our purposes

Requirements upon selection of $\bar{a}_i, \bar{b}_i, \bar{n} \cdot (\bar{q}_{3,8}, \dots, \bar{l}_{3,8})$

- (i) Top Yukawa via $q_3 u_3^c \varphi \rightarrow \lambda_t \sim 1$
All other Yukawas suppressed / hierarchical
→ Naturally obtain desirable pattern**
- (ii) Dirac and Majorana RHN couplings should naturally generate desirable neutrino oscillations**

- (iii) Care must be taken for canceling anomalies**

$$A_{111} = \sum Q_i^3 \quad A_{Y11} = \sum Y_i Q_i^2$$

- (iv) Ratios of the states' charges should be rational**

→ allow (phenomenologically required) couplings between them.

One solution – charge assignment

Normalization: $Y(l) = 1$ and $Q_{B-L}(q) = 1/3$

$$\bar{a}_i = \frac{1}{3}\{46, 43, 10\} , \quad \bar{b}_i = \frac{1}{3}\{-91, 35, 38\} ,$$

$$\{\bar{q}_3, \bar{u}_3, \bar{d}_3, \bar{l}_3\} = \frac{1}{3}\{-16, 7, -67/2, -3/2\} ,$$

$$\{\bar{q}_8, \bar{u}_8, \bar{d}_8, \bar{l}_8\} = \frac{1}{9}\{38, -41, 23/2, 51/2\} , \quad \bar{n} = -\frac{5}{3}$$

Table 1: $U(1)_F$ charge (Q) assignment for the states. $Q_X = 1$, $Q_\varphi = -7$.

	$\{q_1, q_2, q_3\}$	$\{u_1^c, u_2^c, u_3^c\}$	$\{d_1^c, d_2^c, d_3^c\}$	$\{l_1, l_2, l_3\}$	$\{e_1^c, e_2^c, e_3^c\}$	$\{N_1, N_2, N_3, N_4\}$
Q	$\{-11, -2, 0\}$	$\{26, 13, 7\}$	$\{-10, -1, -9\}$	$\{48, 6, -15\}$	$\{-61, -17, 6\}$	$\{-32, 10, 11, 5\}$

1) All anomalies vanish

**2) This Q selection gives nice textures →
Natural understanding of hierarchies**

Yukawa couplings are fixed by $U(1)_F$ charges:

$$(q_1, q_2, q_3) \begin{pmatrix} \bar{\varepsilon}^8 & \varepsilon^5 & \varepsilon^{11} \\ \bar{\varepsilon}^{17} & \bar{\varepsilon}^4 & \varepsilon^2 \\ \bar{\varepsilon}^{19} & \bar{\varepsilon}^6 & 1 \end{pmatrix} \begin{pmatrix} u_1^c \\ u_2^c \\ u_3^c \end{pmatrix} \varphi$$

$$(q_1, q_2, q_3) \begin{pmatrix} \varepsilon^{14} & \varepsilon^5 & \varepsilon^{13} \\ \varepsilon^5 & \bar{\varepsilon}^4 & \varepsilon^4 \\ \varepsilon^3 & \bar{\varepsilon}^6 & \varepsilon^2 \end{pmatrix} \begin{pmatrix} d_1^c \\ d_2^c \\ d_3^c \end{pmatrix} \tilde{\varphi}$$

$$(l_1, l_2, l_3) \begin{pmatrix} \varepsilon^6 & \bar{\varepsilon}^{38} & \bar{\varepsilon}^{61} \\ \varepsilon^{48} & \varepsilon^4 & \bar{\varepsilon}^{19} \\ \varepsilon^{69} & \varepsilon^{25} & \varepsilon^2 \end{pmatrix} \begin{pmatrix} e_1^c \\ e_2^c \\ e_3^c \end{pmatrix} \tilde{\varphi}$$

$$\frac{X}{M_{\text{Pl}}} \equiv \varepsilon, \quad \frac{X^*}{M_{\text{Pl}}} \equiv \bar{\varepsilon}$$

Hierarchical, good fit with: $\langle \varepsilon \rangle = \langle \bar{\varepsilon} \rangle \equiv \epsilon \approx 0.2$

Some elements $\approx 0 \rightarrow$ Texture zeros:

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$$(q_1, q_2, q_3) \begin{pmatrix} \varepsilon^{-8} & \varepsilon^5 & \varepsilon^{11} \\ \varepsilon^{-17} & \varepsilon^{-4} & \varepsilon^2 \\ \varepsilon^{-19} & \varepsilon^{-6} & 1 \end{pmatrix} \begin{pmatrix} u_1^c \\ u_2^c \\ u_3^c \end{pmatrix} \varphi$$

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Neutrino Dirac & Majorana Couplings

$$(l_1, l_2, l_3) \begin{pmatrix} \overline{\varepsilon}^9 & \overline{\varepsilon}^{51} & \overline{\varepsilon}^{52} \\ \varepsilon^{33} & \overline{\varepsilon}^9 & \overline{\varepsilon}^{10} \\ \varepsilon^{54} & \varepsilon^{12} & \varepsilon^{11} \end{pmatrix} \begin{pmatrix} N_1 \\ N_2 \\ N_3 \end{pmatrix} \varphi$$

$$(N_1, N_2, N_3) \begin{pmatrix} \varepsilon^{64} & \varepsilon^{22} & \varepsilon^{21} \\ \varepsilon^{22} & \overline{\varepsilon}^{20} & \overline{\varepsilon}^{21} \\ \varepsilon^{21} & \overline{\varepsilon}^{21} & \overline{\varepsilon}^{22} \end{pmatrix} \begin{pmatrix} N_1 \\ N_2 \\ N_3 \end{pmatrix} M_{\text{Pl}}$$

$$M_{\text{Pl}} N_4 N_4 \overline{\varepsilon}^{10}$$



$$Q = 5$$

No Yukawas & mixing with N_4

Possible to forbid:

$$N_4 \rightarrow -N_4$$

By reflection symm.

Neutrino Dirac & Majorana Couplings

$$(l_1, l_2, l_3) \begin{pmatrix} \overline{\varepsilon}^9 & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \overline{\varepsilon}^9 & \overline{\varepsilon}^{10} \\ \mathbf{0} & \varepsilon^{12} & \varepsilon^{11} \end{pmatrix} \begin{pmatrix} N_1 \\ N_2 \\ N_3 \end{pmatrix} \varphi$$

$$(N_1, N_2, N_3) \begin{pmatrix} \mathbf{0} & \varepsilon^{22} & \varepsilon^{21} \\ \varepsilon^{22} & \overline{\varepsilon}^{20} & \overline{\varepsilon}^{21} \\ \varepsilon^{21} & \overline{\varepsilon}^{21} & \overline{\varepsilon}^{22} \end{pmatrix} \begin{pmatrix} N_1 \\ N_2 \\ N_3 \end{pmatrix} M_{\text{Pl}}$$

These zeros lead to the Prediction(s)

Quark Sector

Basis: $q^T Y_U u^c h_u$ $q^T Y_D d^c h_d$

Parameterization:

$$Y_U \simeq \begin{pmatrix} a'_1 \epsilon^8 & a_1 \epsilon^5 & 0 \\ 0 & a_2 \epsilon^4 & \epsilon^2 \\ 0 & 0 & 1 \end{pmatrix} \lambda_t^0 ,$$

$$Y_D \simeq \begin{pmatrix} e^{-i\eta_1} & 0 & 0 \\ 0 & e^{-i\eta_2} & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 0 & b_1 \epsilon^3 & 0 \\ b'_1 \epsilon^3 & b_2 \epsilon^2 & b'_2 \epsilon^2 \\ 0 & 0 & 1 \end{pmatrix} \kappa_b \epsilon^2$$

$\eta_{1,2}$ do not contribute to masses. Relevant for CP

Hierarchical Yukawas \rightarrow accurate analytic relations:

$$\lambda_t = \lambda_t^0 [1 + \mathcal{O}(\epsilon^4)] \quad \lambda_b = \kappa_b \epsilon^2 [1 + \mathcal{O}(\epsilon^4)]$$

$$\frac{\lambda_u}{\lambda_t} \simeq \frac{a'_1 \epsilon^8}{\sqrt{1 + (a_1 \epsilon / a_2)^2}}, \quad \frac{\lambda_c}{\lambda_t} \simeq a_2 \epsilon^4 \sqrt{1 + (a_1 \epsilon / a_2)^2}$$

$$\frac{\lambda_d}{\lambda_b} \simeq \frac{b_1 b'_1 \epsilon^4}{\sqrt{b_2^2 + (b_1^2 + b_1'^2) \epsilon^2}}, \quad \frac{\lambda_s}{\lambda_b} \simeq \epsilon^2 \sqrt{b_2^2 + (b_1^2 + b_1'^2) \epsilon^2}$$

CKM elements: $|V_{us}| = |c_u s_d e^{i\eta_1} - s_u c_d e^{i\eta_2}|$

$$|V_{cb}| = c_u \epsilon^2 \frac{|1 - e^{i\eta_2} b'_2 (1 + b_2^2 \epsilon^4)|}{\sqrt{1 + \epsilon^4} \sqrt{1 + b_2'^2 \epsilon^4}} + \mathcal{O}(\epsilon^8), \quad \frac{|V_{ub}|}{|V_{cb}|} = \tan \theta_u = \frac{a_1}{a_2} \epsilon$$

$$\bar{\rho} + i\bar{\eta} = -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} = \frac{c_u c_d e^{i\eta_1} + s_u s_d e^{i\eta_2}}{c_d s_u e^{i\eta_1} - c_u s_d e^{i\eta_2}} \tan \theta_u$$

$$\tan \theta_u = \frac{a_1}{a_2} \epsilon, \quad \tan 2\theta_d = \frac{2b_1 b_2 \epsilon}{b_2^2 - (b_1^2 - b_1'^2) \epsilon^2}$$

Help to find fit

Renormalization from High scale to weak scale

$$\left. \frac{\lambda_{u,c}}{\lambda_t} \right|_{M_t} = \eta_{u,c} \left. \frac{\lambda_{u,c}}{\lambda_t} \right|_{\Lambda} , \quad \left. \frac{\lambda_{d,s}}{\lambda_b} \right|_{M_t} = \eta_{d,s} \left. \frac{\lambda_{d,s}}{\lambda_b} \right|_{\Lambda} ,$$

$$V_{\alpha\beta}|_{M_Z} = \eta_{mix} V_{\alpha\beta}|_{\Lambda} , \quad \text{if } (\alpha\beta) = (ub, cb, td, ts)$$

$$V_{\alpha\beta}|_{M_Z} = V_{\alpha\beta}|_{\Lambda} , \quad \text{if } (\alpha\beta) = (ud, us, cd, cs, tb) ,$$

For:

$$\tilde{M}_t = 172.5 \text{ GeV and } \alpha_3(M_Z) = 0.1179$$

$$\eta_{u,c} \simeq 1.1262 + 0.00187 \cdot \ln\left(\frac{\Lambda}{2 \cdot 10^{16} \text{ GeV}}\right) ,$$

$$\eta_{d,s} \simeq 0.8916 - 0.00143 \cdot \ln\left(\frac{\Lambda}{2 \cdot 10^{16} \text{ GeV}}\right) ,$$

$$\eta_{mix} \simeq 0.89157 - 0.001433 \cdot \ln\left(\frac{\Lambda}{2 \cdot 10^{16} \text{ GeV}}\right) ;$$

- the interpolated expressions which work pretty well for $10^{15} \text{ GeV} < \Lambda < M_{\text{Pl}}$.

Fit – Quark sector

input: $M_t = 172.5 \text{ GeV}, \quad m_b(m_b) = 4.18 \text{ GeV}$

$$\epsilon = 0.21, \quad \{a_1, a'_1, a_2\} = \{0.6974, 1.7065, 1.6606\}, \quad \{\eta_1, \eta_2\} = \{3.01985, -1.3954\}.$$

$$\{b_1, b'_1, b_2, b'_2\} = \{0.47834, 0.54541, 0.45448, 0.59088\}.$$

output:

$$(m_u, m_d, m_s)(2 \text{ GeV}) = (2.16, 4.67, 93) \text{ MeV}, \quad m_c(m_c) = 1.27 \text{ GeV}$$

$$\mu = M_Z : \quad |V_{us}| = 0.225, \quad |V_{cb}| = 0.04182, \quad |V_{ub}| = 0.00369,$$

$$\bar{\rho} = 0.159, \quad \bar{\eta} = 0.3477$$

All results given above are in perfect agreement with experiments

Lepton Sector

$$Y_E \simeq \begin{pmatrix} c_1 \epsilon^4 & 0 & 0 \\ 0 & c_2 \epsilon^2 & 0 \\ 0 & 0 & 1 \end{pmatrix} \kappa_\tau \epsilon^2$$

input:

$$M_\tau = 1.777 \text{ GeV}$$

$$\text{at } \mu = \Lambda, \quad \{c_1, c_2\} \simeq \{0.1437, 1.335\}$$

output:

$$M_e = 0.511 \text{ MeV}, \quad M_\mu = 105.66 \text{ MeV},$$

Neutrino Sector

No important contribution from Y_E

Y_E^{diag} basis \rightarrow Lepton mixing matrix U

$$M_\nu = P U^* P' M_\nu^{Diag} U^\dagger P,$$

$$U = \begin{pmatrix} c_{13}c_{12} & c_{13}s_{12} & s_{13}e^{-i\delta} \\ -c_{23}s_{12} - s_{23}s_{13}c_{12}e^{i\delta} & c_{23}c_{12} - s_{23}s_{13}s_{12}e^{i\delta} & s_{23}c_{13} \\ s_{23}s_{12} - c_{23}s_{13}c_{12}e^{i\delta} & -s_{23}c_{12} - c_{23}s_{13}s_{12}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$$P = \text{Diag} (e^{i\omega_1}, e^{i\omega_2}, e^{i\omega_3}), \quad P' = \text{Diag} (1, e^{i\rho_1}, e^{i\rho_2})$$

Neutrino Dirac & Majorana Matrices

$$m_D \simeq \begin{pmatrix} A\epsilon^9 & 0 & 0 \\ 0 & B_1\epsilon^9 & C_1\epsilon^{10} \\ 0 & B_2\epsilon^{12} & C_2\epsilon^{11} \end{pmatrix} v, \quad M_R \simeq \begin{pmatrix} 0 & a\epsilon^2 & d\epsilon \\ a\epsilon^2 & b & c\epsilon \\ d\epsilon & c\epsilon & \epsilon^2 \end{pmatrix} \bar{c} M_{Pl} \epsilon^{20}$$

See-saw → $M_\nu \simeq -m_D M_R^{-1} m_D^T \simeq \begin{pmatrix} \beta & \gamma & \gamma' \\ \gamma & \alpha^2 & \alpha \\ \gamma' & \alpha & 1 \end{pmatrix} \bar{m}.$

$$M_\nu^{(2,2)} M_\nu^{(3,3)} - (M_\nu^{(2,3)})^2 = 0.$$

Relations → $\tan^2 \theta_{13} = \frac{m_3}{m_2} \left| s_{12}^2 e^{i\rho_1} + \frac{m_2}{m_1} c_{12}^2 \right|$

$$2\delta = \pi - \rho_2 + \text{Arg} \left(s_{12}^2 e^{i\rho_1} + \frac{m_2}{m_1} c_{12}^2 \right)$$

Predict inverted hierarchical neutrinos!

(Z.T. PRD 87, 075026)

$$\cos \rho_1 = \frac{m_1^2 m_2^2 \tan^4 \theta_{13} - m_3^3 (m_1^2 s_{12}^4 + m_2^2 c_{12}^4)}{2m_1 m_2 m_3^2 s_{12}^2 c_{12}^2}$$

$$2\delta = \pm\pi - \rho_2 + \text{Arg} \left(s_{12}^2 e^{i\rho_1} + \frac{m_2}{m_1} c_{12}^2 \right).$$

is incompatible with normal hierarchical neutrino masses.

(IH) in neutrino masses $0.001129 \text{ eV} \lesssim m_3 \lesssim 0.002833 \text{ eV}$

$$0.1002 \text{ eV} \lesssim \sum m_i \lesssim 0.1021$$

($0\nu\beta\beta$) parameter $m_{\beta\beta} = |c_{12}^2 c_{13}^2 m_1 + s_{12}^2 c_{13}^2 m_2 e^{i\rho_1} + s_{13}^2 m_3 e^{i(2\delta+\rho_2)}|$

$$0.01864 \text{ eV} \lesssim m_{\beta\beta} \lesssim 0.0483 \text{ eV}$$

both parameters $\sum m_i$ and $m_{\beta\beta}$ are unequivocally determined
by the m_3 's values.

correlation between $\sum m_i$ and $m_{\beta\beta}$.

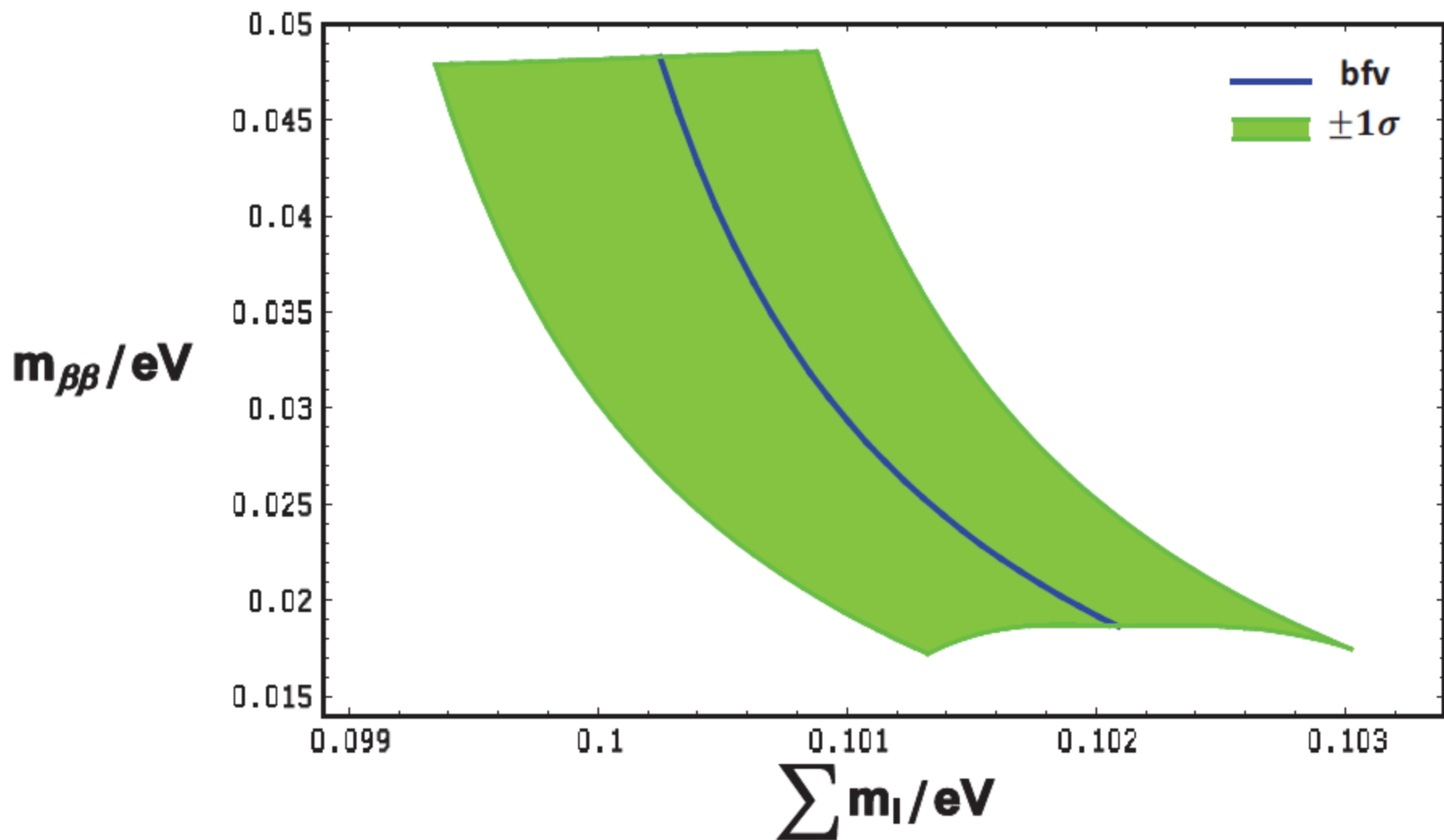


Figure 1: Correlation between $\sum m_i$ and $m_{\beta\beta}$. Solid blue line corresponds to the bfv's of the oscillation parameters [1,2]. Green area corresponds to the cases with oscillation parameters within the 1σ deviations.

All hierarchies, needed values Realized by original parameters' natural values:

**With
input:**

$$\{A, B_1, B_2, C_1, C_2\} \simeq \{2.0236, 2.0236, 1.6189, 2.4283, -0.8094\}$$

$$\{a, b, c, d, \bar{c}\} \simeq \{3.2672e^{i1.5473}, 0.79405e^{i0.0053733}, 0.89097e^{i0.0028735}, 0.15853e^{1.5586}, 0.56333e^{2.9194}\}$$

→ Perfect Fit: $\{\sin^2 \theta_{12}, \sin^2 \theta_{23}, \sin^2 \theta_{13}\} = \{0.3035, 0.57, 0.02235\}$

$$\Delta m_{\text{sol}}^2 = m_2^2 - m_1^2 = 7.39 \cdot 10^{-5} \text{eV}^2, \quad \Delta m_{\text{atm}}^2 = m_2^2 - m_3^2 = 2.492 \cdot 10^{-3} \text{eV}^2$$

$$\{m_1, m_2, m_3\} = \{0.049197, 0.049942, 0.0015\} \text{eV},$$

$$\{\delta, \rho_1, \rho_2\} = \{276^\circ, 91.69^\circ, 11.49^\circ\}, \quad \omega_{1,2,3} = 0$$

$$\{M_{N_1}, M_{N_2}, M_{N_3}\} \simeq \{1.6, 953.5, 32480\} \text{GeV}$$

Suppressed Additional contribution to $(0\nu\beta\beta)$ parameter

$$\left| \sum_{i=1}^3 U_{ei}^2 m_i P_i'^* + \frac{M_{N_1}}{1 + M_{N_1}^2 / \langle p^2 \rangle} U_{eN_1}^2 \right| =$$

$$\left| e^{-0.421i} 0.0362 \text{ eV} + \frac{e^{-0.151i} 2.76 \cdot 10^{-11} M_{N_1}}{1 + M_{N_1}^2 / \langle p^2 \rangle} \right| = 0.0368 \text{ eV}$$

(for $\langle p^2 \rangle = (200 \text{ MeV})^2$)

With $M_{N_1} \simeq 1.6 \text{ GeV}$, and mixing $|U_{eN_1}|^2 \simeq 2.76 \cdot 10^{-11}$

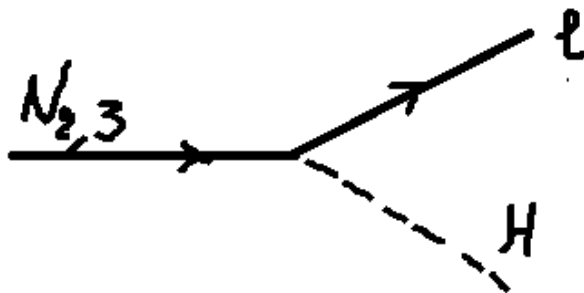
Additional contribution: within $(0.5 - 1.8)\%$, i.e. negligible.

$$\text{for } \langle p^2 \rangle = (100 - 200 \text{ MeV})^2$$

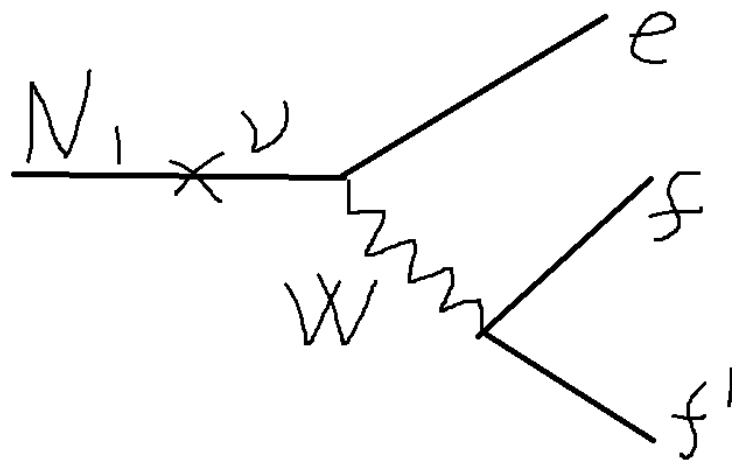
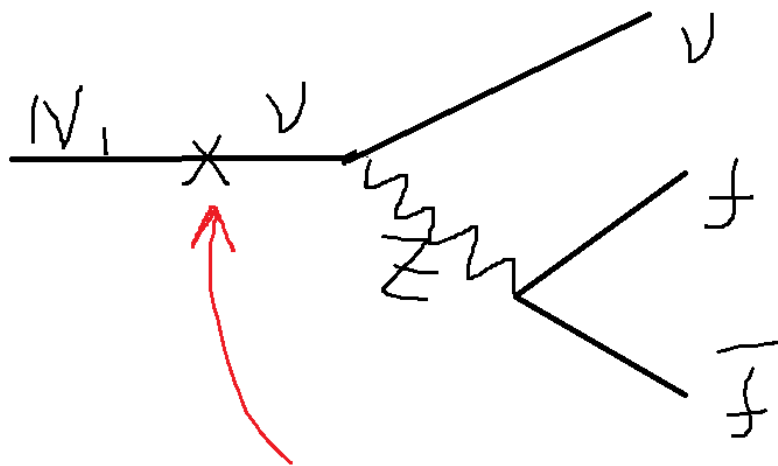
Consistency (with BBN)

$$M_{N_{1,2,3,4}} = \{1.6, 2 \cdot 10^3, 5 \cdot 10^4, 4 \cdot 10^{11}\} \text{ GeV}$$

$N_{2,3}$ Decay quickly



N_1 Decays – mixing with ν 's



$$|U_{iN_1}|^2 \simeq \{2.76, 1.29, 1.09\} \cdot 10^{-11}$$

$$\Gamma(N_1) = \frac{1}{\tau_{N_1}} \simeq \frac{G_F^2 M_{N_1}^5}{16\pi^3} (1.37|U_{1N_1}|^2 + 1.35|U_{2N_1}|^2 + 0.487|U_{3N_1}|^2) \simeq \frac{1}{0.0038 \text{ s}}$$

Consistency (with BBN)

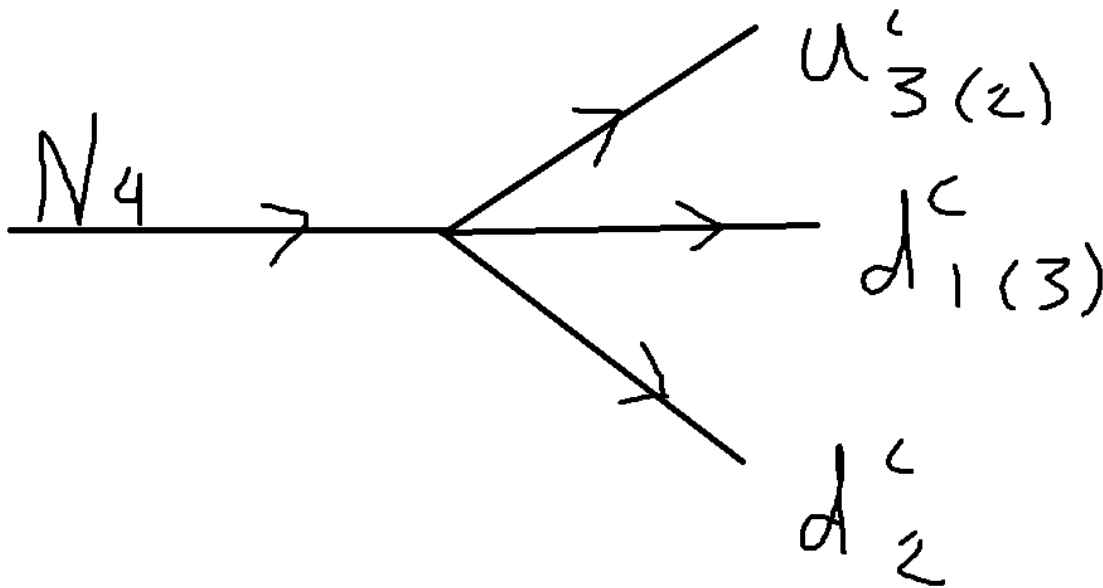
N_4 Decays – due to $d=6$ operator couplings

$$\frac{1}{M_{Pl}^2} (\bar{\epsilon}(N_4 u_3^c)(d_1^c d_2^c) + \epsilon(N_4 u_2^c)(d_2^c d_3^c))$$

Consistent with
symmetry

$$N_4 \rightarrow -N_4$$

$$(q, u^c, d^c) \rightarrow -(q, u^c, d^c)$$



$$\Gamma(N_4) \simeq 1/(10^{-4}\text{sec.})$$

Baryon Asymmetry

Generation of $\frac{n_B - n_{\bar{B}}}{n_\gamma} \approx 10^{-10}$ | asymmetry

Also requires SM extension

Having extension with Right handed neutrinos →

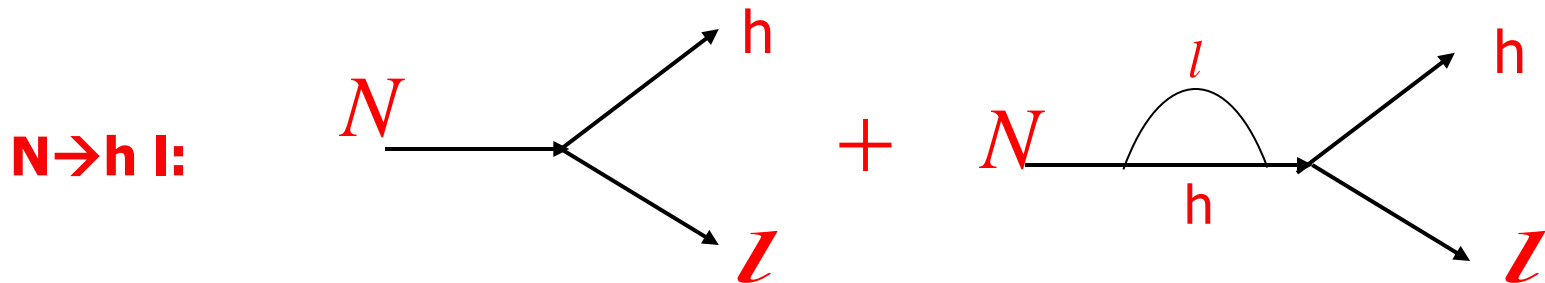
- B-asm. Through leptogenesis

(Fukugita & Yanagida'1986)

Leptogenesis

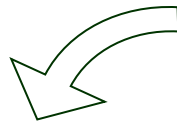
RHNs \rightarrow L, CP viol \rightarrow **Leptogenesis** (Fikugita, Yanagida'86)

By out of equilibrium N-decays



In our considered model: Lightest RHN mass $<$ TeV

Hierarchical neutrinos for leptogenesis require $M_R \geq 10^9 \text{ GeV}$
(Davidson-Ibarra'02 bound)



Hierarchical RHNs will not work for the considered case ...

Alternatively:

- **Quasi Degenerate RHNs** → **Resonant Leptogenesis**

*Flanz et al'96
Pilaftsis'97
Underwood'03*

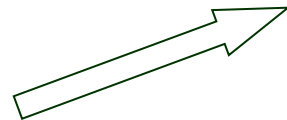


- **Allows low M_R**

With degenerate N's, CP asymmetry:

$$\epsilon_1 = \frac{\text{Im}(\hat{Y}_\nu^\dagger \hat{Y}_\nu)_{21}^2}{(\hat{Y}_\nu^\dagger \hat{Y}_\nu)_{11}(\hat{Y}_\nu^\dagger \hat{Y}_\nu)_{22}} \frac{(M_2^2 - M_1^2) M_1 \Gamma_2}{(M_2^2 - M_1^2)^2 + M_1^2 \Gamma_2^2}$$

*Pilaftsis &
Underwood'03*



Has maximum with $M_1 = M |1 - \delta_N|$, $M_2 = M |1 + \delta_N|$, $\delta_N \ll 1$

For arbitrary M !

Select parameters in M_R matrix \rightarrow

- To get: quasi deg. Two RHNs
- then find: Dirac Yukawas which accommodate neutrino sector
- investigate resonant leptogenesis

It works!

M_R Diagonalization and Spectrum

$$Y_\nu^0 = \begin{pmatrix} \bar{A} & 0 & 0 \\ 0 & \bar{B}_1 & \bar{C}_1 \\ 0 & \bar{B}_2 & \bar{C}_2 \end{pmatrix}, \quad M_R^0 = \begin{pmatrix} 0 & \tilde{n}_2 & \tilde{n}_3 \\ \tilde{n}_2 & \tilde{n}_1 & \tilde{n}_4 \\ \tilde{n}_3 & \tilde{n}_4 & 1 \end{pmatrix} \bar{M}^0$$

Convenient basis: $Y_\nu = \begin{pmatrix} A & 0 & 0 \\ 0 & B_1 & C_1 e^{i\varphi_1} \\ 0 & B_2 & C_2 e^{i\varphi_2} \end{pmatrix},$

$$M_R = \begin{pmatrix} 0 & n_2 & n_3 \\ n_2 & n_1 e^{i\varphi} & 0 \\ n_3 & 0 & 1 \end{pmatrix} \bar{M}, \text{ With } n_3 \ll 1, \text{ for } n_2 \gg |n_1|, n_3^2 \rightarrow$$

$$M_{N_1} \simeq \left(1 - \frac{1}{2n_2} |n_1 - n_3^2|\right) \bar{M} n_2, \quad M_{N_2} \simeq \left(1 + \frac{1}{2n_2} |n_1 - n_3^2|\right) \bar{M} n_2$$

$$M_{N_3} \simeq (1 + n_3^2) \bar{M}.$$

Lighter N_1 and N_2 are quasi-degenerate!

Preliminary Results

One possible parameter selection:

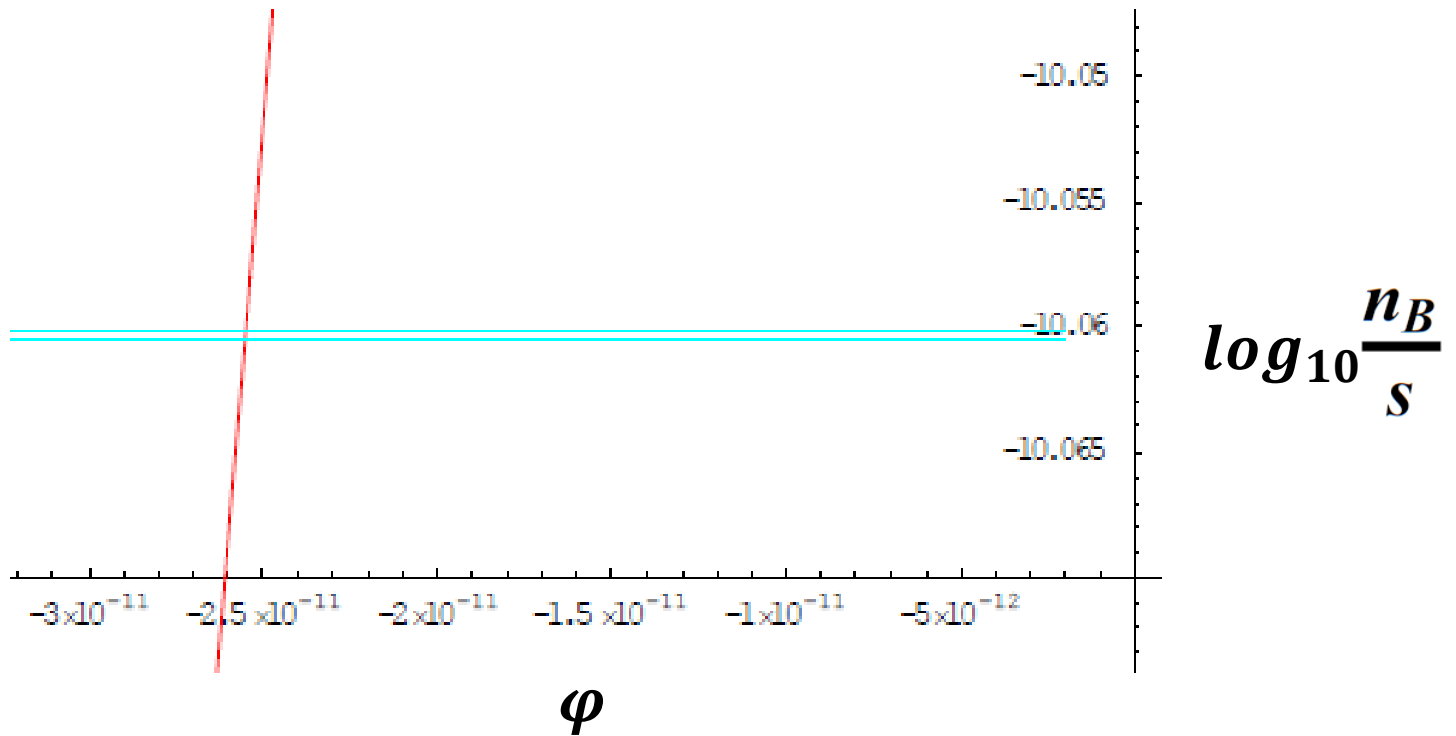
$$Y_\nu = \begin{pmatrix} 7.47 \cdot 10^{-7} & 0 & 0 \\ 0 & 3.57 \cdot 10^{-7} & -5.99 \cdot 10^{-7} - 5.44 \cdot 10^{-7}i \\ 0 & 4.33 \cdot 10^{-7} & 3.89 \cdot 10^{-8} + 4.49 \cdot 10^{-8}i \end{pmatrix}$$

$$M_R = \begin{pmatrix} 0 & 250 & 433.013 \\ 250 & 75 - 9.38 \cdot 10^{-10}i & 0 \\ 433.013 & 0 & 2500 \end{pmatrix} \times \text{GeV}$$

$$M_1 \cong M_2 \cong 250 \text{ GeV}$$

Preliminary Results

Baryon Asymmetry:



How natural are couplings & scales?

$U(1)_F$ symmetry gives:

$$Y_\nu \simeq \begin{pmatrix} \tilde{a}\epsilon^9 & 0 & 0 \\ 0 & \tilde{b}_1\epsilon^{10} & \tilde{c}_1\epsilon^9 \\ 0 & \tilde{b}_2\epsilon^{11} & \tilde{c}_2\epsilon^{12} \end{pmatrix}, \quad M_R \simeq \begin{pmatrix} 0 & \hat{n}_2\epsilon & \hat{n}_3\epsilon^2 \\ \hat{n}_2\epsilon & \hat{n}_1\epsilon^2 & \epsilon \\ \hat{n}_3\epsilon^2 & \epsilon & 1 \end{pmatrix} \hat{n} M_{Pl} \epsilon^{20}$$

From the neutrino sector & leptogenesis,

For $\epsilon = 0.21$ we need:

$$\begin{aligned} \tilde{a} &\simeq 0.94, & b_1 &\simeq 2.1, & b_2 &\simeq 1.2, & \tilde{c}_1 &\simeq 0.75, & \tilde{c}_2 &\simeq 8 \\ \hat{n}_1 &\simeq 0.68, & \hat{n}_2 &\simeq 0.48, & \hat{n}_3 &\simeq 3.9 \\ \hat{n} &\simeq 0.037 \\ \hat{n} M_{Pl} &\simeq 9 \cdot 10^{16} \text{ GeV} \end{aligned}$$

Natural values

Scales unexplained...

Accurate quasi-degeneracy of RHNs requires tunings

SUMMARY

- SM extension with $U(1)_{\text{Flavor}}$ model proposed:
 - **Found** Non-anomalous ch. selection \rightarrow texture zeros;
 - Successful ch. fermion mass hierarchies /mixings;
 - Desirable Neutrino (**inverted hierarchical**) oscillations
 - Satisfactory low scale resonant leptogenesis
- Interesting to extent: to GUTs [like $SU(5)$, $SO(10)$] – more predictive?

Thank You

Backup Slides

- Charged fermion masses & mixings

Observed Noticeable Hierarchies:

$$\lambda_t \sim 1, \quad \lambda_u : \lambda_c : \lambda_t \sim \lambda^8 : \lambda^4 : 1$$

$$\lambda_b \sim \lambda_\tau \sim \frac{m_b}{m_t} \tan \beta, \quad \lambda_d : \lambda_s : \lambda_b \sim \lambda^4 : \lambda^2$$

With $\lambda=0.2$

$$\lambda_e : \lambda_\mu : \lambda_\tau \sim \lambda^5 : \lambda^2 : 1$$

$$V_{us} \approx \lambda, \quad V_{cb} \approx \lambda^2, \quad V_{ub} = \lambda^4 - \lambda^3$$

What is origin of these hierarchies?

Is there any relation or sum rule?

Why three families?

Within SM no answer to these questions...

Evidences for New Physics: Neutrino Data

- Origin of these scales and mixings?

Unexplained in SM

$$\leftarrow m_\nu \lesssim 10^{-4} \text{ eV}$$

$$m_\nu \sim \frac{M_{EW}^2}{M_{Pl}}$$

**Without New
Physics**

Neutrino masses via see-saw

+ RHN - V_R

→ Oscillations

→ Leptogenesis

$V^c \equiv N \square (1, 1, 0)$

SM singlet

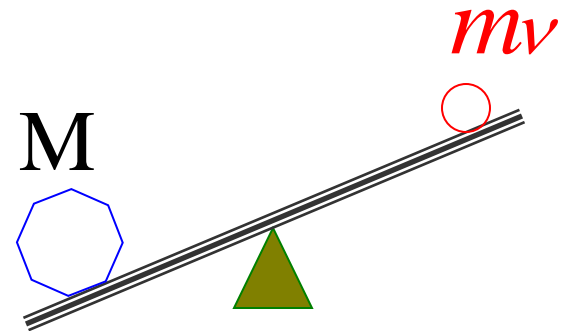
$l N \langle H \rangle$

$M N N$

→ $\Delta L=2$ Lepton number viol.

$$\begin{pmatrix} 0 & \langle H \rangle \\ \langle H \rangle & M \end{pmatrix}$$

$$m_\nu \sim \frac{\langle H \rangle^2}{M}$$



$$M_N \simeq M$$

$$M \sim 10^{14} \text{ GeV} \rightarrow m_\nu \sim \text{few} \cdot 0.01 \text{ eV}$$

Some related works:

- Within MSSM, anom. free $U(1)_F$'s with successful $Y_{U,D,E}$
Dudas, Pokorski, Savoy, hp/9504292;
- Within MSSM & SU(5) GUT, some examples/models of
anom. free $U(1)_F$'s : *Mu-Chun Chen, et al, ph/0612017, 0801.0248;*

Backup Slides for Leptogenesis

No apriory reason to expect Matter-antimatter asymmetry..

Early Universe → 50% -- 50%

$$\frac{n_B - n_{\bar{B}}}{n_\gamma} \approx 10^{-10}$$

(with units $n_\gamma = 1$)

For 10.000.000.000 Baryons \leftrightarrow 9.999.999.999 antiBaryons

How/why such asymmetry Emerges???

Sakharov Conditions (1967) *for Baryogenesis*

1. B-number violation
2. C- and CP-violation
3. Out of thermal Equilibrium

(necessary conditions)

-- *SM meets 3 conds. But too small asymmetry!*

-- *GUT \leftrightarrow sphaleron washout problem (?)*

-- *see Babu & Mohapatra'2012*

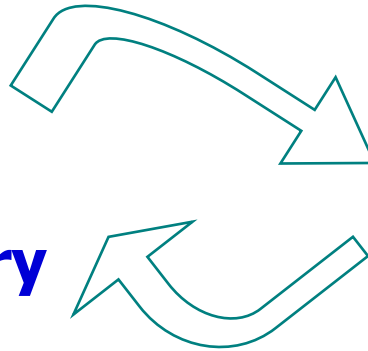
GUT baryogenesis revamped!

Needed Physics Beyond **SM** (Standard Model)

-- Neutrino Sector

-- Baryon asymmetry

...



Are related?

interesting to try!

-- Neutrino mass **$\nu\nu$ -operator** $\rightarrow \Delta L \neq 0$

- Sphalerons **$\Delta(B-L)=0 \rightarrow \Delta B \neq 0$** (good!)

Remaining 2 conds. \sim details of Leptogenesis

(Fukugita & Yanagida'1986)